Homework #5 Due by Thursday 4/11, 11:59pm

Submission instructions:

- 1. You should turn in 5 '.py' files: one for each question. Name your files: 'YourNetID_hw5_q1.py', 'YourNetID_hw5_q2.py', etc. Note: your netID follows an abc123 pattern, not N12345678.
- 2. In this assignment, we provided 'ArrayList.py', 'ArrayStack.py', 'ArrayQueue.py' and 'ArrayDeque.py' files. **You are not allowed to put any changes in these files.**

In questions where you need to **use** ArrayStack, ArrayQueue or ArrayDeque objects, make the definition in a separate file. That is, for example, you should have an **import** statement in the file that define functions that are using Stacks (don't write the functions in 'ArrayStack.py').

- 3. You should submit your homework via Gradescope. For Gradescope's autograding feature to work:
 - a. Name all functions and methods exactly as they are in the assignment specifications.
 - b. Make sure there are no print statements in your code. If you have tester code, please put it in a "main" function and do not call it.
 - c. You don't need to submit the 'ArrayList.py', 'ArrayStack.py', 'ArrayQueue.py' and 'ArrayDeque.py' files

Question 1:

Implement an interpreter-like **postfix calculator**. Your program should repeatedly:

- Print a prompt to the user. The prompt should be: '-->'
- Read an expression from the user
- Evaluate that expression
- Print the result

Your calculator should support 2 kinds of expressions:

- 1. <u>Arithmetic expressions</u> are given in postfix notation. The tokens of the expression are separated by a space.
- 2. **Assignment expressions** are expression of the form:

```
variable_name = arithmetic_expression
```

When evaluated, it first evaluates the *arithmetic_expression* (given in postfix notation), and then it associates that value with *variable_name* (in a data structure of your choice).

Notes:

- The value of an assignment expression, is the name of the variable being assigned.
- Assume that the *variable_name*, the '=' symbol, and the *arithmetic_expression* are separated by a space.

Notes:

- 1. Arithmetic expressions can contain variable names, for referencing to values associated with variables that were defined before.
- 2. You may assume that the input the user enters, is valid. That is, the arithmetic expressions are legal; all variables used in an expression were already defined; etc.
- 3. The program should keep reading, and evaluating expressions until the user types 'done()'.

Your program should interact with the user **exactly** as demonstrated in the example below:

```
--> 4
4
--> 5 1 -
4
--> x = 5 1 -
x
--> x
4
--> x x +
8
--> y = 1 x + 3 4 * - 2 /
y
--> y
-3.5
--> done()
```

Question 2:

Give a Python implementation for the *MaxStack* ADT. The *MaxStack* ADT supports the following operations:

- MaxStack(): initializes an empty MaxStack object
- maxS.is_empty(): returns True if maxS does not contain any elements, or False otherwise.
- len (maxS): Returns the number of elements in maxS
- maxS.push(e): adds element e to the top of maxS.
- maxS.top(): returns a reference to the top element of maxS, without removing it; an exception is raised if maxS is empty.
- maxS.pop(): removes and return the top element from maxS; an exception is raised if maxS is empty.
- maxS.max(): returns the element in maxS with the largest value, without removing it; an exception is raised if maxS is empty.

Note: Assume that the user inserts only integers to this stack (so they could be compared to one another, and a maximum data is well defined).

For example, your implementation should follow the behavior below:

```
>>> maxS = MaxStack()
>>> maxS.push(3)
>>> maxS.push(1)
>>> maxS.push(6)
>>> maxS.push(4)
>>> maxS.max()
6
>>> maxS.pop()
4
>>> maxS.pop()
6
>>> maxS.pop()
6
>>> maxS.pop()
```

Implementation Requirements:

- 1. For the representation of MaxStack objects, your data members should be:
 - A Stack of type ArrayStack
 - Additional $\theta(1)$ space for additional data members, if needed
- 2. Your implementation should support the max operation in $\theta(1)$ worst-case time. For all other Stack operation, the running time should remain as it was in the original implementation.

<u>Hint</u>: You may want to store a tuple, as elements of the ArrayStack. That is, to attach to every "real" data in this stack some additional information.

Question 3:

Give a Python implementation for the *MidStack* ADT. The *MidStack* ADT supports the following operations:

- MidStack (): initializes an empty MidStack object
- midS.is_empty(): returns True if S does not contain any elements, or False otherwise.
- len(midS): Returns the number of elements midS
- midS.push(e): adds element e to the top of midS.
- midS.top(): returns a reference to the top element of midS, without removing it; an exception is raised if S is empty.
- midS.pop(): removes and returns the top element from midS; an exception is raised if midS is empty.
- midS.mid_push(e): adds element e in the middle of midS. That is, assuming there are n elements in S: In the case n is even, e would go exactly in the middle. If n is odd, e will go after the $\frac{n+1}{2}th$ element.

For example, your implementation should follow the behavior as demonstrated in the two execution examples below:

```
>>> midS = MidStack()
                                  >>> midS = MidStack()
>>> midS.push(2)
                                  >>> midS.push(2)
>>> midS.push(4)
                                  >>> midS.push(4)
>>> midS.push(6)
                                  >>> midS.push(6)
>>> midS.push(8)
                                  >>> midS.push(8)
>>> midS.mid push(10)
                                  >>> midS.push(10)
>>> midS.pop()
                                  >>> midS.mid push(12)
8
                                  >>> midS.pop()
>>> midS.pop()
                                  10
                                  >>> midS.pop()
>>> midS.pop()
10
                                  >>> midS.pop()
>>> midS.pop()
                                  12
                                  >>> midS.pop()
>>> midS.pop()
                                  >>> midS.pop()
                                  >>> midS.pop()
```

Implementation Requirements:

- 1. For the representation of MidStack objects, your data members should be:
 - A Stack of type ArrayStack
 - A double ended queue of type ArrayDeque
 - Additional $\theta(1)$ space for additional data members, if needed
- 2. Your implementation should support the mid_push operation in $\theta(1)$ amortized time. For all other Stack operation, the running time should remain as it was in the original implementation (That is, $\theta(1)$ amortized for push and pop, and $\theta(1)$ worst-case for top, len and is empty).

Question 4:

Give an alternative implementation for the *Queue* ADT.

Implementation Requirements:

- 1. For the representation of Queue objects, your data members should be:
 - Two Stacks of type ArrayStack
 - Additional $\theta(1)$ space for additional data members, if needed
- 2. Any sequence of n enqueue and dequeue operations (starting with an empty queue) should run in worst-case of $\theta(n)$ altogether.

Question 5:

Implement the following function:

```
def permutations(lst)
```

The function is given a list lst of integers, and returns a list containing all the different permutations of the elements in lst. Each such permutation should be represented as a list.

```
For example, if lst=[1, 2, 3], the call permutations (lst) could return [[1, 2, 3], [2, 1, 3], [1, 3, 2], [3, 2, 1], [3, 1, 2], [2, 3, 1]]
```

Implementation Requirements:

- 1. Your implementation should be **non-recursive**.
- 2. Your implementation is allowed to use a Stack, a Queue, and $\theta(1)$ additional space.

Hint: Use the stack to store the elements yet to be used to generate the permutations and use the queue to store the (partial) collection of permutations generated so far.