## Deep Imbalanced Regression

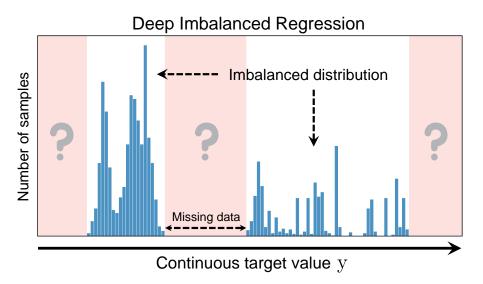
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### Overview



## **Problem Settings**

- $\{(\mathbf{x}_i, y_i)\}_{i=1}^N$ : training set
- $\mathbf{x}_i \in \mathbb{R}^d$ : input
- $y_i \in \mathcal{Y}$ : continuous label or target
- $b_i \in \mathcal{B}$ : discrete label or target
- $\mathcal{Y} \subset \mathbb{R}$ : continuous label space
- $\mathfrak{B} = \{1, \dots, M\} \subset \mathbb{Z}^+$ : index space
  - lacktriangle divides  $\mathcal Y$  into M groups (bins) with equal intervals  $[t_j,t_{j+1})$
  - $\{[t_0, t_1), \ldots, [t_{M-1}, t_M)\}$ : discrete label space
  - $t_k \in \mathcal{Y}$
  - minimum resolution
    - ★ e.g.,  $\delta y \triangleq t_{j+1} t_j = 1$  in age estimation
- $\hat{y}_i = g(\mathbf{z}_i) \in \mathbb{R}$ : predicted continuous label
- $\mathbf{z}_i = f(\mathbf{x}_i; \theta) \in \mathbb{R}^{d'}$ : learned representation
- $\theta$ : trainable model parameters

#### **Evaluation**

- Divide target space into disjoint regions (bins)
  - ► *Many-shot*: > 100 training examples
  - ▶ *Medium-shot*: 20-100 training examples
  - ► Few-shot: < 20 training examples
  - ► Zero-shot: 0 training examples
  - Inspired by Liu et al. 2019

#### Metrics

- Mean Absolute Error (MAE)
- Mean Squared Error (MSE)
- ► Pearson Correlation (PCC)
- Geometric Mean Error (GM)

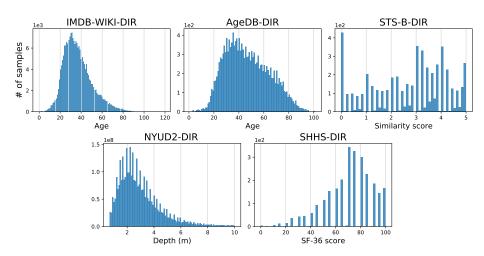
$$GM = \sqrt[n]{\prod_{i=1}^{n} |y_i - \hat{y}_i|}$$

★ Pros: + fairness (uniformity) in prediction

## Datasets - Overview

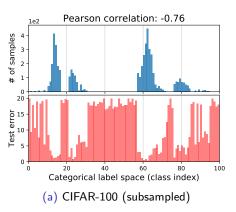
| Dataset       | Target type            | Target ran | ge | Bin size | Max bin densit       | у | Min bin density    | / # Training set             | # Val. set | # Test set                    |
|---------------|------------------------|------------|----|----------|----------------------|---|--------------------|------------------------------|------------|-------------------------------|
| IMDB-WIKI-DIR | Age                    | 0 - 186    |    | 1        | 7,149                | Π | 1                  | 191,509                      | 11,022     | 11,022                        |
| AgeDB-DIR     | Age                    | 0 - 101    |    | 1        | 353                  |   | 1                  | 12,208                       | 2,140      | 2,140                         |
| STS-B-DIR     | Text similarity score  | 0 - 5      |    | 0.1      | 428                  | - | 1                  | 5,249                        | 1,000      | 1,000                         |
| NYUD2-DIR     | Depth                  | 0.7 - 10   |    | 0.1      | $1.46 \times 10^{8}$ | T | $1.13\times10^{6}$ | $ 50,688 (3.51 \times 10^9)$ | -          | 654 (8.70 × 10 <sup>5</sup> ) |
| SHHS-DIR      | Health condition score | 0 - 100    |    | 1        | 275                  | Τ | 0                  | 1,892                        | 369        | 369                           |

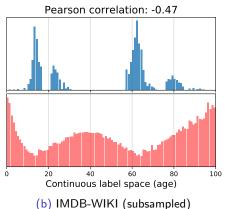
## (Training) Datasets - Label Distributions



