Feng Shiwei UID: 305256428

a.
$$y_1 = \beta_1 x_1^2 + \xi_1^2 + \xi_1$$

$$\frac{1}{2} \left[\left(\frac{\partial^2}{\partial x} \right) = \frac{1}{N} \left[\frac{N}{N} \right] \left[\frac{N^2}{N^2} \left[\frac{N^2}{N} \right] \right] = \frac{N-1}{N} \left[\frac{N^2}{N} \right]$$

 $\frac{n}{n-1} \int_{-1}^{2} \int_{-1}^{2}$

$$\frac{\sum_{i=1}^{n} \left(\frac{y_{i} - \beta_{i} \chi_{i}}{\sigma} \right)^{2} - \sum_{i=1}^{n} \left(\frac{e_{i}}{\sigma} + \frac{(\beta_{i} - \beta_{i}) \chi_{i}}{\sigma} \right)^{2} - \sum_{i=1}^{n} \left(\frac{e_{i}}{\sigma} + \frac{(\beta_{i} - \beta_{i}) \chi_{i}}{\sigma} \right)^{2} - \sum_{i=1}^{n} \frac{e_{i}^{2}}{\sigma^{2}} + \frac{(\beta_{i} - \beta_{i}) \chi_{i}^{2}}{\sigma^{2}} + \frac{2(\beta_{i} - \beta_{i}) \chi_{i}^{2}}{\sigma^{2}} +$$

$$\frac{n}{|i-1|} \frac{ei^2}{\sigma^2} = \frac{n \hat{\sigma}^2}{\sigma^2} = \frac{(n-1) \cdot Se^2}{\sigma^2}$$

$$(2) \hat{\beta}_{1} = \frac{\sum x_{1}^{2}y_{1}^{2}}{\sum x_{1}^{2}} = \frac{\sum x_{1}^{2}y_{1}^{2}}{\sum x_{1}^{2}y_{2}^{2}} = \frac{\sum x_{1}^{2}y_{1}^{2}}{\sum x_{1}^{2}y_{1}^{2}} = \frac{\sum x_{1}^{2}y_{1}^{2}}{\sum x_{1}^{2}} = \frac{\sum x_{1}^{2}y_{1}^{2}}{\sum x_{1}^{2}} = \frac{\sum x_{1}^{2}y_{1}^{2}}{\sum x_{1}^{2}} = \frac{\sum x_{1}^{2}y_{1}^{2}}{\sum x_{1}^{2}} = \frac{\sum x_{1}^{2}y_{1}^{2}}{\sum x_{1}^{2}}$$

$$\frac{(\hat{\beta}_{1}-\beta_{1})^{\frac{m}{2}}X_{1}^{2}}{\sigma^{2}} = \frac{(\hat{\beta}_{1}-\beta_{1})^{2}}{(\hat{\beta}_{1}-\beta_{1})^{2}} \sim \chi^{2}$$

(3)
$$\frac{n}{2}$$
 $x_i e_i = \frac{n}{2} x_i (y_i - \hat{\beta}_i x_i) = \frac{n}{2} x_i y_i - \hat{\beta}_i \frac{n}{2} x_i^2 = 0$

Notice that
$$cov(e_i, \hat{\beta}_i) = cov(y_i - \hat{\beta}_i \chi_i, \hat{\beta}_i) = cov(y_i, \frac{\chi_i y_i}{\sum \chi_i^2}) - \chi_i vor(\hat{\beta}_i)$$

$$= \frac{\chi_i}{\sum \chi_i^2} vor(y_i^2) - \chi_i \cdot \frac{\sigma^2}{\sum \chi_i^2} = 0.$$

$$\frac{(n-1)5e^{2}}{5} \quad \text{and} \quad \left(\frac{(\beta_{1}-\beta_{1})}{5/\sqrt{2}\times z^{2}}\right)^{2} \quad \text{are independent}$$

