A Quick Guide for the cubfits Package (Ver. 0.1-0)

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This document is written to explain the main functions of **cubfits** (Chen *et al.* 2014b), version 0.1-0. Every effort will be made to ensure future versions are consistent with these instructions, but features in later versions may not be explained in this document.

1. Introduction

Coding sequences or open reading frames (ORFs) are regions of genome encoding proteins required to properly function any living biological organism. In order to adopt to environment, growth in limited resource, or maintain population size, the protein production needs to be reflect quickly under those condition. The efficiency of protein translation is essentially critical for some tiny organism, such as yeast. For example, we may model the translation rates, from a codon sequence to a protein, with several factors and in several ways. Once the codon information encoded behind a genome is estimated/approximated appropriately, then the model can be used to predict gene expression levels or protein production rates. Therefore, it is interesting to know what factors may affect production rates, how strong they are, or whether genomes evolve accordingly.

In a simplified example, Cysteine (Cys/C) is one of 20 amino acids and can be encoded by two synonymous codons, TGT and TGC. Suppose Cysteine are observed in two coding sequences and used to encode two proteins. Suppose further one has lower expression level, but the other one has higher expression level. Assume TGT and TGC both have no effect to expression level, then the chance of observing TGT and TGC is roughly 50% and 50% among both coding sequences. Suppose the chance of observing TGC is much higher than observing TGT in the protein has higher expression level, then we may guess that TGT is more efficient than TGC for that protein translation.

cubfits (Chen *et al.* 2014b) models the biased patterns of codon usage among other information and fits model parameters. The implemented models are introduced in (Gilchrist 2007; Shah and Gilchrist 2011; Wallace *et al.* 2013) that combines several modeling techniques of Population Genetics and Statistics to predict protein production rates.

Package requirements and installation of **cubfits** are described next. Section 2 gives short examples for main functions. Section 3 provides parallel implementations that simply speedup computations, and discusses technical issues. In Section 4, useful work flows built in **cubfits** are introduced. Section 5 introduces implemented methods of data input/output and conversion between different data structures with examples. Finally, Section 6 introduces some useful functions.

1.1. Requirements

cubfits is a package of R (R Core Team 2013) built and test on R 3.0.0, but may be compatible back to 2.15.0 or early. It requires **methods** package which is default in R, and suggests **seqinr** (Charif and Lobry 2007) and **VGAM** (Yee 2013) packages that both are available and can be installed from CRAN or it's mirror sites. The **seqinr** takes care input and output of DNA sequence data in FASTA format, and the **VGAM** takes care several core functions of model fitting used by **cubfits**. The **cubfits** also uses several high performance computing techniques

to speed up computation including **parallel** (R Core Team 2012) and **pbdMPI** (Chen *et al.* 2012b).

The cubfits uses a core function vglm() of VGAM for model fitting, and (optionally) parallelizes via mclapply() of parallel package and task.pull() or pbdLapply() of pbdMPI package. The parallelization is designed across the 20 amino acids. Note that mclapply() is only supported on Unix-like systems and on shared memory machines, while tak.pull() and pbdLapply() are supported on most systems (Linux/Unix/MacOS/Windows) and on both of shared memory machines and distributed clusters provided a MPI (Gropp et al. 1994) library is installed. See Chen et al. (2014a) for more details of installation of a MPI library and pbdMPI.

1.2. Installation and Test

The **cubfits** can be either installed within an R session as

R Script

```
> install.packages("seqinr")
> install.packages("VGAM")
> install.packages("cubfits")
```

or installed from a command line as

Shell Command

```
$ R CMD INSTALL seqinr_3.7-0.tar.gz
$ R CMD INSTALL VGAM_0.3-9.tar.gz
$ R CMD INSTALL cubfits_0.1-0.tar.gz
```

provided other requirements are installed correctly. Note that **parallel** and **pbdMPI** are optional.

A simple test can be used to see if the **cubfits** installed correctly as

R Script

```
> demo(plotbin, 'cubfits')
```

within an R session, and this demo provides a plot as in Figure 1.

