

TITLE

by

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SUMMARY

TITLE

by

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LIST OF ABBREVIATIONS

ABC	Write out in full
DEF	What the abbreviation represents
GHI	Note the use of case
JKL	Write out in full
MNO	What the abbreviation represents
PQR	Note the use of case
STU	Write out in full
VWX	What the abbreviation represents
YZ	Note the use of case

TABLE OF CONTENTS

CHAPTER 1	INTRODUCTION	1
1.1	PROBLEM STATEMENT	1
1.1.1	Context of the problem	1
1.1.2	Research gap	1
1.2	RESEARCH OBJECTIVE AND QUESTIONS	1
1.3	HYPOTHESIS AND APPROACH (FOR ILLUSTRATION THIS HEADING CON- TINUES ONTO THE NEXT LINE)	1
1.4	RESEARCH GOALS	1
1.5	RESEARCH CONTRIBUTION	1
1.6	OVERVIEW OF STUDY	2
CHAPTER 2	LITERATURE STUDY	3
2.1	CHAPTER OBJECTIVES	3
2.2	FAULT DETECTION AND ANALYSIS	3
2.2.1	PAGERANK DERIVATION	3
2.2.2	LOOPRANK ADAPTION	5
2.2.3	LOOPRANK DEVELOPMENT	5
2.3	VISUALIZATION FOR FAULT DETECTION	6
2.3.1	VISUALIZATION IN GENERAL	6
2.3.2	VISUAL ANALYTICS	7
2.3.3	VALUE OF RECORD KEEPING IN VISUALIZATION	12
2.3.4	A subsection with a long heading that continues from the first line onto the second line see also table of contents	15
CHAPTER 3	METHODS (FOR ILLUSTRATION THIS HEADING CONTINUES ONTO THE NEXT LINE)	17

3.1	CHAPTER OVERVIEW	17
CHAPTER 4	RESULTS	18
4.1	CHAPTER OVERVIEW	18
CHAPTER 5	DISCUSSION	19
5.1	CHAPTER OVERVIEW	19
CHAPTER 6	CONCLUSION	20
6.1	EXAMPLE HEADING	20
REFERENCES	21
ADDENDUM A	DERIVATION OF HIGHER ORDER MODELS	23
A.1	EXAMPLE HEADING	23
A.1.1	Subheading example	23

CHAPTER 1 INTRODUCTION

1.1 PROBLEM STATEMENT

1.1.1 Context of the problem

Context of the problem context of the problem context of the problem

1.1.2 Research gap

Research gap research gap research gap research gap research gap

1.2 RESEARCH OBJECTIVE AND QUESTIONS

Research objective and questions research objective and questions

- Is this a research question?
- Is this the second research question?
- Is this the third research question?

Research objective and questions

1.3 HYPOTHESIS AND APPROACH (FOR ILLUSTRATION THIS HEADING CONTINUES ONTO THE NEXT LINE)

Hypothesis and approach hypothesis and approach hypothesis and

1.4 RESEARCH GOALS

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1.5 RESEARCH CONTRIBUTION

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1.6 OVERVIEW OF STUDY

Overview of study overview of study overview of study overview of

CHAPTER 2 LITERATURE STUDY

2.1 CHAPTER OBJECTIVES

This chapter explores the basic

2.2 FAULT DETECTION AND ANALYSIS

New data driven methods that apply concepts from other fields have started to show some promising results. One of these methods is the use of the PageRank algorithm [1] employed by google on the ranking of control loops based on the degree of interaction.[2] has developed a methodology called LoopRank with the aim of prioritizing control loop maintenance by highlighting loops that have a higher correlation with other loops. In this methodology a relative weight matrix is compiled using partial correlation between input and output variables. The importance scores of each variable is then determined by calculating the normalized eigenvector of the relative weight matrix.

2.2.1 PAGERANK DERIVATION

The ranking algorithm developed by [1] started with the idea of ranking web sites depending on how many times they are referenced by other websites.

Consider a group of 4 websites that contain references to each other in the manner indicated in Figure 2.1. References are indicated by arrows. An initial idea would be that a page that has more references

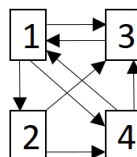


Figure 2.1. web pages with references

or back links is more important. Let x_k be the importance of page k. If this method is followed then $x_3 = 3$ would be the most important web page because it has the most references.

