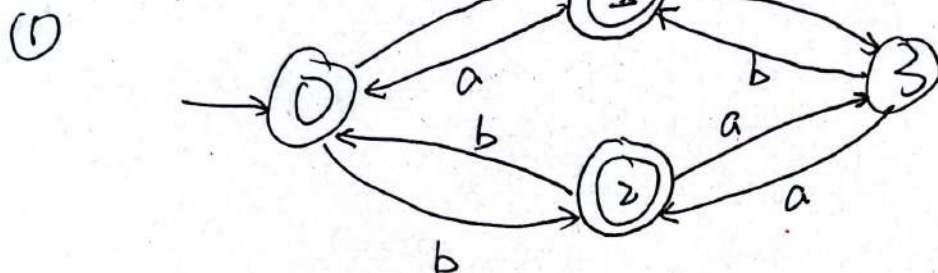


- Exercise 2.4

$L = \{ \varepsilon, a, b, bc, \overbrace{aaa, aab, aba, abb, baa, bab, bba, bbb}^3, \underbrace{aa, ab, abc, ba, bb, bbc, bca, beb}_{2} \}$

①

• Exercise 3.1.



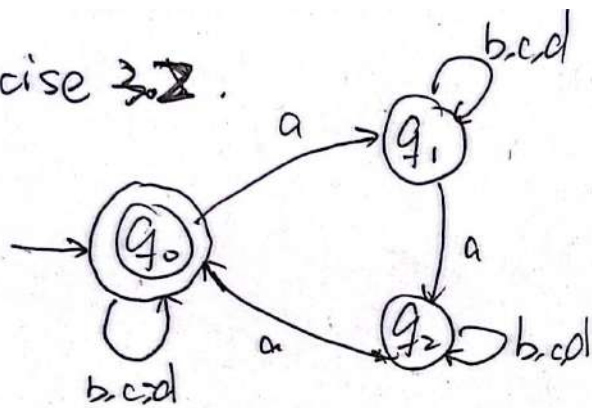
(2)  $\epsilon \times$   $b \checkmark$   $abaab \checkmark$   $bababbbba \times$

$$\begin{aligned}
 (3) \quad \hat{\delta}_A(0, abba) &= \hat{\delta}_A(\delta_A(0, a), bba) = \hat{\delta}_A(1, bba) \\
 &= \hat{\delta}_A(\delta_A(1, b), ba) = \hat{\delta}_A(3, ba) \\
 &= \hat{\delta}_A(\delta_A(3, b), a) = \hat{\delta}_A(1, a) \\
 &= \hat{\delta}_A(\delta_A(1, a), \epsilon) = \hat{\delta}_A(0, \epsilon) = 0
 \end{aligned}$$

(4)  $L(A) = \{w \mid w \text{ contains only character } a \text{ or } b \text{ and is of odd length}\}$

• Exercise 3.2.

B.



$$Q = \{q_0, q_1, q_2\}.$$

We need 3 states to represent each state of number of "a"s in word.

$$q_0: \#a \bmod 3 \equiv 0$$

$$q_1: \#a \bmod 3 \equiv 1$$

$$q_2: \#a \bmod 3 \equiv 2.$$

## Exercise 3.5

① accepted: abce. not-accepted: d.

②. NFA  $A = (Q, \Sigma, \delta_A, S, F)$ ,  $S = \{q_0, q_1, q_3\}$ .

DFA  $D(A) = (P(Q), \Sigma, \delta_{D(A)}, S, F)$ .

Transition Table.

$\delta_{D(A)}$	a	b	c
$\rightarrow * \{q_0, q_1, q_3\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_1, q_4\}$	$\{q_0, q_2, q_3\}$
$* \{q_0, q_1, q_4\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_1\}$	$\{q_0, q_2\}$
$* \{q_0, q_2, q_3\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_4\}$	$\{q_0, q_3\}$
$* \{q_0, q_1\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_1\}$	$\{q_0, q_2\}$
$* \{q_0, q_2\}$	$\{q_0, q_1, q_3\}$	$\{q_0\}$	$\{q_0\}$
$* \{q_0, q_3\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_4\}$	$\{q_0, q_3\}$
$* \{q_0, q_4\}$	$\{q_0, q_1, q_3\}$	$\{q_0\}$	$\{q_0\}$
$\{q_0\}$	$\{q_0, q_1, q_3\}$	$\{q_0\}$	$\{q_0\}$