2. Main Functions

The **cubfits** package is composed of three main functions:

- 1. cubfits() fits models for sequences with observed ϕ (expression level) values and measurement errors,
- 2. cubappr() approximates models for sequences without any observed ϕ values, and
- 3. cubpred() fits models for sequences with observed ϕ values and measurement errors, and then predicts ϕ values for sequences without observations.

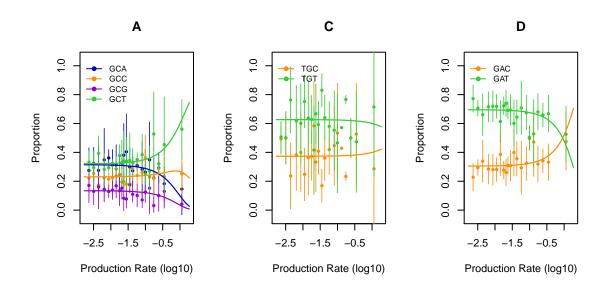


Figure 1: A simple demo plot. Figures show the empirical binning results by expression levels where dots are mean proportions of synonymous codons of 100 sequences in every 5% expression windows, and horizontal lines are 90% empirical intervals. The curves are theoretical prediction of synonymous codon usages (Shah and Gilchrist 2011). See Section 6 for details. For amino acid A, the selection effect dominates the mutation effect for some codons at expression level larger than -1.5. For C, it is mainly mutation effect. For D, the selection effect can be observed at expression level larger than -0.75.

See package's help pages for details of other input options.¹

2.1. Demonstrations

The **cubfits** package provides quick examples for its three main functions:

```
R Script

> demo(roc.train, 'cubfits')  # for cubfits()
> demo(roc.appr, 'cubfits')  # for cubappr()
> demo(roc.pred, 'cubfits')  # for cubpred()
```

These **cubfits** demos perform short MCMC runs and analyze toy datasets (ex.train and ex.test) for the Ribosome Overhead Cost (ROC) model (Shah and Gilchrist 2011) which is shown in Figure 1. The toy datasets have only 100 short sequences, and only 3 amino acids are considered.

For a standard data analysis, the process essentially consists of:

- 1. reading sequences and expressions files,
- 2. converting to appropriate data structures,
- 3. running a main function (MCMC),

¹ ?cubfits::cubfits, ?cubfits::cubappr, and ?cubfits::cubpred.

- 4. summarizing MCMC outputs, and
- 5. plotting predictions.

The **cubfits** package also provides an example using simulated data:

```
R Script
> demo(simu.roc, 'cubfits') # cubfits() is called.
```

Note that this demo will generate a fake sequence file (toy_roc.fasta) in FASTA format in the working directory, and (for testing) read it back. Also, it converts the data into the correct format needed by cubfits(), and finally runs MCMC and generates a plot.

2.2. Generic Functions (Aside)

Note that the three main functions are wrappers of other generic functions that perform parameter initializations, propose new parameters, compute MCMC acceptance/rejection ratio, and more. The function init.function() initializes generic functions that will be called by the three main functions. Although init.function() is called within each of three main functions to setup the generic functions, it also needs to be called before using other utility functions, such as fitMultinom(), see Section 6 for examples.

Accompanying control variables such as .CF.CT and .CF.OP, the init.function() will dispatch the corresponding generic functions into a default environment .cubfitsEnv, allowing other main functions may call those generic functions dynamically.

Note that generic functions in R typically only depend on input object types. However, the design in **cubfits** has several advantages:

- functions are clearer by making good use of data structures and simplifying options,
- extensions are easier to create; simply add more generic functions rather than changing main functions, and
- performance is more efficient by avoiding extra conditional checks such as if (...) {...} else {...} in every iteration.