This initial ranking method indicates that x_3 is important, but it doesn't take into account the importance that x_3 passes on to x_1 because it is the only page referenced by x_3 .

Another approach would be to let back links from important pages count more than back links from less important pages. If a page k has a back link from page j, then the score given to this back link can be calculated as $x_k = \frac{x_j}{n_j}$ where n_j is the total number of references made by page j. The total score for page x_k is then calculated by the sum of all back links to it adjusted for the number of references made. Applying this new method the importance score for each node is calculated:

$$x_1 = \frac{x_3}{1} + \frac{x_4}{2}$$

$$x_2 = \frac{x_1}{3}$$

$$x_3 = \frac{x_1}{3} + \frac{x_2}{2} + \frac{x_4}{2}$$

$$x_4 = \frac{x_1}{3} + \frac{x_2}{2}$$

These equations can be written in a matrix form, which will be defined as the link matrix A:

$$A = \begin{bmatrix} 0 & 0 & 1 & \frac{1}{2} \\ \frac{1}{3} & 0 & 0 & 0 \\ \frac{1}{3} & \frac{1}{2} & 0 & \frac{1}{2} \\ \frac{1}{3} & \frac{1}{2} & 0 & 0 \end{bmatrix}$$

Each row in the matrix A represents a page or node while each column represents the importance score from another node. For example row one represents node 1 and it has a back link from node 3 with an importance score of 1 and a back link from node 4 with a importance score of $\frac{1}{2}$.

if $x = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 \end{bmatrix}^T$ then the problem can be defined as the eigenvector problem:

$$Ax = x\lambda$$

with x being an eigenvector for A with an eigenvalue of 1

if A is a $n \times n$ matrix, then a nonzero vector x is an eigenvector if $Ax = \lambda x$ for some scalar λ . The eigenvector x that solves this equation is then calculated to be:

$x \approx \begin{bmatrix} 0.387 & 0.129 & 0.290 & 0.194 \end{bmatrix}^T$ which shows that node one is in fact more important than node three.

2.2.2 LOOPRANK ADAPTION

[2] developed a method called LoopRank which is based on the PageRank algorithm to prioritize control loop maintenance. Modern industrial sites have a large number of control loops which becomes challenging to maintain effectively given limited technical resources.

The LoopRank method can be summarized in five steps:

1. Collect time series data of control loop parameters
2. Calculate the partial correlation between all the variables in the data set. This information is used to build a relative weight matrix A or link matrix as referred to in the PageRank algorithm
3. Compute the LoopRank based on the relative weight matrix A using the eigenvector centrality theorem
4. multiply the result for each loop with a pre-defined weight that is based on the criticality of the loop. This weight is assigned heuristically depending on loop type and profitability
5. Normalize the results to express the score for each loop as a percentage

[2] demonstrated the efficacy of LoopRank by testing it on an industrial case study in which it successfully flagged the most critical control loops.

2.2.3 LOOPRANK DEVELOPMENT

[3] compared LoopRank with a more traditional data driven method that utilizes the integral of absolute or squared error to determine loop interaction. Canonical correlation was used to calculate the relative weight matrix in the LoopRank methodology. It was found that both methods delivered similar results.

The LoopRank methodology was further expanded on by [4] who tested the LoopRank using transfer entropy in an attempt to get a better estimation of causality when calculating the relative weight matrix. [5] used this methodology for incipient fault detection by calculating importance scores over multiple overlapping time regions.

2.3 VISUALIZATION FOR FAULT DETECTION

The methodologies involved in fault detection and diagnosis of industrial processes rely heavily on the visual analysis of time series data. Data is continuously generated by industrial processes, this data in its simplest form can be floating point or boolean values on a control system interface screen. This data is used by plant personnel as feedback on the current status of automated processes.

This study will focus on methods and approaches taken to visualize temporal or time series data.

2.3.1 VISUALIZATION IN GENERAL

Some of the first books to discuss information visualization date back to 1967 with the publication of Jacques Bertin's *Semiologie Graphique* [6]. A survey by [6] highlighted the number of visualization books have been published each year, displayed in 2.2.

