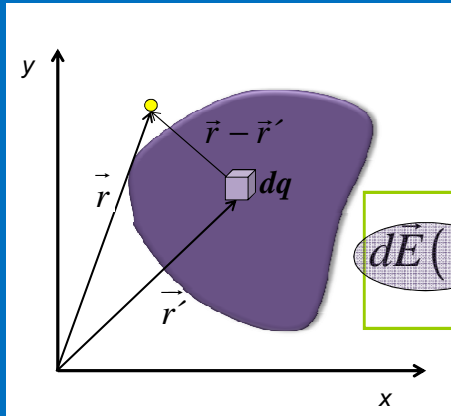


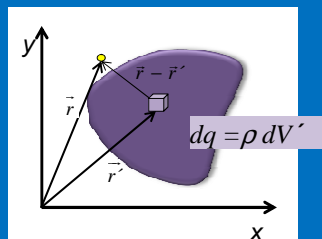
## Distribuciones continuas de carga



$$\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{Q}{|\vec{r} - \vec{r}'|^3} \vec{r} - \vec{r}'$$

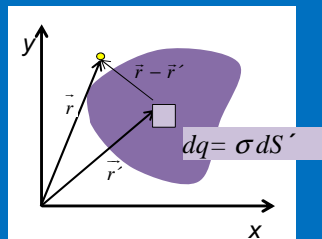
$$d\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{dq}{|\vec{r} - \vec{r}'|^3} (\vec{r} - \vec{r}')$$

$$\vec{E}(\vec{r}) = \int d\vec{E}(\vec{r})$$

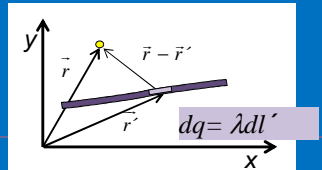


$$d\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{dq}{|\vec{r} - \vec{r}'|^3} (\vec{r} - \vec{r}')$$

$$\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_V \frac{\rho dV'}{|\vec{r} - \vec{r}'|^3} (\vec{r} - \vec{r}')$$

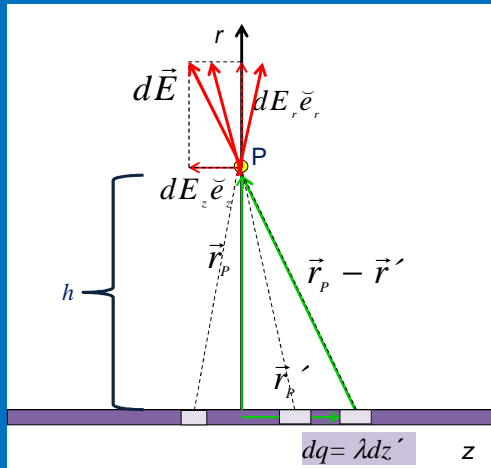


$$\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_A \frac{\sigma dS'}{|\vec{r} - \vec{r}'|^3} (\vec{r} - \vec{r}')$$



$$\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_L \frac{\lambda dl'}{|\vec{r} - \vec{r}'|^3} (\vec{r} - \vec{r}')$$

## Campo E de una línea de carga infinita



$$\vec{E}(\vec{r}) = \int d\vec{E}(\vec{r})$$

$$\vec{E}(\vec{r}_p) = \frac{1}{4\pi\epsilon_0} \int_L \frac{dq}{|\vec{r}_p - \vec{r}'|^3} (\vec{r}_p - \vec{r}')$$

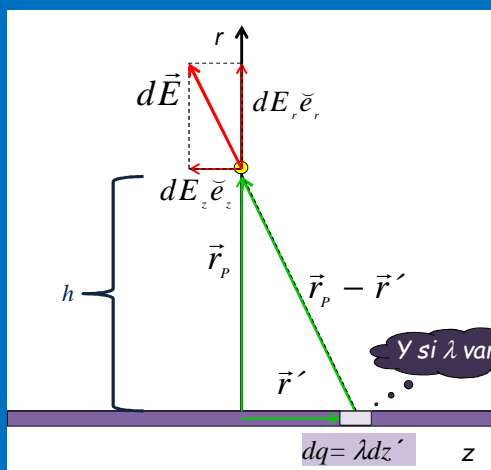
$$\left. \begin{aligned} \vec{r}_p &= h\vec{e}_r \\ \vec{r}' &= z'\vec{e}_z \end{aligned} \right\} \begin{aligned} \vec{r}_p - \vec{r}' &= h\vec{e}_r - z'\vec{e}_z \\ |\vec{r}_p - \vec{r}'| &= \sqrt{h^2 + z'^2} \end{aligned}$$

$$\vec{E}(\vec{r}_p) = \int d\vec{E}(\vec{r}_p) = \int dE_r \vec{e}_r + \int dE_z \vec{e}_z$$

$$dE_r(\vec{r}_p) = k \frac{hdq}{|\vec{r}_p - \vec{r}'|^3} = k \frac{h\lambda dz'}{(h^2 + z'^2)^{3/2}}$$

