

## Foundation Calculus & Mathematical Techniques (CELEN037)

## Sample Exam Answers

1) This is a proof question the final answer is already given

2) 
$$\frac{dy}{dx} = \left(\frac{x^2 - 1}{x^2}\right) \ln(x) + \frac{x^2 + 1}{x^2}$$

3) This is a proof question the final answer is already given

4) 
$$\frac{dy}{dx} = -3\sin(3x+2)e^{\cos(3x+2)}$$

$$5) \qquad \frac{dy}{dx} = \frac{2}{7}$$

6) 
$$\frac{dy}{dx} = \left[ 6\cot(2x) - \frac{1}{5x} - \frac{\sec^2(x)}{\tan(x)} \right] \frac{\sin^3(2x)}{\sqrt[5]{x}\tan(x)}$$

7) 
$$\frac{dy}{dx} = \frac{b}{a} \left[ \frac{1}{2\sin(2\theta)} + \cot(2\theta) \right]$$

8) Tangent line: 
$$2y + 5x - 10 = 0$$

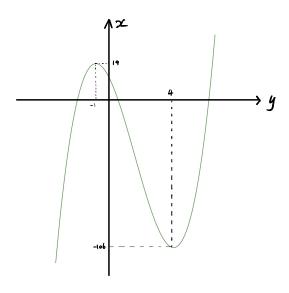
9) Minimum at 
$$(4, -106)$$
 and  $(-1, 19)$ 

10)

$$11) \quad \frac{dh}{dt} = 250\sqrt{3} \, km/h$$

12) 
$$\frac{dy}{dx} = \sec^2(x)$$
  $\frac{d^2y}{dx^2} = 2\sec^2(x)\tan(x)$   $\frac{d^3y}{dx^3} = 4\sec^2(x)\tan^2(x) + 2\sec^4(x)$ 

13) 
$$\ln(1-x) = -x - \frac{x^2}{2} - \frac{x^3}{3} - \frac{x^4}{4} - \dots$$
  $\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$ 



14) x = 1.4422496 to 7d.p.

15) 
$$\int \frac{x^4 - 27x}{3 - x} dx = -\frac{x^4}{4} - x^3 - \frac{9}{2}x^2 + C$$

16) 
$$\int \frac{\sin(3x)}{\left[1 + 2\cos(3x)\right]^3} dx = \frac{1}{12\left[1 + 2\cos(3x)\right]^2} + C$$

17) 
$$\int \frac{\cos(x)}{\sqrt[3]{4+\sin(x)}} dx = \frac{3}{2} \left[4+\sin(x)\right]^{\frac{2}{3}} + C$$

18) 
$$\int \frac{1}{\sqrt{4x^2 + 4x + 3}} dx = \frac{1}{2} \ln \left| \left( x + \frac{1}{2} \right) + \sqrt{x^2 + x + \frac{3}{4}} \right| + C$$

19) 
$$\int \sin^8(x)\cos^3(x)dx = \frac{\sin^9(x)}{9} - \frac{\sin^{11}(x)}{11} + C$$

20) 
$$\int \cos(7x)\cos(3x)dx = \frac{1}{2} \left[ \frac{\sin(10x)}{10} + \frac{\sin(4x)}{4} \right] + C$$