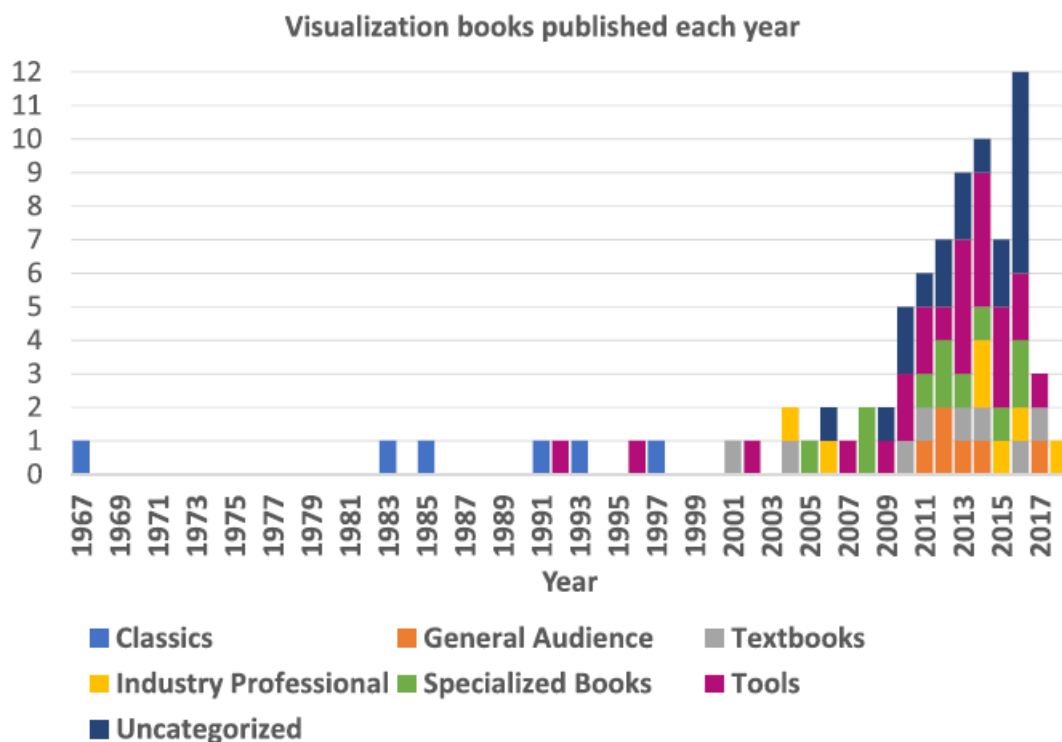


Figure 2.2. Visualization books published each year

The IEEE Visualization conference series aimed at sharing developments in this field started in 1990 and has contributed a large amount of data on how visualization assists other fields to better understand their data. [7] compiled a database of these publications to assist researchers in this field to understand the history of visualization in a field and make the researcher aware of new developments trends. The

papers presented through these conferences serve as valuable source to describe previous work related to visualization for the use of fault detection and diagnosis.

2.3.2 VISUAL ANALYTICS

Before designing it is important to understand the mental processes behind data analytics that are used by people to understand and gain insight into data. The work discussed in this section first attempts to describe the human aspect of the process and then attempts to integrate the role of the machine or computer into the process.

One of the earliest models for that describe the process of 'sensemaking' was developed by [8]. In this model intelligence analysis or sensemaking consists of:

1. information gathering
2. representation of the information in the form of an outline or model that aids the analysis
3. development of insight through manipulation of the outline or model
4. Creation of a knowledge product or direct action based on the analysis

, The process is visually described by Figure2.3.

