Parallel & Distributed Computing: Lecture 12

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Project: Add-ons modules to LARLIB.jl

Example of Python to Julia conversion

- Step one: removal of dependencies from larlib.largrid.py
- 2 Step two: syntactic translation of functions
- 3 Step three: integration test
- Step four: Debug, debug, debug

Introduction from largrid.pdf

This report aims to discuss the design and the implementation of the largrid module of the LAR-CC library, including also the Cartesian product of general cellular complexes. In particular, we show that both n-dimensional grids of (hyper)-cuboidal cells and their d-dimensional skeletons ($0 \le d \le n$), embedded in \mathbb{E}^n , may be properly and efficiently generated by assembling the cells produced by a number n of either 0- or 1-dimensional cell complexes, that in such lowest dimensions coincide with simplicial complexes.

In Section 2 we give the simple implementation of generation of lower-dimensional (say, either 0- or 1-dimensional) regular cellular complexes with integer coordinates. In Section 3 a functional decomposition of the generation of either full-dimensional cuboidal complexes in \mathbb{E}^n and of their d-skeletons $(0 \le d \le n)$ is given, showing in particular that every skeleton can be efficiently generated as a partition in cell subsets produced by the Cartesian product of a proper disposition of 0-1 complexes, according to the binary representation of a subset of the integer interval $[0, 2^n]$. In Section 5 we provide a very simple and general implementation of the topological product of two cellular complexes of any topology. When applied to embedded linear cellular complexes (i.e. when the coordinates of 0-cells of arguments are fixed and given) the algorithm produces a Cartesian product of its two arguments. In Section 6 the exporting of the module to different languages is provided. The Section 7 contains the unit tests associated to the various algorithms, that are exported by the used literate environment in the proper test subdirectory—depending on the implementation

Figure 1: Introduction to module

Step one: removal of dependencies from larlib.largrid.py

Look for function definitions

Get the significant subset

```
def larModelProduct(twoModels):
def grid_0(n):
def grid_1(n):
def larGrid(n):
def index2addr (shape):
def binaryRange(n):
def larVertProd(vertLists):
def filterByOrder(n):
def larCellProd(cellLists):
def larGridSkeleton(shape):
def larImageVerts(shape):
def larCuboids(shape, full=False):
def mergeSkeletons(larSkeletons):
```

From largrid.py To largrid-test.py 0/5

3 Cuboidal grids

More interesting is the generation of hyper-cubical grids of intrinsic dimension d embedded in n-dimensional space, via the Cartesian product of d 1-complexes and (n-d) 0-complexes. When d=n the resulting grid is said solid; when d=0 the output grid is 0-dimensional, and corresponds to a grid-arrangement of a discrete set of points in \mathbb{E}^n .

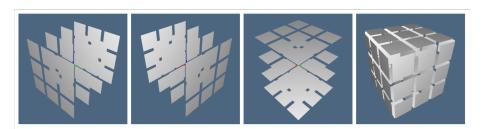


Figure 3: 2-skeleton of a 3-grid in \mathbb{E}^3

From largrid.py To largrid-test.py 1/5

```
Original code

def grid0(n):
    cells = AA(LIST)(range(n+1))
    return cells

def grid1(n):
    ints = range(n+1)
    cells = TRANS([ints[:-1],ints[1:]])
    return cells
```

From largrid.py To largrid-test.py 1/5

```
def grid0(n):
    cells = AA(LIST)(range(n+1))
    return cells

def grid1(n):
    ints = range(n+1)
    cells = TRANS([ints[:-1],ints[1:]])
    return cells

Removed dependencies in python

def grid_0(n):
    return [[i] for i in xrange(n+1)]
```

return [[i,i+1] for i in xrange(n)]

def grid 1(n):

Original code

Multidimensional array shape

From Python Numpy Tutorial

 An array is a grid of values, all of the same type, and is indexed by a tuple of nonnegative integers (multiindex)