Also, the design can avoid tedious CRAN checks since there are some restrictions in accessing .GlobalEnv. For example, .cubfitsEnv\$my.fitMultinomAll() is called in several internal functions to fit multinomial logistic regression in every MCMC iterations. In particular, it has four generic functions:

- 1. my.fitMultinomAll.lapply() ueses lapply() in the serial version,
- 2. my.fitMultinomAll.mclapply() uses parallel::mclapply() in shared memory machines,
- my.fitMultinomAll.task.pull() uses pbdMPI::task.pull() in distributed clusters, and
- 4. my.fitMultinomAll.pbdLapply() uses pbdMPI::pbdLapply() in distributed clusters, but is only efficient for homogeneous tasks.

Through init.function(), there is no need to check which generic function should be called within the MCMC step, and there is no need to worry about serial or parallel details when designing a MCMC algorithm.

3. Speedup (Aside)

The main bottleneck of **cubfits** is in calls to fitMultinom*() or my.fitMultinom*(). The reasons are that

- models assume conditional independence of amino acids, and
- it is tedious to extract parallelism within the VGAM::vglm() function.²

Fortunately, by carefully utilizing summarized data structures, one can avoid some burdens and boost the MCMC computation significantly. For example, sorting by ORF's names before MCMC may avoid subsetting a data.frame in some cases, and further computation can be easily moved to C.

Further, **cubfits** offers three ways of parallelizing computations to speedup computations, including parallel::mclapply(), pbdMPI::task.pull(), and pbdMPI::pbdLapply(). Note that only **pbdMPI** functions have received the most thorough testing in **cubfits**. We now briefly describe these three approaches.

3.1. mclapply

The function mclapply() is a function in the parallel package and is particularly useful for multi-core/shared memory machines; however, as it relies on the system's fork utility, it is only available for Unix-like systems such as Linux and Mac OS. On Windows systems, this function is identical to lapply(). As the name implies, mclapply() is a parallel version of R's own lapply(), and as such it is usually trivial to migrate to mclapply() from code using lapply().

With this approach in **cubfits**, we split the work into jobs (tasks) at the level of 20 amino acids, because of the conditional independence assumption. However, the computation is not evenly distributed across amino acids, as some have more synonymous codons than others; e.g. Leucine (Leu/L) has 6 synonymous codons. In other words, the 20 jobs are not homogeneous (and as an aside, Leucine generally needs the most computing in those fitMultinom*() calls). Therefore, we use the mclapply() option mc.preschedule = FALSE, and limit the number of cores to 4 or 5. In doing so, we are able to somewhat overcome this computational imbalance.

The warning section of the mclapply() help page notes that it is _strongly discouraged_ to use these functions in GUI or embedded environments. For small tests, i.e. those with fewer sequences and shorter MCMC iterations, the mclapply() approach works well and with reasonable efficiency in cubfits. However, we did observe some occasional crashes when using this approach for longer runs of MCMC, such as in a work flow.

² As long as the number of sequences is not too large and summary statistics are used, there is no need to consider this approach. Although this can lead to huge improvement in speed, it may require the need to rewrite all of vglm() and reorganize data structures, which is highly non-trivial.

3.2. task.pull

The **pbdMPI** package is designed in single program multiple data (SPMD) framework, and is a simpler approach to parallelize codes than the perhaps more familiar manager/worker paradigm. Although only batch computing (i.e., no interactivity) is allowed in **pbdMPI**, one of the benefits is that it is not strictly limited to shared memory machines, and can be applied on most systems with an MPI library installed. See Chen *et al.* (2014a) for details on installing an MPI library and **pbdMPI**.

The task pull is a simple parallelism strategy and is very similar to mc.preschedule = FALSE in mclapply(); in particular, this approach gains performance economically for non-homogeneous jobs. task.pull() in pbdMPI is a convenient implementation that can boost the performance of fitMultinom*() functions, and has similar syntax as mclapply().

3.3. pbdLapply

For some cases, task pull is neither economical nor efficient. For example, in **cubfits**, one needs to initialize the expected expression level of each sequence via a call to **estimatePhiAll*()**. Generally, this performs the same computation on all sequences. Therefore, a task pull on 5,000 sequences may not be a good idea, since the extra 5,000 calls for requesting unfinished sequences are unavoidable in this approach.