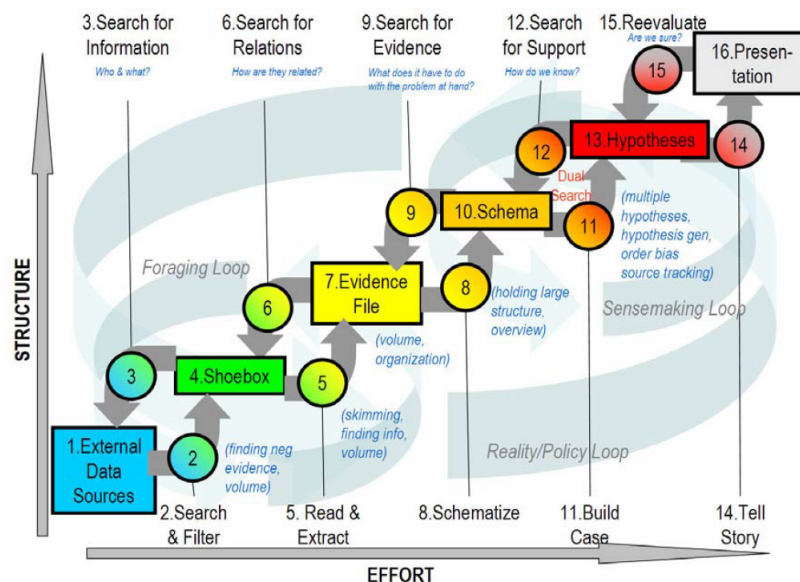


Figure 2.3. [8] sensemaking model

The rectangles represent the flow of data and the circles represent the process flow. What is very clear from this model is that there are a lot of back loops and sets of activities that cycle around finding information and making sense of the information. The end result of the process is the generation of novel information by the analyst.

The External data sources are filtered into a smaller data set called a shoebox. Snippets are then extracted from the shoe box based on observed relationships and placed in the Evidence File. A Schema or model is then developed and verified using the Evidence file. A Hypotheses is then form based on this model with a feedback loop that search for additional support of this hypotheses. Finally there is a presentation that is first reevaluated before becoming the product of this work. This model can be used in a top-down (theory to data) or bottom-up (data to theory) approach.

Another approach that represents a more non-linear model that might be a closer representation to how humans actually process information. [9] present a model that starts of with the assumption that people always start making sense of something with some perspective, viewpoint or framework. The frame basically functions as hypothesis of how the data fits together.

These frameworks or frames actually define what counts as data and shape the data. Frames also change as we acquire data making it a two way path between a frame and data.

The first cycle that starts from the frame/ data idea is the elaboration cycle. In this cycle the frame is expanded and questioned - there could be doubt about the explanation it provides. If the doubt, possibly caused by troublesome data is explained away then the frame is preserved.

The second cycle involves a re framing process. If questioning the frame leads to its rejection, it might lead to its replacement with a better one. We could compare frames to see which one fits the data best.

This model is displayed in Figure2.4.

This is a continuous process in which a frame is strengthened or improvement at each iteration.

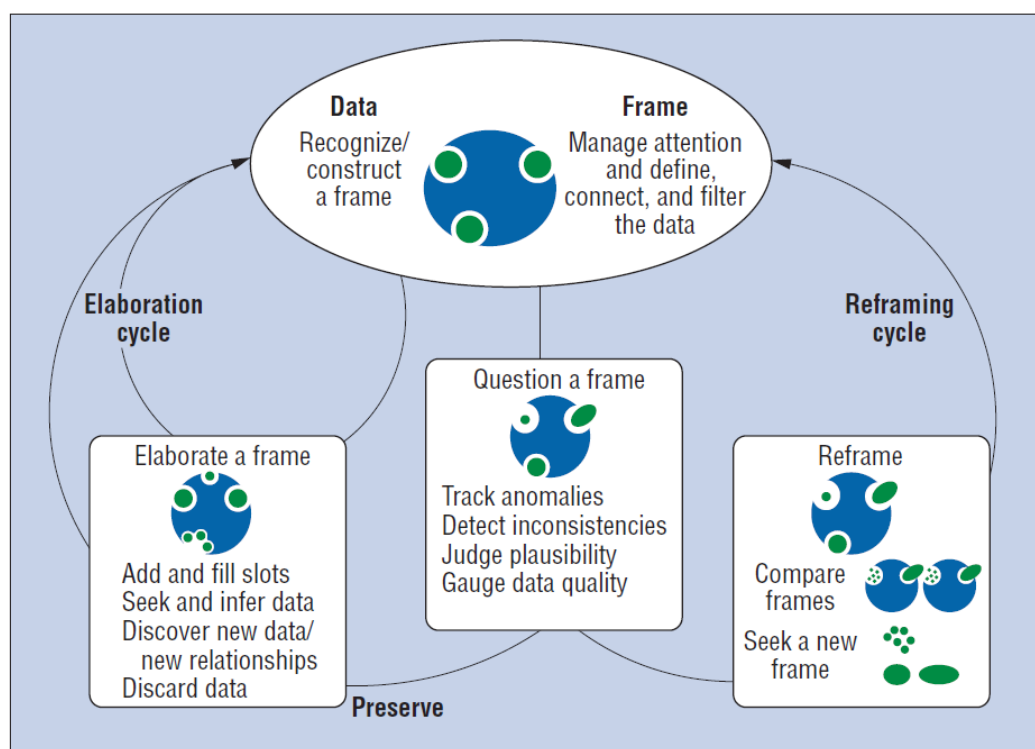


Figure 2.4. [9] frame-data sensemaking model

Any method for turning data into knowledge requires the manipulation of the data. The analysis would start with an analysis of the data. This analysis has traditionally been done manually but with the exponential growth in the amount of data that can form part of an analysis other methods are being developed to make this step more efficient. [11] analyzed this challenge in the emerging field of knowledge discovery in databases (KDD). In simple terms this field is concerned with development of methods and techniques for making sense of data.

