

Is (S, R) a poset if S is a set of all people in the world and $(a, b) \in R$, where a and b are people if

i) a weighs more than b

$(a, a) \in R \Rightarrow a$ weighs more than a

not Reflexive

not a poset

$\leq \rightarrow$ Relation

Def:- The elements a and b of a poset (S, R) are **comparable** if either aRb or bRa

When a and b are elements of S such that neither aRb or bRa are called **incomparable**

$(\mathbb{Z}^+, |)$ 3 and 9 are comparable to each other
 $\therefore 3|9$

2/4
3/4

5 and 7 $5 \nmid 7$ and $7 \nmid 5$ so
 \rightarrow **incomparable**

Def:- If (S, R) is a poset and every two elements of S are comparable. S is called a **totally ordered** or **linearly ordered set**.

The poset (\mathbb{Z}, \leq) is totally ordered

$\dots -5 < -4 < -3 < -2 < -1 < 0 < 1 < 2 < 3 < 4 < 5 \dots$

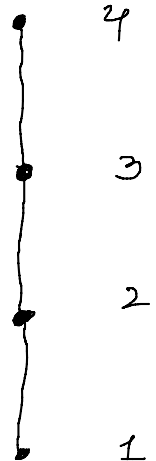
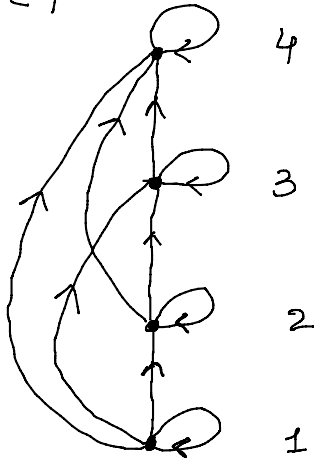
$$\dots -5 \leq -4 \leq -3 \leq -2 \leq -1 \leq 0 \leq 1 \leq 2 \leq 3 \leq 4 \leq 5 \dots$$

A totally ordered set is also called a chain.

Hasse Diagram :-

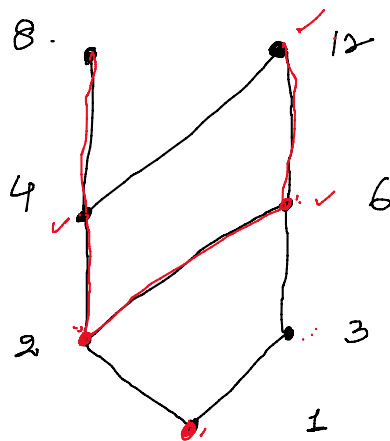
$$\{1, 2, 3, 4\}, \leq$$

$$\begin{array}{lll} 1 \leq 1 & 2 \leq 2 & 3 \leq 3 & 4 \leq 4 \\ 1 \leq 2 & 2 \leq 3 & 3 \leq 4 & \\ 1 \leq 3 & 2 \leq 4 & & \\ 1 \leq 4 & & & \end{array}$$



Reflexive ✓ a.k.b
antisymmetric
Transitive ✓

$S = \{1, 2, 3, 4, 6, 8, 12\}, \mid \rightarrow \text{divisibility}$



Hasse Diagram