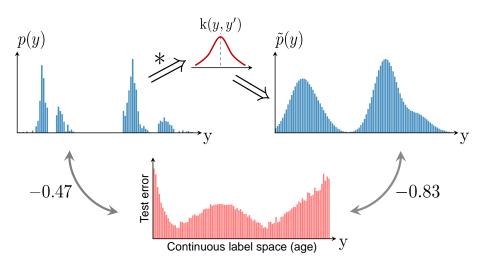
Label Distribution Smoothing (LDS)

## Test Error on Categorical vs. Continuous Label Space





## The LDS Algorithm



- Starting points
  - lacktriangledown Continuity in the **feature** space

- Starting points
  - Ontinuity in the target space ←→ Continuity in the feature space

- Starting points
  - Ontinuity in the target space ←→ Continuity in the feature space
  - ② Data balance ⇒ close feature statistics of nearby targets
- Feature statistics: mean and variance w.r.t. each bin

$$\{\boldsymbol{\mu}_b, \boldsymbol{\sigma}_b\}_{b=1}^B$$

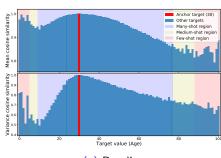
- Starting points
  - Ontinuity in the target space ←→ Continuity in the feature space
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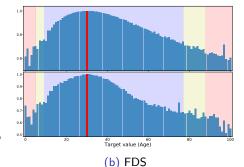
$$\{\boldsymbol{\mu}_b, \boldsymbol{\sigma}_b\}_{b=1}^B$$

- (next slides) Feature statistics similarity: cosine similarity of feature statistics between one anchor bin  $b_0$  and all other bins
  - $b_0 = 0, 30, 60, 90$  (age): chosen anchor bins
  - ▶ different target densities: many (>100), medium (20-100), few (<20) examples</p>
  - ▶ task: person's picture → person's age
  - data source: IMDB-WIKI

# Feature statistics similarity (1/4)

#### Anchor age 30



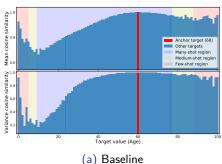


- (a) Baseline
- High similarity in neighbourhood
- High similarities with further regions
- Lower similarities with some closer regions

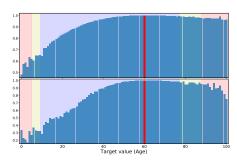
- Improved feature statistics calibration:
  - ► High similarity only in neighbourhood
  - "The further the region the lower the similarity"
  - More gradual similarity change

# Feature statistics similarity (2/4)

#### Anchor age 60



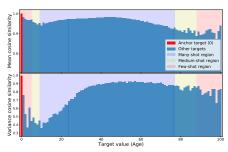
- 4
- High similarity in neighbourhood
- High similarities with further regions
- Lower similarities with some closer regions



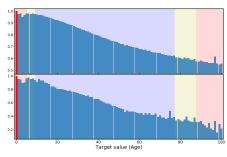
- (b) FDS
- Improved feature statistics calibration:
  - High similarity only in neighbourhood
  - "The further the region the lower the similarity"
  - More gradual similarity change

# Feature statistics similarity (3/4)

#### Anchor age 0



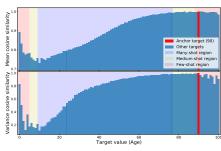
- (a) Baseline
- High similarity in neighbourhood for mean
- High similarities with further regions
- Lower similarities with some closer regions, e.g., variance neighbourhood



- (b) FDS
- Improved feature statistics calibration:
  - High similarity only in neighbourhood
  - "The further the region the lower the similarity"
  - More gradual similarity change

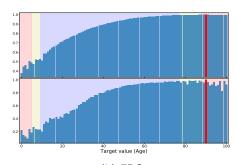
# Feature statistics similarity (4/4)

#### Anchor age 90





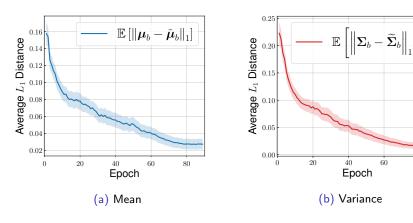
- High similarity in neighbourhood, esp. for mean
- High similarities with further regions
- Lower similarities with some closer regions



## (b) FDS

- Improved feature statistics calibration:
  - High similarity only in neighbourhood
    - "The further the region the lower the similarity"
  - More gradual similarity change

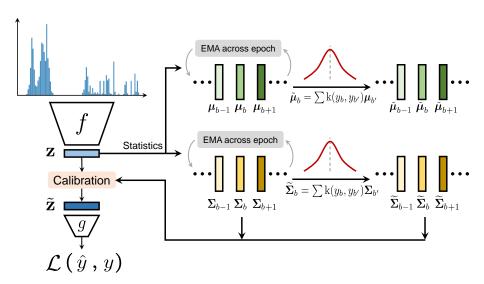
## Change of feature statistics w.r.t. epoch



