

## Exercise Sheet 2

Discrete Mathematics, 2020.9.22

**Note:** The following exercises involve a new logical operators  $\oplus$ . Its truth table is as follows:

$p$	$q$	$p \oplus q$
T	T	F
T	F	T
F	T	T
F	F	F

- Prove: if  $\phi \models \psi$  then  $\phi \wedge \psi \equiv \phi$  and  $\phi \vee \psi \equiv \psi$ .
  - Use the conclusion above to prove absorption laws that we learnt in class.
- Prove that  $\neg(p \oplus q) \equiv (\neg p) \oplus q$ .
  - Prove that  $p \oplus (\neg p) \oplus q \equiv \neg q$ .
- Consider the compound proposition  $\phi = \neg(p \wedge \neg(q \oplus r))$  where  $p, q, r$  are propositional variables. Give a disjunctive normal form of  $\phi$ .