$$\frac{(n-1)5e^{2}}{5} \quad \sim \chi_{1}^{2}$$

C.
$$\frac{(n-1)se^{2}}{\sigma^{2}} \sim \chi_{n-1}^{2}$$
 $M_{\frac{(n-1)se^{2}}{\sigma^{2}}}(t) = (1-2t)^{-\frac{(n-1)}{2}}$
 $M_{\frac{(n-1)se^{2}}{\sigma^{2}}}(t) = M_{\frac{(n-1)se^{2}}{\sigma^{2}}}(\frac{\sigma^{2}}{n-1}t) = (1-\frac{2\sigma^{2}}{n-1}t)^{-\frac{(n-1)}{2}}$
 $M_{\frac{(n-1)se^{2}}{\sigma^{2}}}(t) = M_{\frac{(n-1)se^{2}}{\sigma^{2}}}(\frac{\sigma^{2}}{n-1}t) = (1-\frac{2\sigma^{2}}{n-1}t)^{-\frac{(n-1)se^{2}}{2}}(\frac{\sigma^{2}}{n-1}t)$
 $M_{\frac{(n-1)se^{2}}{\sigma^{2}}}(t) = M_{\frac{(n-1)se^{2}}{\sigma^{2}}}(\frac{\sigma^{2}}{n-1}t) = (1-\frac{2\sigma^{2}}{n-1}t)^{-\frac{(n-1)se^{2}}{2}}(\frac{\sigma^{2}}{n-1}t)$

$$\frac{d}{d} \cdot E(x) = \int_{0}^{3} x \cdot \frac{d}{3x} x^{d-1} dx = \frac{d}{3x} \int_{0}^{3} x^{d} dx$$

$$= \frac{d}{3x} \cdot \frac{1}{x+1} x^{d+1} \Big|_{0}^{3}$$

$$= \frac{3d}{d+1}$$

$$\frac{1}{1} = \frac{3\alpha}{\alpha + 1} \implies \hat{\lambda} = \frac{x}{3 - \bar{x}}$$

$$L = \alpha^{n} \cdot 3^{-n} \cdot (11 \times 1)^{\alpha - 1}$$

$$\frac{\partial \ln L}{\partial \alpha} = \frac{\eta}{\alpha} - \eta \ln \beta + \sum_{i=1}^{n} \ln \chi_i = 0$$

$$\therefore \hat{\mathcal{L}} = \frac{n}{n \ln \beta - \sum_{i=1}^{n} \ln x_i}$$

Q.
$$y_{i} \sim N \left(\beta_{o} + \beta_{i} \chi_{i}^{*}, \epsilon_{i} \right)$$

$$f(y_{i}) = \frac{1}{\sqrt{n}} e^{-\frac{1}{2\sigma^{2}} \left(y_{i} - \beta_{o} - \beta_{i} \chi_{i}^{*} \right)^{2}}$$

$$\vdots \quad L = \left(2\pi \sigma^{2} \right)^{-\frac{n}{2}} \cdot e^{-\frac{1}{2\sigma^{2}} \sum_{i=1}^{n} \left(y_{i} - \beta_{o} - \beta_{i} \chi_{i}^{*} \right)^{2}}$$

$$|nL| = -\frac{n}{2} |n 2\pi \sigma^{2}| - \frac{1}{2\sigma^{2}} \sum_{i=1}^{n} \left(y_{i} - \beta_{o} - \beta_{i} \chi_{i}^{*} \right)^{2}$$

$$\frac{\partial |nL|}{\partial \beta_{o}} = \frac{1}{\sigma^{2}} \sum_{i=1}^{n} \left(y_{i} - \beta_{o} - \beta_{i} \chi_{i}^{*} \right) \frac{\partial |nL|}{\partial \beta_{1}} = \frac{1}{\sigma^{2}} \sum_{i=1}^{n} \left(y_{i} - \beta_{o} - \beta_{i} \chi_{i}^{*} \right) \chi_{i}^{*}$$

 $\frac{\partial M}{\partial x^2} = -\frac{n}{\nu} \cdot \frac{1}{\sigma^2} + \frac{1}{2(\sigma^2 + \frac{1}{2(\sigma^2 + \frac{1}{2})})^2}$

$$I(\theta) = -E \left(\frac{3hL}{3h^{2}} \frac{3hL}$$

$$\frac{1}{N} = \frac{\delta^{2} \sum X_{i}^{2}}{N \sum (X_{i} - \overline{X})^{2}} = \frac{\delta^{2} \sum X_{i}}{N \sum (X_{i} - \overline{X})^{2}} = \frac{\delta^{2} \sum X_{i}^{2}}{N \sum (X_{i} - \overline{X})^{2}} = \frac{\delta^{2} \sum X_{i}^$$

$$= \sigma^{2} \cdot \frac{\sum (X_{i} - \overline{X})^{2}}{\sum (X_{i} - \overline{X})^{2}}$$

$$= \sigma^{2} \cdot \frac{\sum (X_{i} - \overline{X})^{2} + n\overline{X}^{2}}{n \sum (X_{i} - \overline{X})^{2}}$$

$$= \frac{\sigma^{2} \cdot \sum X_{i}^{2}}{n \sum (X_{i} - \overline{X})^{2}}$$