

$$\omega_0 = \frac{1}{\sqrt{LC}} \quad \& \quad f_0 = \frac{\omega_0}{2\pi} \quad \& \quad a = \frac{R}{2L} \quad \& \quad \zeta = \frac{a}{\omega_0}$$

Given  $L_1 = 1\text{mH}$ ,  $C_1 = 1\text{nF}$ ,  $\& \quad R_1 = 330\Omega; 910\Omega; 2.2\text{k}\Omega; 4.5\text{k}\Omega$

For  $R_1 = 330\Omega$ :  $\omega_0 = \frac{1}{\sqrt{0.001\text{H} \cdot (1 \times 10^{-9}\text{F})}} = \frac{1}{\sqrt{1 \times 10^{-12}\text{s}^2}}$

\*  $1\text{F} = \frac{\text{C}}{\text{V}} \quad \& \quad 1\text{Hz} = \frac{1}{\text{s}}$

$\text{H} = \text{kg} \cdot \text{m}^2 \cdot \text{s}^{-2} \cdot \text{A}^{-2}$

$\text{Ohms} = \text{kg} \cdot \text{m}^2 \cdot \text{s}^{-3} \cdot \text{A}^{-2}$

$\omega_0 = \frac{1 \text{ rad}}{1 \times 10^{-6} \text{ s}}$

$f_0 = \frac{\frac{1}{1 \times 10^{-6} \text{ s}}}{2\pi} = \frac{1}{2\pi \times 10^{-6}} \text{ Hz}$

$a = \frac{330\Omega}{2 \cdot 0.001\text{H}} = 165000 \frac{\text{rad}}{\text{sec}}$

$\zeta = \frac{165000 \frac{\text{rad}}{\text{sec}}}{\frac{1}{1 \times 10^{-6}} \frac{\text{rad}}{\text{sec}}} = 0.165$

For  $R_1 = 910\Omega$ :  $\omega_0$  stays the same for all  $R_1$ 's  $\& \quad f_0$  also

$a = \frac{910\Omega}{2 \cdot 0.001\text{H}} = 455000 \frac{\text{rad}}{\text{sec}}$

$\zeta = \frac{455000 \frac{\text{rad}}{\text{sec}}}{\frac{1}{1 \times 10^{-6}} \frac{\text{rad}}{\text{sec}}} = 0.455$

For  $R_1 = 2.2\text{k}\Omega$ :  $a = \frac{2200\Omega}{0.002\text{H}} = 1,100,000 \frac{\text{rad}}{\text{sec}}$

$\zeta = \frac{1,100,000 \frac{\text{rad}}{\text{sec}}}{\frac{1}{1 \times 10^{-6}} \frac{\text{rad}}{\text{sec}}} = 1.1$

For  $R_1 = 4.5\text{k}\Omega$ :  $a = \frac{4500\Omega}{0.002\text{H}} = 3,750,000 \frac{\text{rad}}{\text{sec}}$

$\zeta = \frac{3,750,000 \frac{\text{rad}}{\text{sec}}}{\frac{1}{1 \times 10^{-6}} \frac{\text{rad}}{\text{sec}}} = 3.75$

$R_1 = 330\Omega \& 910\Omega$  are underdamped;  $R_1 = 2.2\text{k}\Omega$  is critically damped

$R_1 = 4.5\text{k}\Omega$  is overdamped