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$$\int x^2 \cdot \cos(x) \, dx$$

$$\Rightarrow \int u(x) \cdot v'(x) \, dx = u(x) \cdot v(x) - \int u'(x) \cdot v(x) \, dx$$

$$\begin{array}{ll} u(x) = x^2 & u'(x) = 2x \\ v'(x) = \cos(x) & v(x) = \sin(x) \end{array}$$

$$\int (x^2 \cdot \cos(x)) \, dx = x^2 \cdot \sin(x) - \int (2x \cdot \sin(x)) \, dx$$

$$\begin{array}{ll} u_1(x) = 2x & u_1'(x) = 2 \\ v_1'(x) = \sin(x) & v_1(x) = -\cos(x) \end{array}$$

$$\int (2x \cdot \sin(x)) \, dx = 2x \cdot (-\cos(x)) - \int (2 \cdot (-\cos(x))) \, dx$$

$$= -2x \cdot \cos(x) + 2 \cdot \sin(x)$$

$$\Rightarrow \int (x^2 \cdot \cos(x)) \, dx = x^2 \cdot \sin(x) - (-2x \cdot \cos(x) + 2 \cdot \sin(x))$$

$$= x^2 \cdot \sin(x) + 2x \cdot \cos(x) - 2 \cdot \sin(x)$$