Multidimensional array shape

From Python Numpy Tutorial

- An array is a grid of values, all of the same type, and is indexed by a tuple of nonnegative integers (multiindex)
- The number of dimensions is the rank or dimension of the array

Multidimensional array shape

From Python Numpy Tutorial

- An array is a grid of values, all of the same type, and is indexed by a tuple of nonnegative integers (multiindex)
- The number of dimensions is the rank or dimension of the array
- The shape of an array is a tuple of integers giving the size of the array along each dimension

From largrid.py To largrid-test.py 2/5

Multi-index to address transformation The second-order utility index2addr function transforms a shape list for a multidimensional array into a function that, when applied to a multindex array, i.e. to a list of integers within the shape's bounds, returns the integer address of the array component within the linear storage of the multidimensional array.

The transformation formula for a d-dimensional array with shape $(n_0, n_1, ..., n_{d-1})$ is a linear combination of the 0-based multi-index $(i_0, i_1, ..., i_{d-1})$ with weights equal to $(w_0, w_1, ..., w_{d-2}, 1)$:

$$addr = i_0 \times w_0 + i_1 \times w_1 + \dots + i_{d-1} \times w_{d-1}$$

where

$$w_k = n_{k+1} \times n_{k+2} \times \cdots \times n_{d-1}, \qquad 0 \le k \le d-2.$$

Therefore, we get index2addr([4,3,6])([2,2,0]) = $48 = 2 \times (3 \times 6) + 2 \times (6 \times 1) + 0$, where [2,2,0] represent the numbers of (pages, rows, columns) indexing an element in the three-dimensional array of shape [4,3,6].

Figure 5: Generation of address of elements in a linearized array

From largrid.py To largrid-test.py 2/5

Original code

```
def index2addr (shape):
    n = len(shape)
    shape = shape[1:]+[1]
    weights = [PROD(shape[k:]) for k in range(n)]
    def index2addr0 (multindex):
        return INNERPROD([multindex, weights])
    return index2addr0
```

From largrid.py To largrid-test.py 2/5

Original code

```
def index2addr (shape):
    n = len(shape)
    shape = shape[1:]+[1]
    weights = [PROD(shape[k:]) for k in range(n)]
    def index2addr0 (multindex):
        return INNERPROD([multindex, weights])
    return index2addr0
```

Removed dependencies

```
def index2addr (shape):
    n = len(shape)
    theShape = shape[1:]+[1]
    weights = [prod(theShape[k:]) for k in xrange(n)]
    def index2addr0 (multiIndex):
        return dot(multiIndex, weights)
    return index2addr0
```

From largrid.py To largrid-test.py 3/5

Original code

```
def larVertProd(vertLists):
    return AA(CAT)(CART(vertLists))
```

From largrid.py To largrid-test.py 3/5

Original code def larVertProd(vertLists): return AA(CAT)(CART(vertLists)) Removed dependencies using IterTools def larVertProd(vertLists):

return [[x[0] for x in v] for v in itertools.product(*vertLists)]

From largrid.py To largrid-test.py 4/5

Original code

From largrid.py To largrid-test.py 4/5

Removed dependencies

From largrid.py To largrid-test.py 5/5

Original code

From largrid.py To largrid-test.py 5/5

```
Original code
```

Removed dependencies

Step two: syntactic translation of functions

Step two: syntactic translation of functions

Language translation 1/7

 $\mathsf{largrid.py\text{-}test.py} \to \mathsf{largrid\text{-}test.jl}$

transformed code def grid_0(n): return [[i] for i in xrange(n+1)] def grid_1(n): return [[i,i+1] for i in xrange(n)] def larGrid(n): def larGrid1(d): if d==0: return grid_0(n) elif d==1: return grid_1(n) return larGrid1

