

March 10, 2025

Introduction to Internet of Things Course

# Augmented reality on your knees



Seminar by Nikita Ligostaev

# What a heck why AR?

Web-camera is a sensor by construction, image formation is crucial for any kind of visualization.

We will consider very basic principles of linear algebra used in computer vision without going into details.

AR is just a straightforward application for today's seminar.

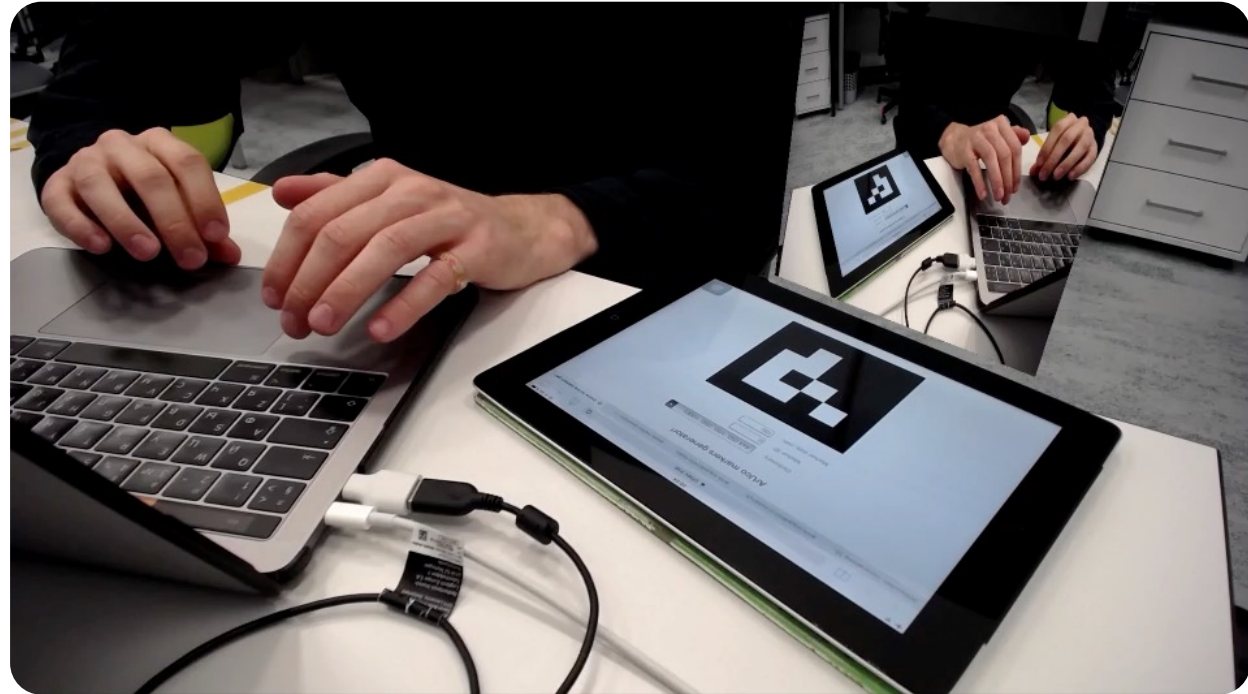


By the end of the seminar you will be able to use monocular camera for projection of anything in the camera frame.

Hopefully, it will be useful for common understanding and your research (in ideal case).