- ullet  $\mu, \Sigma$ : Running mean and variance
- $oldsymbol{ ilde{\mu}}, ilde{oldsymbol{\Sigma}}$ : Smoothed mean and variance

80

## The FDS Algorithm



# Baselines (1/2)

- Vanilla: neglects data imbalance
- Synthetic samples
  - ► SMOTER (Torgo et al. 2013)
    - Defines frequent and rare regions using label density.
    - ② Creates synthetic samples for pre-defined rare regions by linearly interpolating both inputs and labels.
  - ▶ SMOGN (Branco et al. 2017): augments SMOTER with Gaussian noise
- Focal-R

$$\frac{1}{n} \sum_{i=1}^{n} \sigma(|\beta e_i|)^{\gamma} e_i$$

- Error-aware loss
- ▶ Maps the absolute error into [0, 1].
- $e_i$ :  $L_1$  error for the *i*-th sample
- $\triangleright \beta$ ,  $\gamma$ : hyper-parameters
- ▶ Inspired by Focal Loss (Lin 2017) for classification

# Baselines (2/2)

- Regressor re-training (RRT)
  - Two-stage training
    - Train encoder
    - Re-train regressor with inverse re-weighting and frozen encoder.
  - ▶ Inspired by Kang et al. 2019
- Cost-sensitive re-weighting: re-weighting schemes based on label distribution
  - Inverse-frequency weighting (INV)
  - Square-root weighting variant (SQINV)

## Results

# Could LDS + FDS help when the label distribution is skewed with one or more Gaussian peaks?

- Experimental setup
  - Curated skewed label distributions with 1-4 Gaussian peaks on IMDB-WIKI-DIR
  - ► Compared with the vanilla model
- Findings
  - Robustness to distribution change
  - Brings improvement

## Skewed label distribution with one Gaussian peak

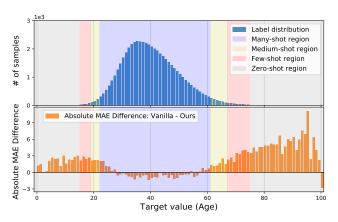


Figure: MAE gains of LDS + FDS over the vanilla model.

## Skewed label distribution with two Gaussian peaks

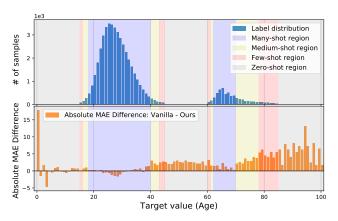


Figure: MAE gains of LDS + FDS over the vanilla model.

## Skewed label distribution with three Gaussian peaks

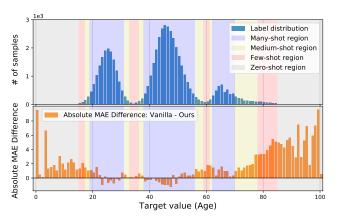


Figure: MAE gains of LDS + FDS over the vanilla model.

## Skewed label distribution with four Gaussian peaks

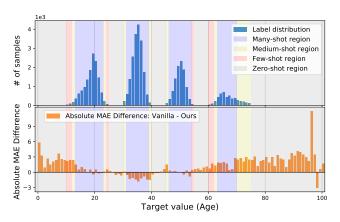


Figure: MAE gains of LDS + FDS over the vanilla model.

# Skewed label distribution with two Gaussian peaks on IMDB-WIKI-DIR

| Metrics   |       | MA      | E↓      |         |      | GN      |         |         |  |
|---|-------|---------|---------|---------|------|---------|---------|---------|--|
| Shot  | All   | w/ data | Interp. | Extrap. | All  | w/ data | Interp. | Extrap. |  |
| VANILLA   | 11.72 | 9.32    | 16.13   | 18.19   | 7.44 | 5.33    | 14.41   | 16.74   |  |
| Vanilla + LDS   | 10.54 | 8.31    | 14.14   | 17.38   | 6.50 | 4.67    | 12.13   | 15.36   |  |
| Vanilla + FDS   | 11.40 | 8.97    | 15.83   | 18.01   | 7.18 | 5.12    | 14.02   | 16.48   |  |
| Vanilla + LDS + FDS   | 10.27 | 8.11    | 13.71   | 17.02   | 6.33 | 4.55    | 11.71   | 15.13   |  |
| Ours (best) vs. Vanilla $ +1.45 +1.21 +2.42 +1.17 +1.11 +0.78 +2.70 +1.61 $ |       |         |         |         |      |         |         |         |  |

