

### Question 1:

Consider the following two implementations of a function that if given a list, `lst`, create and return a new list containing the elements of `lst` in reverse order.

```
def reverse1(lst):  
    1 rev_lst = []  
    1 i = 0  
    O(n) while (i < len(lst)):  
        rev_lst.insert(0, lst[i]) O(n)  
        i += 1  
    return rev_lst
```

$O(n^2)$

```
def reverse2(lst):  
    1 rev_lst = []  
    1 i = len(lst) - 1  
    O(n) while (i >= 0):  
        rev_lst.append(lst[i])  
        i -= 1  
    return rev_lst
```

$O(1)$  depends on  $n$   $O(1)$

If `lst` is a list of  $n$  integers,

1. What is the worst case running time of `reverse1(lst)`? Explain of your answer.  
 $O(n^2)$ ,  $O(n)$  for the while loop &  $O(n)$  for insert operation b/c it shifts  $n$  times
2. What is the worst case running time of `reverse2(lst)`? Explain of your answer.  
 $O(n)$ ,  $O(n)$  for the while loop and  $O(1)$  for the append  
 $O(1) * O(n) = O(n)$

q2

1) First, an empty array means that its capacity is  $\geq 1$ , therefore each append call will cost  $O(1)$  time. However after  $n$  calls, the append function will cost  $O(n)$  times because the capacity of the array will need expansion ("doubling"). We will not be doubling because we already have capacity  $[2n]$ .

After appending  $n$  times, the array is going to have  $n$  items to pop. Therefore, we will call  $\text{pop}()$   $n$  times and each time it will cost  $O(1)$ .

$$2(n * O(1)) = 2n = O(n)$$

2) After  $n$  appends for an array,  $\text{Capacity} := n$ . Suppose we call  $\text{pop}$   $n/2$  times. By the definition of the strategy given, the array will resize its capacity to  $n/2$ . This follows another sequence of  $n$  appending and  $n/2$  popping until the capacity shrinks to 1.

Each resize =  $O(n)$  and it happens  $\frac{n}{2}$  times

$$\frac{n}{2} * O(n) = \frac{1}{2}n^2 = \Omega(n^2)$$

3.6

My code uses  $O(n)$  runtime.

The first for loop iterates over list once  
 $n$  times  $= O(n)$ .

The second for loop iterates over count  
once which has  $n$  elements  $\therefore = O(n)$

} note that  
 $n$  here has a  
different value  
than  $n$  in the  
1st loop.

$$O(n) + O(n)$$

Overall complexity

$$= O(n) \text{ (linear time)}$$

4.9

Worst case, value is not in list.

Each remove call will cost  $O(n)$

to iterate over all  $n$  items of the list

and will be called  $n$  times.

$$O(n) \cdot n = O(n^2)$$

4.1

My code has 2 for loops (not nested).

Both of which contain operations that  
take constant time. However they run  
 $O(n)$  times

$$= O(n)$$