# ! Spoilers for seminar

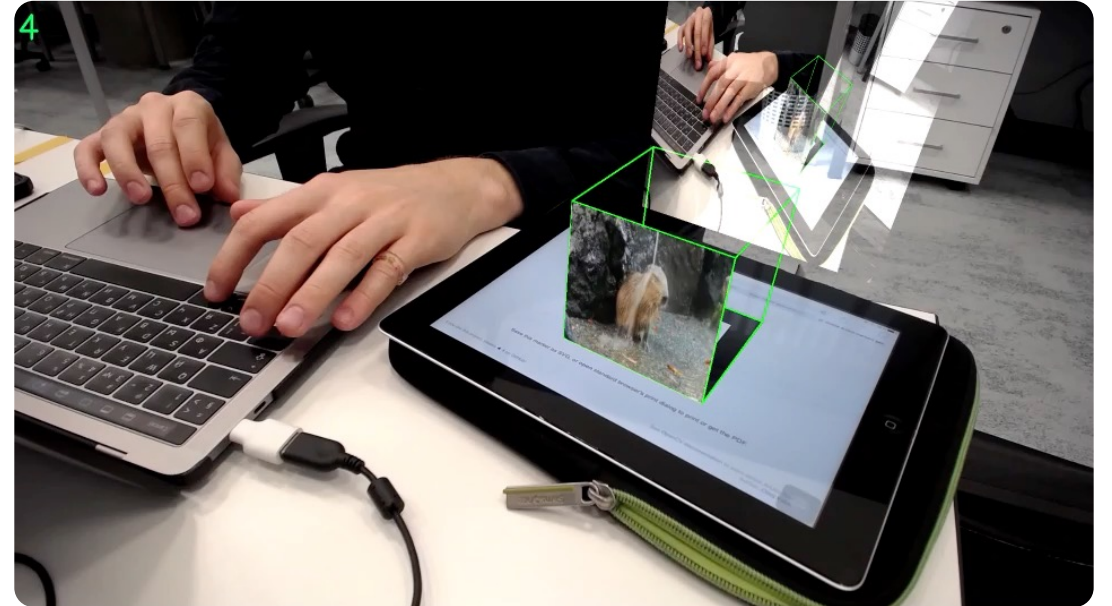
numero uno



Web-camera feed projection on the plane

# ! Spoilers for homework

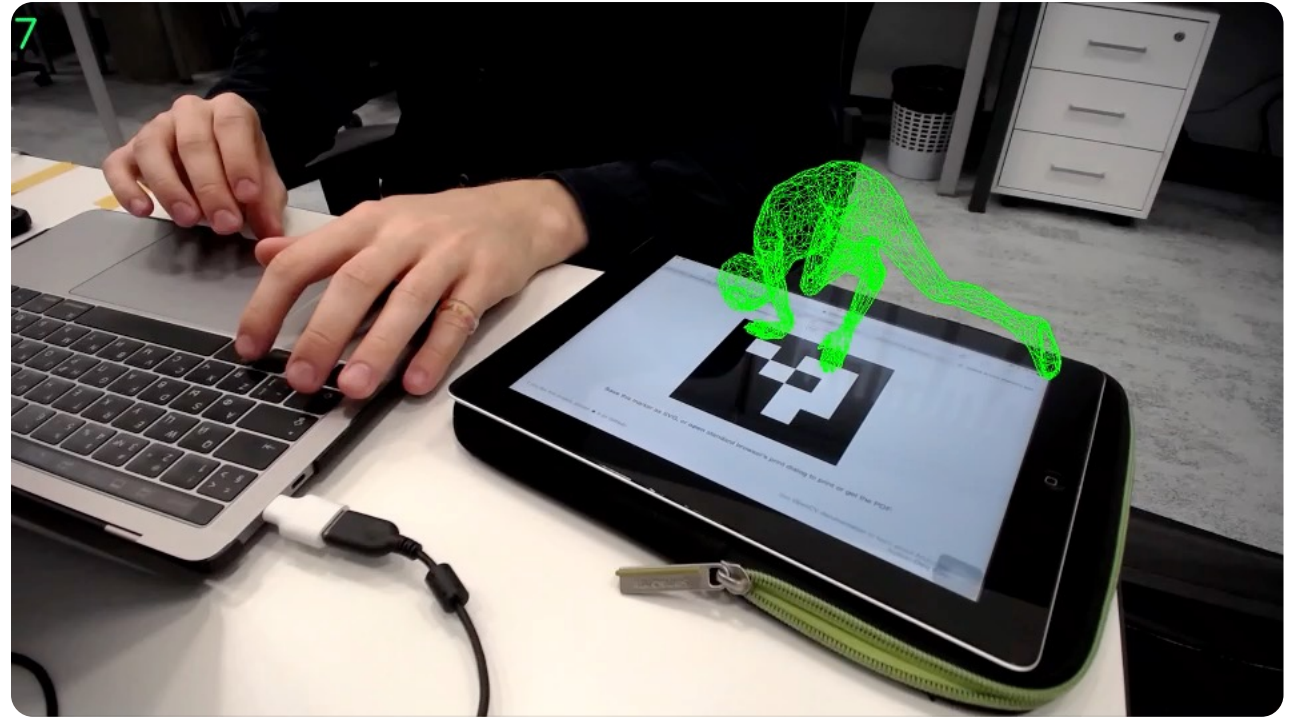
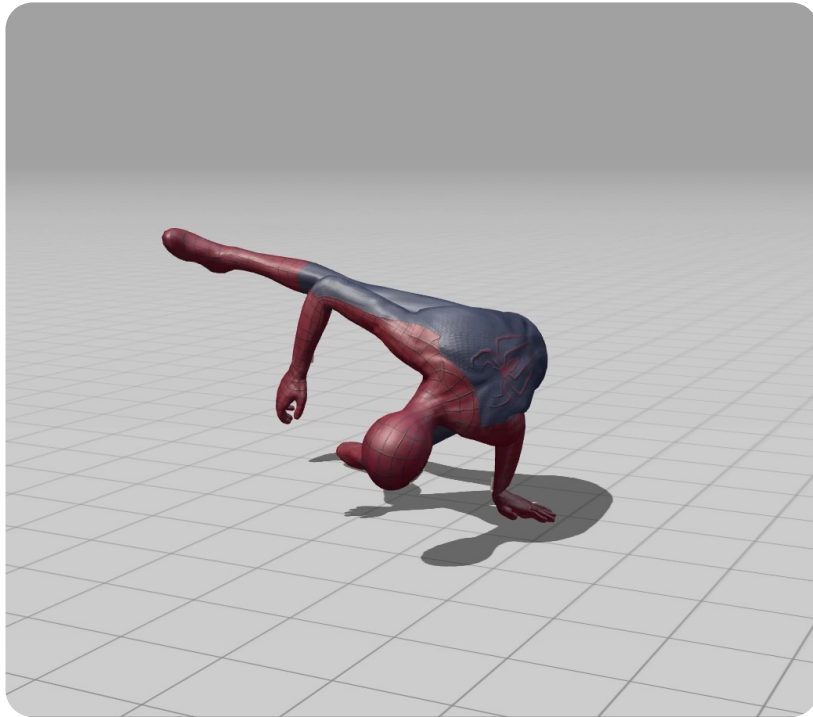
numero due



Video projection on the cube plane  
and web-camera feed projection functionality

# ! Spoilers for bonus

numero tre



Animated .obj model projection

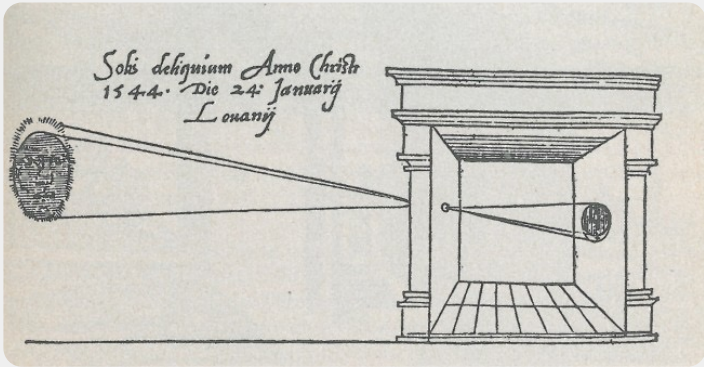
# Instructions

All tasks and their description are available in Github repository (the same repository you used for conda setup)