Language translation 1/7

 $largrid.py-test.py \rightarrow largrid-test.jl$

```
transformed code

def grid_0(n):
    return [[i] for i in xrange(n+1)]

def grid_1(n):
    return [[i,i+1] for i in xrange(n)]

def larGrid(n):
    def larGrid1(d):
        if d==0: return grid_0(n)
            elif d==1: return grid_1(n)
        return larGrid1
```

Julia translation

```
function grid_0(n)
    return hcatt([[i] for i in range(0,n+1)]...) end
function grid_1(n)
    return hcatt([[i,i+1] for i in range(0,n)]...) end
function larGrid(n)
    function larGrid(d)
    if d==0
        return grid_0(n)
    elseif d==1
        return grid_1(n)
    end end
    return larGrid1 end
```

Language translation 1/7

 $largrid.py-test.py \rightarrow largrid-test.jl$

```
transformed code

def grid_0(n):
    return [[i] for i in xrange(n+1)]

def grid_1(n):
    return [[i,i+1] for i in xrange(n)]

def larGrid(n):
    def larGrid1(d):
        if d==0: return grid_0(n)
        elif d==1: return grid_1(n)
    return larGrid1
```

Julia translation

```
function grid_0(n)
    return hcat([[i] for i in range(0,n+1)]...) end
function grid_1(n)
    return hcat([[i,i+1] for i in range(0,n)]...) end
function larGrid(n)
    function larGrid(d)
        if d==0
            return grid_0(n)
        elseif d==1
            return grid_1(n)
        end end
    return larGrid1 end
```

Language translation 2/7

 $largrid.py-test.py \rightarrow largrid-test.jl$

transformed code

```
def index2addr (shape):
    n = len(shape)
    theShape = shape[1:]+[1]
    weights = [prod(theShape[k:]) for k in xrange(n)]
    def index2addr0 (multiIndex):
        return dot(multiIndex, weights)
    return index2addr0
```

Language translation 2/7

 $largrid.py-test.py \rightarrow largrid-test.jl$

```
transformed code
```

```
def index2addr (shape):
    n = len(shape)
    theShape = shape[1:]+[1]
    weights = [prod(theShape[k:]) for k in xrange(n)]
    def index2addr0 (multiIndex):
        return dot(multiIndex, weights)
    return index2addr0
```

Julia translation

```
function index2addr(shape)
   n = length(shape)
   theShape = append!(shape[2:end],1)
   weights = [prod(theShape[k:end]) for k in range(1,n)]
   function index2addr0(multiIndex)
        return dot(collect(multiIndex), weights) + 1
   end
   return index2addr0
end
```

Language translation 3/7

 $largrid.py-test.py \rightarrow largrid-test.jl$

transformed code

```
def binaryRange(n):
    return [('{0:0'+str(n)+'b}').format(k) for k in xrange(2**n)]
def larVertProd(vertLists):
    return [[x[0] for x in v] for v in itertools.product(*vertLists)]
def filterByOrder(n):
    terms = [[int(elem) for elem in list(term)] for term in binaryRange(n)]
    return [[term for term in terms if sum(term) == k] for k in xrange(n+1)]
```

Language translation 3/7

 $largrid.py-test.py \rightarrow largrid-test.jl$

```
transformed code
def binaryRange(n):
    return [('{0:0'+str(n)+'b}').format(k) for k in xrange(2**n)]
def larVertProd(vertLists):
    return [[x[0] for x in v] for v in itertools.product(*vertLists)]
def filterByOrder(n):
    terms = [[int(elem) for elem in list(term)] for term in binaryRange(n)]
    return [[term for term in terms if sum(term) == k] for k in xrange(n+1)]
Julia translation
using IterTools
function binaryRange(n)
    return [bin(k,n) for k in range(0,2^n)] end
function larVertProd(vertLists)
    coords = [[x[1] for x in v] for v in IterTools.product(vertLists...)]
    return sortcols(hcat(coords...)) end
function filterByOrder(n)
    terms = [[parse(Int8,bit) for bit in convert(Array(Char,1),term)]
                for term in binaryRange(n)]
    return [[term for term in terms if sum(term) == k] for k in range(0,n+1)] end
```