One of the most noteworthy fields where these methods are applied is in the areas of astronomy. These fields contain terabytes of data contained in images. Although industrial application of data analysis contain a lot less data than this it could still be worth while studying these techniques to see if they can assist with effectively utilizing large amounts of time series data.

The goal of KDD is extracting high-level knowledge from low-level data in the context of large data sets [11]. The KDD process is visually described by Figure 2.5. The process is described by the following steps:

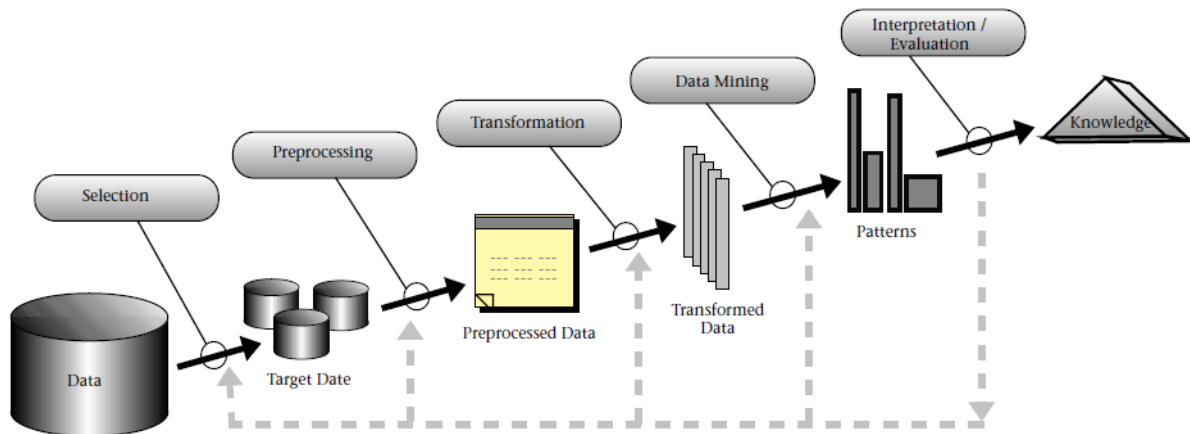


Figure 2.5. [11] steps in the knowledge discovery in databases model

1. Develop understanding of application domain and use prior knowledge to determine the goal of the KDD
2. Create a data set or subset of the available data that will be used to discover useful information
3. Data cleaning, in this step invalid data like noise or questionable data is removed in order to prevent false deductions
4. Data reduction and projection - finding useful features to represent the data, in this step dimensional reduction can be done to simplify the analysis
5. Match the goals of KDD to a specific data mining method
6. Exploratory analysis of the model and hypothesis selection, in this step the data mining method is chosen as well as the methods that will be used to search for patterns
7. Data mining - searching for patterns in the data that would confirm the hypothesis
8. Interpreting the mined patterns
9. Acting on the discovered knowledge, using it to solve the problem

These steps describe a linear process but there can be movement back and forth between the steps to refine the process.

[10] goes a step further to describe the process in which knowledge is generated from data by developing a model that defines how the human and computer interact. This model is split into two parts:

1. computer system which involves the data, visualization and analytic models
2. human component that describes the cognitive process associated with an analytical session

What makes visual analytics so effective is the integration of these two parts; the human side provides the perceptive skills, cognitive reasoning and domain knowledge while the computer side provides the computing data storage capability [10]. This visual analytic model also attempts to incorporate some of the other models described earlier like the Sensemaking model [8] and the Knowledge Discovery Process in Databases (KDD) [11]. The complete knowledge generation model with the reference to other models is displayed in Figure 2.6.

