

## CMPUT 274 - Tangible Computing

### Morning Problem: Max Product

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#### Description

A vector  $x$  in  $\mathbb{Z}^n$  is a list of  $n$  integers  $x_1, x_2, \dots, x_n$ . Given two vectors  $x$  and  $y$  in  $\mathbb{Z}^n$ , their inner product is equal to  $x_1 \cdot y_1 + x_2 \cdot y_2 + \dots + x_n \cdot y_n$  (the symbol  $\cdot$  represents multiplication).

Suppose you are allowed to permute (reorder) the values of  $x$  and  $y$  any way you like. What is the maximum possible inner product you can obtain by permuting the values of  $x$  and  $y$ ?

#### Input

There are three lines of input. The first line contains an integer  $n$  ( $1 \leq n \leq 100,000$ ) - the number of values in each vector.

The second line of input contains  $n$  space-separated integers  $x_1, x_2, \dots, x_n$  describing the vector  $x$ . The third line contains  $n$  space-separated integers  $y_1, y_2, \dots, y_n$  describing the vector  $y$ . The absolute value of each of these  $2n$  integers will not exceed 1000.

#### Output

Output should consist of one integer - the maximum possible inner product we can obtain by reordering  $x$  and  $y$ .

#### Sample Input 1

```
3
1 3 -5
-2 4 1
```

#### Sample Output 1

```
23
```

**Explanation** If we kept  $x$  the same and reordered  $y$  as  $1, 4, -2$ , the inner product would be  $1 \cdot 1 + 3 \cdot 4 + (-5) \cdot (-2) = 1 + 12 + 10 = 23$ . No other ordering of  $x$  and  $y$  achieves a larger inner product.

#### Sample Input 2

```
5
1 2 3 4 5
1 0 1 0 1
```

#### Sample Output 2

```
12
```