## PMC Lecture 08

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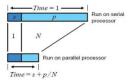
 $28 \ {\rm October} \ 2025$ 

## Chapter 2

# Message passing interfaces

# 2.1 Estimating the speed-up factor of a parallel application

Generally speaking, each program features a "serial fraction" that cannot be parallelized, resulting in a limit to the speed-up factor that can be achieved by parallelizing the application.



In fact, it is possible to reformulate the running time of a parallel application using p processes through the following weighted average:

$$T_{par}(p) = (1 - \alpha)T_{seq} + \alpha \frac{T_{seq}}{p}$$
, where  $0 \le \alpha \le 1$  is the parallelizable fraction.

Most particularly, Amdahl's law exploits this formulation in order to provide an asymptotic estimate of the speed-up factor as follows:

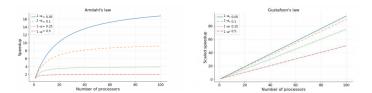
$$S(p) = \frac{T_{seq}}{(1-\alpha)T_{seq} + \alpha \frac{T_{seq}}{p}} \text{ and take } \lim_{p \to \infty} S(p) = \frac{1}{1-\alpha}$$

Keep in mind, however, that Amdahl's law can only be used to explain the speed-up factor of strong scaling applications.

In fact, in the context of weak scaling applications, it is possible to observe that the parallel fraction tends to increase with the problem's size.

For this reason, Gustafson's law considers the following scaled speed-up factor:

 $S(n,p) = (1-\alpha) + \alpha p$ , where  $0 \le \alpha \le 1$  is the parallelizable fraction.



**Example:** Suppose you want to parallelize the sum of two vectors  $\vec{x}$  and  $\vec{y}$ . In the context of message passing interfaces, the master process can use a scatter to read and distribute pieces of the vector to the other working processors, each computing a partial sum.

Then, the master process can perform a gather in order to collect the partial sums and recover the final result.

#### 2.2 Derived datatypes

Derived datatypes are used to simulate structs by storing the type and memory offset of each item in the collection, allowing functions that need to send/receive

data to collect these items.

 $\mathbf{N.B.:}$  When the collection is not needed anymore, its memory space should be freed up.