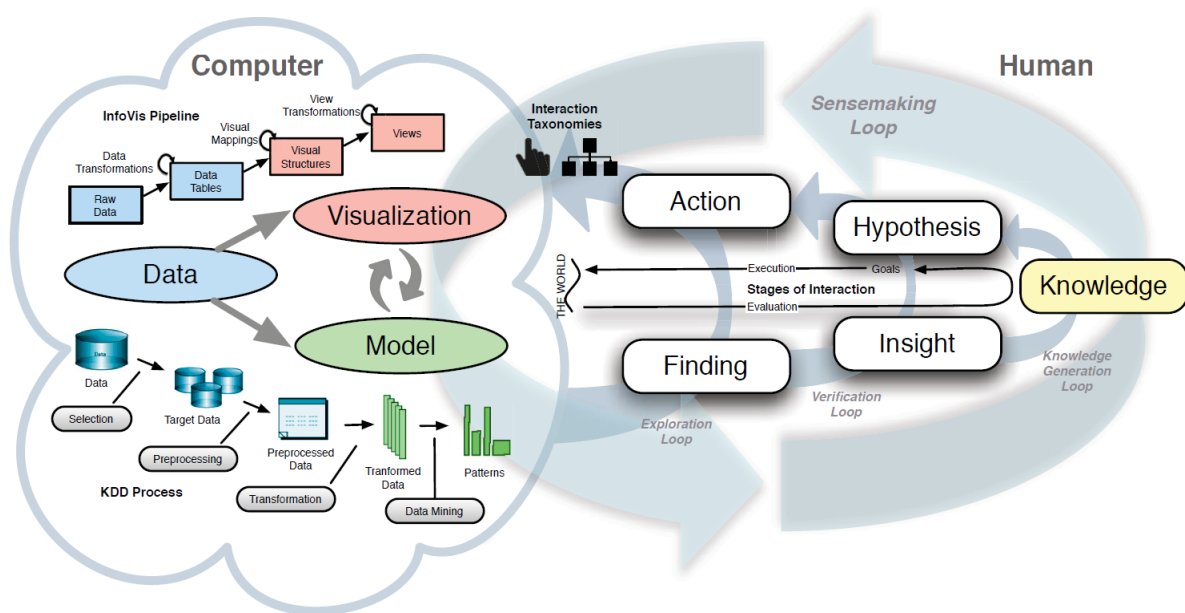


Figure 2.6. [10] computer-human interaction in knowledge generating process

The computer part of the model has three main elements:

1. Data - this includes all the data that describes the analytical problem and includes facts in any structured, semi-structured or unstructured manner. Another element to this is a term called meta data, which could be data that describes the structure of other data or data that summarizes other data.
2. Model - This can be any descriptive measure of the data ranging from statistical properties of the data to complex data mining algorithms. This process can deliver a single number to describe the strength of an hypothesis or a complex pattern.

3. Visualization - In this process the data is transformed into some kind of visual artifact that enables the analyst to detect relationships.

, The human element is also described in three main loops: The computer part of the model has three main elements:

1. Exploration loop - Findings are made based on observations of the visual analytics system, Actions or individual tasks are then performed that result in tangible and unique responses from the visual analytics system.
2. Verification loop - Insight is gained from interpreting Findings, often with previous domain knowledge to generate units of information. A Hypothesis is then formed based on these Insights and tested in the visual analytics system through Actions.
3. Knowledge - The final part is to build up confidence in the Insights from the data and Hypotheses tested on the data. If patterns or stories told by the data makes sense and can be used to answer the questions from the visual analytic process then Knowledge is generated. This Knowledge is added to the domain knowledge of the analyst to ask more questions and generate more Knowledge.

This model proposed by [10] again highlights the iterative process of visual analytics and how feedback loops are used in every element of the model.

2.3.3 VALUE OF RECORD KEEPING IN VISUALIZATION

[12] conducted a experiment to study the visual analytics process and the role of record keeping in this process. This study also elaborated on key elements for the design of a collaborative visual analysis tool. The study required groups to complete tasks given a certain data set using computer aided visual analytics. Actions taken during visual analytics were grouped into four phases:

1. Problem definition - understanding what needs to be solved
2. Visualization - generating visual artifacts
3. Analysis - most complex phase that requires examining of charts and making sense of them combined with other data
4. Dissemination - compiling findings in a report

The findings from the study conducted by [12] confirmed observations by other researchers about the non-linear temporal order of activities. While completing the tasks users would move through the phases in a variety of orders. The visualization and analysis phases were strongly interrelated, the users moved back and forth between these two phases much more than the other phases.