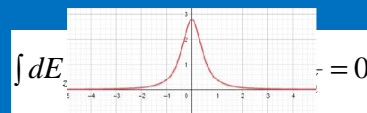
$$dE_z(\vec{r}_p) = k \frac{-z'dq}{|\vec{r}_p - \vec{r}'|^3} = k \frac{-z'\lambda dz'}{(h^2 + z'^2)^{3/2}}$$

## Campo E de una línea de carga infinita

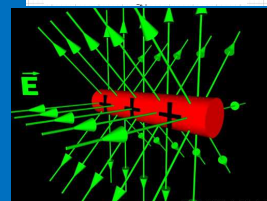


$$\vec{E}(\vec{r}_p) = \int d\vec{E}(\vec{r}_p) = \int dE_r \vec{e}_r + \int dE_z \vec{e}_z$$

$$\int dE_r(\vec{r}_p) = \int_{-\infty}^{\infty} k \frac{h\lambda dz'}{(h^2 + z'^2)^{3/2}} = k \frac{2\lambda}{h}$$



$$\vec{E}(\vec{r}_p) = k \frac{2\lambda}{h} \vec{e}_r$$

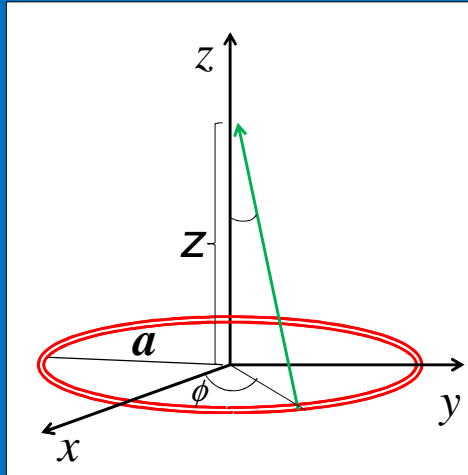


Campo eléctrico a una distancia r de la distr. lineal

$$\vec{E}(\vec{r}) = k \frac{2\lambda}{r} \vec{e}_r = \frac{1}{4\pi\epsilon_0} \frac{2\lambda}{r} \vec{e}_r$$

Y si  $\lambda$  varia?

## Campo E de un anillo cargado sobre el eje de simetría



$$\vec{E}(\vec{r}_p) = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{|\vec{r}_p - \vec{r}'|^2} (\vec{r}_p - \vec{r}') \quad \frac{dq = \lambda dl = \lambda a d\phi}{|\vec{r}_p - \vec{r}'| = \sqrt{z^2 + a^2}}$$

$$\vec{E}(z) = E_z \vec{e}_z = \frac{1}{4\pi\epsilon_0} \frac{\lambda z 2\pi a}{(z^2 + a^2)^{3/2}} \vec{e}_z$$

Si  $z=0$ ?

Si  $z \gg a$ ?

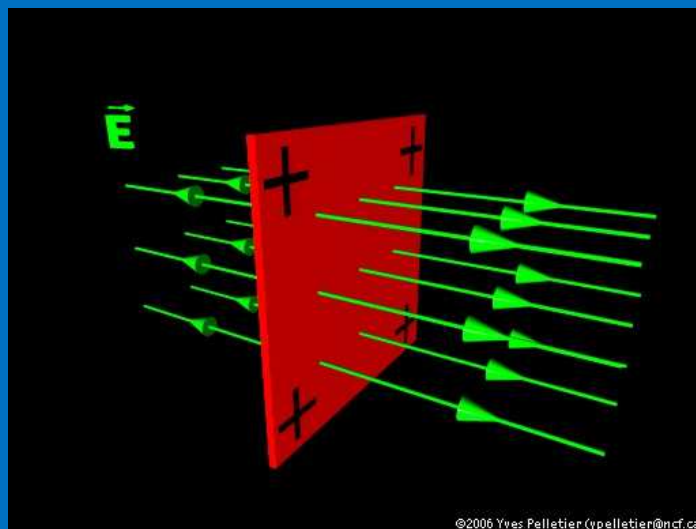
Si  $\lambda$  varia?

Si quiero ver qué pasa en otro lugar?

Si se tratara de un disco?



## Campo eléctrico de un plano infinito



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