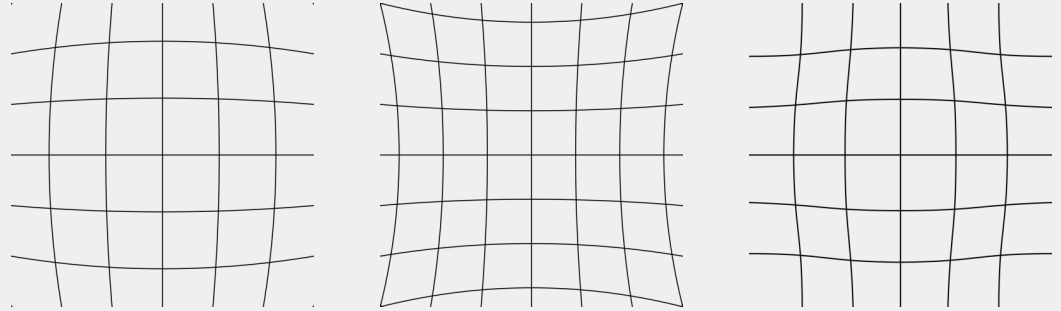
- x solve all tasks from **seminar.ipynb**
- x solve homework from **hw.ipynb**
- x solve **bonus.ipynb** for additional points
- x in case you are done with tasks you are free and can go home
- x **do not forget to submit report in Canvas for seminar, homework or/and bonus**  
(make video recordings of your solution, archive copy of repository, include your videos in **./data/solutions/** folder, put your name in the beginning of **hw.ipynb** or/and **bonus.ipynb**)



# Plan for today



Pinhole camera model



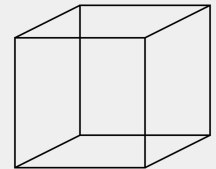
Lens/camera distortion

$$\begin{bmatrix} \hat{x}_s \\ \hat{y}_s \\ \hat{z}_s \end{bmatrix} = \mathbf{K} [\mathbf{R}|t] \begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix}$$