[12] generated a very visual model of these four phases with key elements noted in each phase:

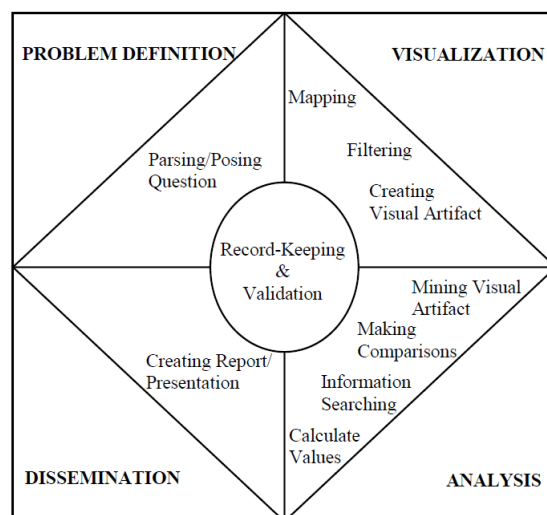


Figure 2.7. Visualization books published each year

Record keeping involves the saving of visual artifacts and notes. In most cases a visual artifact can convey a complex idea more effectively than notes. Visual artifacts were saved for two main reasons; using them in reporting and using them to enhance the analysis process.[12] recommends that visual analytic systems provide functionality to save visual artifacts like charts for later use and comparison. Note taking also plays a critical role in all phases of the process. The notes high level content could be divided into two categories; findings and cues. Findings are a results of mathematical calculations, statistical operations or decisions and outcomes of the analysis process, they could also take to form of saved charts. Cues can be anything that is not directly extracted from the visualizations that could assist the user to framing or understanding the task at hand. A larger proportion of findings were recorded in the analysis phase while the cues were largely taken during the visualization phase. The study concluded that record keeping is used intensively by data analysts.

[13] completed a longitudinal study of a bioinformatics data set analysis to gain understanding of the entire analysis process from raw data to insights. Visual analytics can be described as a process wherein

user gain insight into complex data. The study highlighted how analysts gather and build insights over long periods of time and connecting the data to extensive domain knowledge and expertise. It is emphasized that analyst spend a significant amount of time on manual manipulation of data and this creates a very important need for the visualization tool to be interactive. Inferior visualizations with interaction were preferred over superior static visualizations.

Visualization plays a critical role in these data driven problem solving techniques. [14] has shown that traditional methods like directed-acyclic graphs and Hasse diagrams can display casual links in an intuitive way but becomes less suitable when the number of nodes and interactions in a system grow. The use of two novel visualization techniques called Growing Squares and Growing Polygons demonstrate the use of animations, colors and patterns to better visualize casual relations.

Another approach to improve visualization of casual relations would be to adapt novel techniques used in other fields, similar to how PageRank was adapted to be used as LoopRank in industrial processes. Process monitoring and fault detection of batch processes has received attention in recent years. The extensive use of batch processing in the production of high value products makes it a important to ensure that batch runs are completed with a high level of success. [15] developed a novel approach to process monitoring and fault detection in batch processes by utilizing a technique they termed time-explicit Kiviat diagrams. The core idea behind this technique is based on Multi-way Principle Component Analysis that facilitates batch-wise unfolding of the three dimensional (Time*Variables*Batches) batch data matrix into a two dimensional matrix that captures the variation across batches. The type of data required to warrant the use of this technique is very similar to the data generated by multiple time region analysis in the LoopRank analysis done by [5]. Each batch can be seen as a time region in the LoopRank analysis and the analysis can be seen as the completion of multiple batch runs.

Equation (2.8) shows an example of a numbered equation.