Language translation 4/7

 $\mathsf{largrid.py\text{-}test.py} \to \mathsf{largrid\text{-}test.jl}$

```
transformed code
```

Language translation 4/7

 $\mathsf{largrid.py\text{-}test.py} \to \mathsf{largrid\text{-}test.jl}$

```
transformed\ code
```

Julia translation

```
function larCellProd(cellLists)
    shapes = [length(item) for item in cellLists]
    cart = IterTools.product([range(0,shape) for shape in shapes]...)
    indices = hcat([collect(tuple) for tuple in sort(collect(cart))]...)
    h = 1
    index = indices[:,h]
    inCart = [collect(cells[k+1]) for (k,cells) in collect(zip(index,cellLists))]
    jointCells = sort(collect(IterTools.product(inCart...)))
    for h in range(2,size(indices,2))
        index = indices[:,h]
        inCart = [collect(cells[k+1]) for (k,cells) in collect(zip(index,cellLists))]
        jointCells = hcat( jointCells, sort(collect(IterTools.product(inCart...))))
    end
    convertIt = index2addr([ shape+1 for shape in shapes ])
    [hcat(map(convertIt, jointCells[:,j])...) for j in range(1,size(jointCells,2))]
```

Language translation 5/7

 $largrid.py-test.py \rightarrow largrid-test.jl$

transformed code

```
def larImageVerts(shape):
    def vertexDomain(n):
        return [[k] for k in xrange(n)]
    vertLists = [vertexDomain(k+1) for k in shape]
    vertGrid = larVertProd(vertLists)
    return vertGrid
```

Language translation 5/7

largrid.py-test.py → largrid-test.jl

```
transformed code
```

```
def larImageVerts(shape):
    def vertexDomain(n):
        return [[k] for k in xrange(n)]
    vertLists = [vertexDomain(k+1) for k in shape]
    vertGrid = larVertProd(vertLists)
    return vertGrid
```

Julia translation

```
function larImageVerts(shape)
  function vertexDomain(n)
      return [[k] for k in range(0,n)]
  end
  vertLists = [vertexDomain(k+1) for k in shape]
  vertGrid = larVertProd(vertLists)
  return vertGrid
end
```

Language translation 6/7

```
largrid.py-test.py \rightarrow largrid-test.jl
```

```
transformed code
```

Language translation 6/7

```
largrid.py-test.py → largrid-test.jl
```

Language translation 7/7

```
largrid.py-test.py \rightarrow largrid-test.jl
```

transformed code

```
def larCuboids(shape, full=False):
    vertGrid = larImageVerts(shape)
    gridMap = larGridSkeleton(shape)
    if not full:
        cells = gridMap(len(shape))
    else:
        skeletonIds = xrange(len(shape)+1)
        cells = [ gridMap(id) for id in skeletonIds ]
    return vertGrid, cells
```

Language translation 7/7

```
largrid.py-test.py \rightarrow largrid-test.jl
```

```
transformed code
```

```
def larCuboids(shape, full=False):
    vertGrid = larImageVerts(shape)
    gridMap = larGridSkeleton(shape)
    if not full:
        cells = gridMap(len(shape))
    else:
        skeletonIds = xrange(len(shape)+1)
        cells = [ gridMap(id) for id in skeletonIds ]
    return vertGrid, cells
```

Julia translation

```
function larCuboids(shape, full=false)
  vertGrid = larImageVerts(shape)
  gridMap = larGridSkeleton(shape)
  if ! full
    cells = gridMap(length(shape)+1)
  else
    skeletonIds = range(1,length(shape)+1)
    cells = [ gridMap(id) for id in skeletonIds ]
```

Step three: integration test

Step three: integration test

Execute the functions to be exported (API)

print(larCuboids(shape, true})

Step four: Debug, debug, debug

Step four: Debug, debug, debug