Projective transformation



Markers



Hands-on  
AR demo

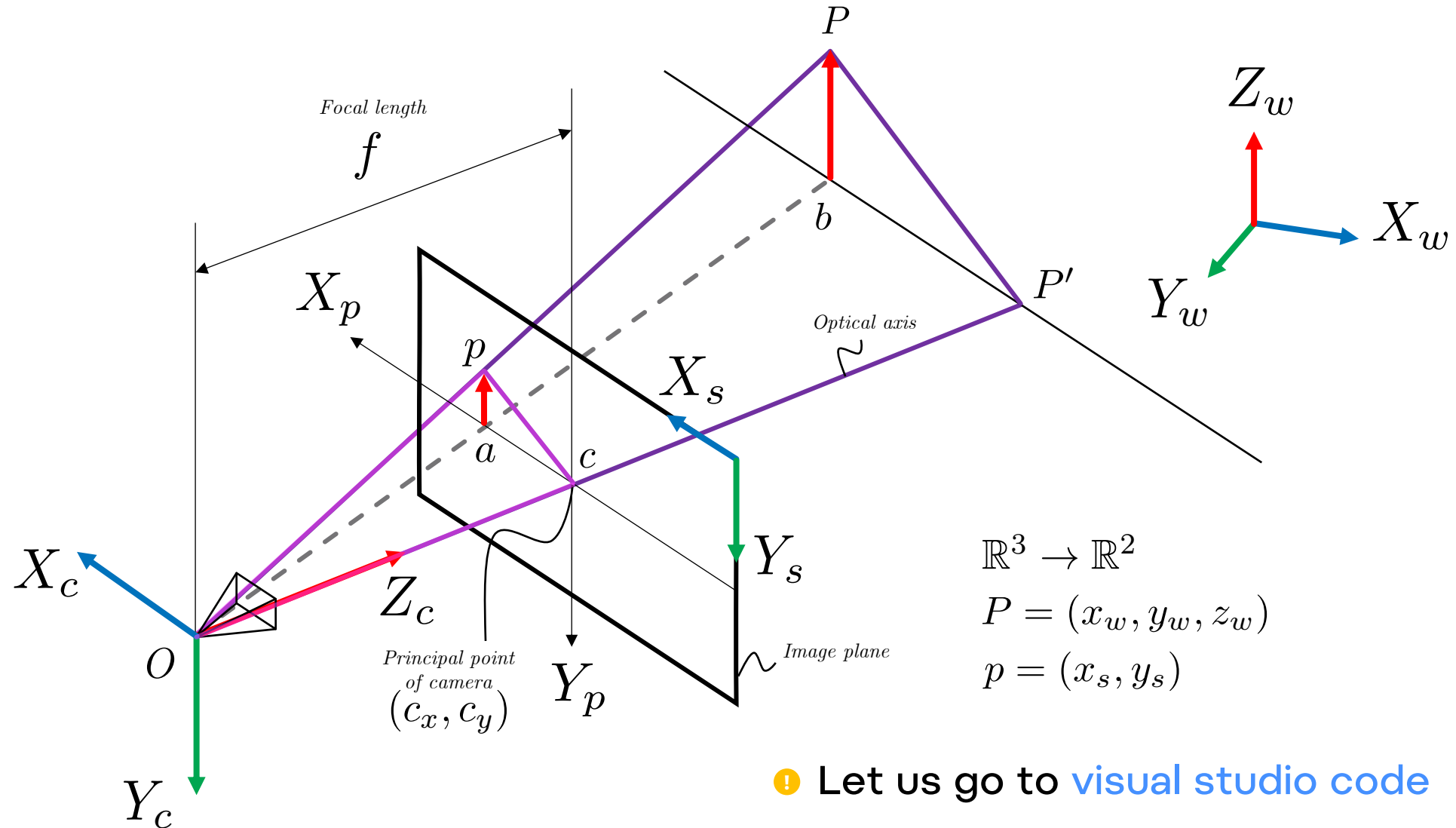
# Pinhole camera model

or how camera perceives the world





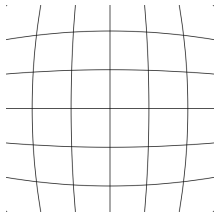
# Pinhole camera model



📌 Let us go to [visual studio code](#)

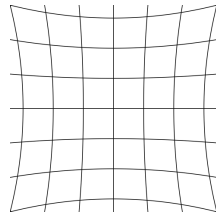
# Camera/lens distortion

and what we can do with it



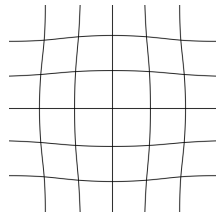
**Barrel**

$$k_1 < 0$$



**Pincushion**

$$k_1 > 0$$



**Moustache**

$$k_1 < 0 \quad k_2 > 0$$

$$L(x_c, y_c) = L_r(x_c, y_c) + L_t(x_c, y_c)$$

$$r^2 = x_c^2 + y_c^2$$

$$L_r(x_c, y_c) = (1 + k_1 r^2 + k_2 r^4 + k_3 r^6) \begin{bmatrix} x_c \\ y_c \end{bmatrix}$$

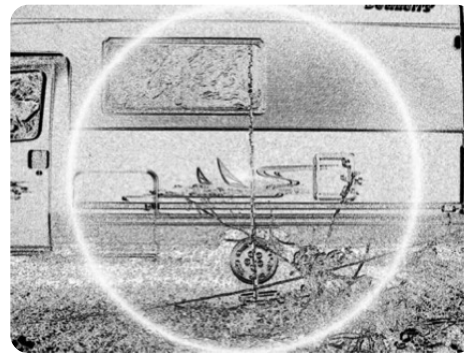
$$L_t(x_c, y_c) = \begin{bmatrix} 2p_1 x_c y_c + p_2 (r^2 + 2x_c^2) \\ p_1 (r^2 + 2y_c^2) + 2p_2 x_c y_c \end{bmatrix}$$



