

$$1. \textcircled{1} \sum_{x=0}^{10} \binom{10}{x} \left(\frac{1}{10}\right)^x \left(\frac{9}{10}\right)^{10-x} = \sum_{x=0}^{10} C_{10}^x \left(\frac{1}{10}\right)^x \left(\frac{9}{10}\right)^{10-x}$$

$f_x(x)$	$x=0$	$b(0; 10, \frac{1}{10}) \approx 0.3487$	$x=6$	$b(6; 10, \frac{1}{10}) \approx 0.0001$
	$x=1$	$b(1; 10, \frac{1}{10}) \approx 0.3874$	$x=7$	$b(7; 10, \frac{1}{10}) \approx 0$
	$x=2$	$b(2; 10, \frac{1}{10}) \approx 0.1937$	$x=8$	$b(8; 10, \frac{1}{10}) \approx 0$
	$x=3$	$b(3; 10, \frac{1}{10}) \approx 0.0574$	$x=9$	$b(9; 10, \frac{1}{10}) \approx 0$
	$x=4$	$b(4; 10, \frac{1}{10}) \approx 0.0112$	$x=10$	$b(10; 10, \frac{1}{10}) \approx 0$
	$x=5$	$b(5; 10, \frac{1}{10}) \approx 0.0015$		

$$\textcircled{2} \mu = np = 10 \times \frac{1}{10} = 1$$

$$\textcircled{3} \sigma^2 = np(1-p) = 10 \times \frac{1}{10} \times \frac{9}{10} = \frac{9}{10}$$

$$\sigma = \sqrt{\frac{9}{10}} = 0.9487$$

$$\textcircled{4} f_y(k) = \frac{C_{10}^k C_{10-k}^9}{C_{10}^{100}} \rightarrow$$

$f_y(0) = 0.3305$	$f_y(5) = 6.378e-4$	$f_y(10) = 5.77e-14$
$f_y(1) = 0.408$	$f_y(6) = 3.1e-5$	
$f_y(2) = 0.2015$	$f_y(7) = 8.144e-7$	
$f_y(3) = 0.0518$	$f_y(8) = 1.0411e-8$	
$f_y(4) = 0.0076$	$f_y(9) = 5.1992e-11$	

⑤ 期望值與標準差與放不放回無關

$$E[Y] + \text{std}[Y] \approx 1 + 0.8487 \approx 1.8487$$

2. ①

$$f(w) = P(100; 1) = \frac{e^{-1} 1^{100}}{100!} = 3.9419e-159$$

②

$$E[w] = \lambda t = 100 \times 1 = 100$$

$$\mu = \sigma^2 = 100 \quad \sigma = \sqrt{100} = 10$$

$$E[w] + \text{std}[w] = 110$$

④

$$P(w > 120) = 0.9999$$

⑤

不符合. 偏差值太大