Table: Interpolation & extrapolation results

Best results by smoothing both label & feature distributions

## Different skewed label distributions on IMDB-WIKI-DIR

| Metrics  |       |      |       | GM ↓  |       |         |         |      |      |      |       |       |         |         |
|--|-------|------|-------|-------|-------|---------|---------|------|------|------|-------|-------|---------|---------|
| Shot   | All   | Many | Med.  | Few   | Zero  | Interp. | Extrap. | All  | Many | Med. | Few   | Zero  | Interp. | Extrap. |
| 1 peak:  |       |      |       |       |       |         |         |      |      |      |       |       |         |         |
| Vanilla  | 11.20 | 6.05 | 11.43 | 14.76 | 22.67 | _       | 22.67   | 7.02 | 3.84 | 8.67 | 12.26 | 21.07 | _       | 21.07   |
| Vanilla + LDS                                    | 10.09 | 6.26 | 9.91  | 12.12 | 19.37 | -       | 19.37   | 6.14 | 3.92 | 6.50 | 8.30  | 16.35 | -       | 16.35   |
| Vanilla + FDS                                    | 11.04 | 5.97 | 11.19 | 14.54 | 22.35 | -       | 22.35   | 6.96 | 3.84 | 8.54 | 12.08 | 20.71 | _       | 20.71   |
| $\mathrm{Vanilla} + \mathbf{LDS} + \mathbf{FDS}$ | 10.00 | 6.28 | 9.66  | 11.83 | 19.21 | -       | 19.21   | 6.09 | 3.96 | 6.26 | 8.14  | 15.89 | -       | 15.89   |
| 2 peaks:   |       |      |       |       |       |         |         |      |      |      |       |       |         |         |
| VANILLA  | 11.72 | 6.83 | 11.78 | 15.35 | 16.86 | 16.13   | 18.19   | 7.44 | 3.61 | 8.06 | 12.94 | 15.21 | 14.41   | 16.74   |
| Vanilla + LDS                                    | 10.54 | 6.72 | 9.65  | 12.60 | 15.30 | 14.14   | 17.38   | 6.50 | 3.65 | 5.65 | 9.30  | 13.20 | 12.13   | 15.36   |
| Vanilla + FDS                                    | 11.40 | 6.69 | 11.02 | 14.85 | 16.61 | 15.83   | 18.01   | 7.18 | 3.50 | 7.49 | 12.73 | 14.86 | 14.02   | 16.48   |
| Vanilla + LDS + FDS                              | 10.27 | 6.61 | 9.46  | 11.96 | 14.89 | 13.71   | 17.02   | 6.33 | 3.54 | 5.68 | 8.80  | 12.83 | 11.71   | 15.13   |
| 3 peaks:   |       |      |       |       |       |         |         |      |      |      |       |       |         |         |
| Vanilla  | 9.83  | 7.01 | 9.81  | 11.93 | 20.11 | _       | 20.11   | 6.04 | 3.93 | 6.94 | 9.84  | 17.77 | _       | 17.77   |
| Vanilla + LDS                                    | 9.08  | 6.77 | 8.82  | 10.48 | 18.43 | -       | 18.43   | 5.35 | 3.78 | 5.63 | 7.49  | 15.46 | _       | 15.46   |
| Vanilla + FDS                                    | 9.65  | 6.88 | 9.58  | 11.75 | 19.80 | -       | 19.80   | 5.86 | 3.83 | 6.68 | 9.48  | 17.43 | -       | 17.43   |
| Vanilla + LDS + FDS                              | 8.96  | 6.88 | 8.62  | 10.08 | 17.76 | -       | 17.76   | 5.38 | 3.90 | 5.61 | 7.36  | 14.65 | -       | 14.65   |
| 4 peaks:   |       |      |       |       |       |         |         |      |      |      |       |       |         |         |
| Vanilla  | 9.49  | 7.23 | 9.73  | 10.85 | 12.16 | 8.23    | 18.78   | 5.68 | 3.45 | 6.95 | 8.20  | 9.43  | 6.89    | 16.02   |
| $\mathrm{Vanilla} + \textbf{LDS}$                | 8.80  | 6.98 | 8.26  | 10.07 | 11.26 | 8.31    | 16.22   | 5.10 | 3.33 | 5.07 | 7.08  | 8.47  | 6.66    | 12.74   |
| Vanilla + FDS                                    | 9.28  | 7.11 | 9.16  | 10.88 | 11.95 | 8.30    | 18.11   | 5.49 | 3.36 | 6.35 | 8.15  | 9.21  | 6.82    | 15.30   |
| $\mathrm{Vanilla} + \mathbf{LDS} + \mathbf{FDS}$ | 8.76  | 7.07 | 8.23  | 9.54  | 11.13 | 8.05    | 16.32   | 5.05 | 3.36 | 5.07 | 6.56  | 8.30  | 6.34    | 13.10   |

### References

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- Kang, Bingyi et al. (2019). "Decoupling representation and classifier for long-tailed recognition". In: arXiv preprint arXiv:1910.09217.
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