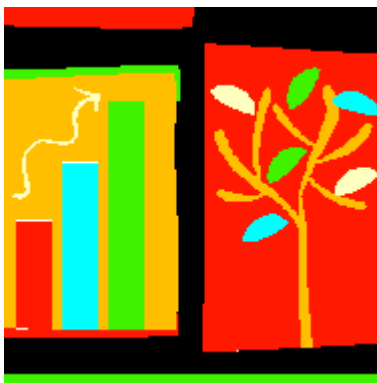
$$\Delta w_{i,j} = \alpha a_i \Delta[j] \quad (2.1)$$

$$\begin{aligned}
 \mathbf{QXa} &= \mathbf{Qy} \\
 \therefore (\mathbf{QX})^T \mathbf{QXa} &= (\mathbf{QX})^T \mathbf{Qy} \\
 \therefore \mathbf{a} &= ((\mathbf{QX})^T \mathbf{QX})^{-1} (\mathbf{QX})^T \mathbf{Qy} \\
 &= (\mathbf{X}^T \mathbf{Q}^T \mathbf{QX})^{-1} \mathbf{X}^T \mathbf{Q}^T \mathbf{Qy} \\
 &= (\mathbf{X}^T \mathbf{WX})^{-1} \mathbf{X}^T \mathbf{Wy}
 \end{aligned} \tag{2.2}$$

2.3.4 A subsection with a long heading that continues from the first line onto the second line
see also table of contents

2.3.4.1 Testing deeper nested section headers

2.8(a) and 2.8(b).



(a) A subfigure



(b) Another subfigure

Figure 2.8. This is a figure caption. In the example (b) is a rotated version of (a).

Third theme of literature study third theme of literature study third theme of literature study third theme of literature study.

Table 2.8 shows an example of a table.

Table 2.1. This is a table caption

Column 1	Column 2	Column 3	Column 4
123	abc	123	abc
123	abc	123	abc
			abc

CHAPTER 3 METHODS (FOR ILLUSTRATION THIS HEADING CONTINUES ONTO THE NEXT LINE)

3.1 CHAPTER OVERVIEW

Chapter overview chapter overview chapter overview chapter overview chapter overview chapter overview chapter overview chapter overview chapter overview.

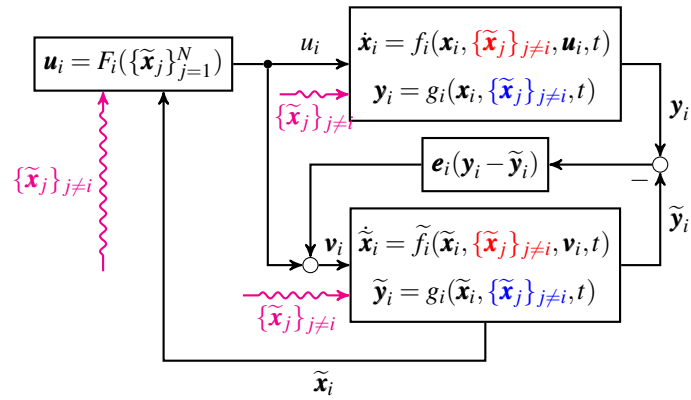


Figure 3.1. Another example of a figure

CHAPTER 4 RESULTS

4.1 CHAPTER OVERVIEW

Chapter overview chapter overview chapter overview chapter overview chapter overview chapter overview chapter overview chapter overview chapter overview.

Table 4.1 shows a more complex example of a table.

Table 4.1. A comparison of the total thermal conductance of the VO_x devices at atmospheric pressure.

Device	Theoretical ^(a) [μWK ⁻¹]	Theoretical ^(b) [μWK ⁻¹]	Simulated [μWK ⁻¹]	Experimental [μWK ⁻¹]
VOX4	14.28	11.02	9.55	8.30
VOX6	22.55	18.03	15.71	11.91
VOX7	22.89	18.11	15.91	13.27
VOX8	23.45	18.54	17.69	11.77
VOX13	18.16	14.96	14.39	13.45
VOX15	22.55	18.03	15.65	12.74
VOX23	21.54	17.62	15.62	9.27
VOX24	22.21	17.95	15.44	10.88
VOX32	16.97	13.75	11.41	9.31
VOX33	16.97	13.72	11.67	12.26
VOX36	21.48	17.56	16.51	15.42
VOX39	12.39	10.20	9.55	10.49

^(a) Theoretical calculation using the standard approach.

^(b) Theoretical calculation using the compensated method by including the thermal constriction resistance.

CHAPTER 5 DISCUSSION

5.1 CHAPTER OVERVIEW

CHAPTER 6 CONCLUSION

6.1 EXAMPLE HEADING

REFERENCES

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ADDENDUM A DERIVATION OF HIGHER ORDER MODELS

A.1 EXAMPLE HEADING

A.1.1 Subheading example

Filler text to test template. Filler text to test template. Filler text to