**Original**



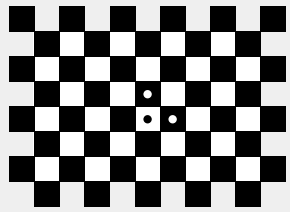
**Corrected**



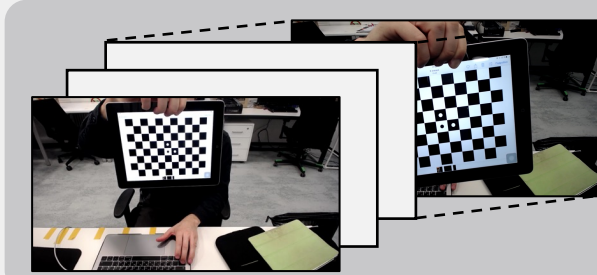
Difference between  
grayscale versions  
of original  
and corrected images

# Projective transformation

## Intrinsic camera matrix



Known-size  
checkerboard  
pattern



Set of calibration samples

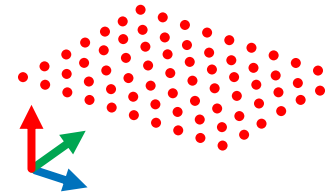


Camera calibration algorithm

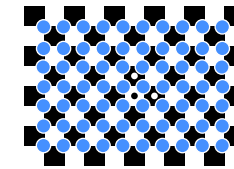
$$\mathbf{K} = \begin{bmatrix} f_x & \gamma & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 858.212 & 0 & 574.698 \\ 0 & 845.243 & 394.842 \\ 0 & 0 & 1 \end{bmatrix}$$

all parameters in px units

## 3D to 2D mapping



3D model of pattern  
(3D points in WCS)



2D object points  
(2D points in CCS)

$$\mathbf{K} = \begin{bmatrix} f_x & \gamma & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}$$

Intrinsic  
camera matrix

$$\mathbf{R} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix} \quad t = \begin{bmatrix} t_1 \\ t_2 \\ t_3 \end{bmatrix}$$

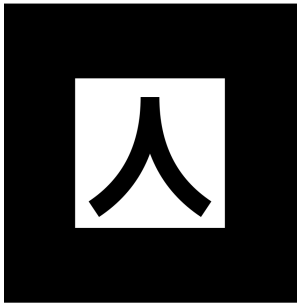
Rotation matrix and translation vector

$$\begin{bmatrix} \hat{x}_s \\ \hat{y}_s \\ \hat{z}_s \end{bmatrix} = \mathbf{K} [\mathbf{R}|t] \begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix}$$

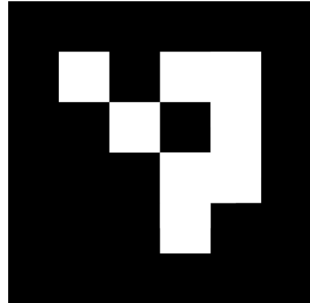
Solution

# Markers

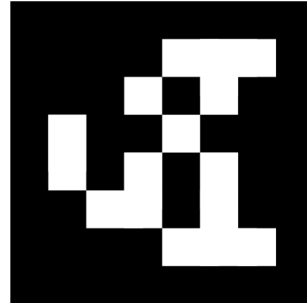
Fiducial markers use the same idea as calibration pattern (known geometry object), but mostly for detection and pose estimation purposes (e.g. in robotics, PCB manufacturing).



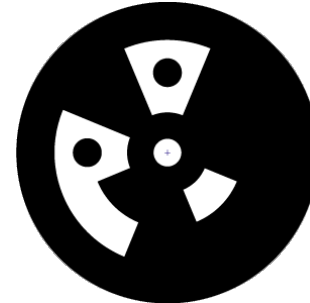
ARToolKit



Aruco



Apritag



Intersense



reactIVision

There a lot of them

# Hands-on session

is on

! Let us go to [visual studio code](#)



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Ciao cacao. Thank You.



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