The function pbdLapply() is similar to set mc.preschedule = TRUE in mclapply(). The 5,000 sequences are equally divided by the number of cores available for processing and processed by each core simultaneously. As such, there is no call for requesting sequences. A good choice of the number of cores to use is generally related to the number of sequences. However, this needs to be tuned with a few empirical runs for optimal performance.

3.4. Performance

The above three methods of parallelizing cubfits calls, (mclapply(), task.pull(), and task.pull()), have all been tested on a Yeast genome which has about 5346 genes and corresponding gene expression. The average run times of 200 iterations of cubfits() are recorded in different numbers of cores. The speedup via parallelization is defined as the run time of one core of mclapply() divided by the run time of the parallel version.

Figure 2 shows that for this test, task.pull() is the best approach, although it needs an additional core for task management. There is no obvious best choice for number of cores, but after about seven cores, task.pull() is beginning to level out. The performance degradation of pbdLapply() at 8 cores is due to the unbalanced pre-assignment of amino acids; e.g. Leu and Arg, both computationally expensive amino acids, may be assigned to the same core. The performance of mclapply() is surprisingly poor by comparison, which may be due to memory copying between the eforking mechanism and mc.preschedule = FALSE.

4. Work Flows

Warning: All work flows are intended to be run in batch mode and on Unix-like systems for optimum performance.

The cubfits package is built with some useful work flows, including

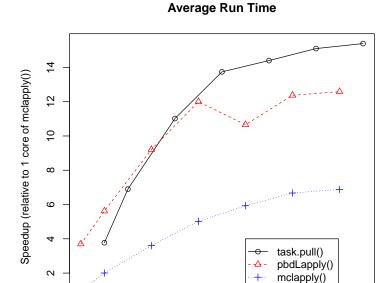


Figure 2: Speedup of three different parallelizations.

Number of cores

6

10

8

12

- 1. simu for simulation studies,
- 2. wphi for sequences with expression levels and measurement errors, and

4

3. wophi for sequences without expression levels.

2

We share these work flows as templates which may be useful for further research. A quick way to obtain a default work flow is by calling cubfits::cp.workflow(), which contains the three aforementioned work flows. Note however that these are only tested privately under a Linux environment, and are merely served as templates. None of them are checked by CRAN. The work flows are stored in the package directory cubfits/inst/workflow/ and installed in \${R_HOME}/library/cubfits/workflow/. Therefore, executing the following script can

Shell Command

regenerate those work flows in three directories ./01-simu/, ./02-wphi/, and ./03-wophi/.

```
$ mkdir 01-simu
$ cd 01-simu/
$ Rscript -e "cubfits::cp.workflow('simu')"
$ cd ../
$ mkdir 02-wphi
$ cd 02-wphi/
$ Rscript -e "cubfits::cp.workflow('wphi')"
$ cd ../
$ mkdir 03-wophi
```

```
$ cd 03-wophi/
$ Rscript -e "cubfits::cp.workflow('wophi')"
$ cd ../
```

Note that a work flow is mainly coded in shell script and sequentially executes analyses via several shell commands and R scripts. The analysis R scripts are managed and stored in cubfits/inst/workflow/code/ and installed in \${R_HOME}/library/cubfits/workflow/code/. Those are served as templates and can be altered by users (copy scripts to local directory and modify as needed.)

After regenerating those work flows, three shell scripts and one R script are created within each directory. These scripts consist of:

- run_0.sh creates the needed subdirectories,
- run_1.sh is the main script of analysis,³
- run_2.sh is for post processing, and
- 00-set_env.r is the R script for cubfits configuration.

For simu work flow, one can sequentially execute those shell scripts (run_*.sh) without further changes, and may learn to adjust scripts for further studies. For wphi and wophi work flows, one needs to provide genome sequences (e.g. ./02-wphi/param/genome.fasta) and expression data (e.g. ./02-wphi/param/genome.phi.tsv).

Examples of post processing from the simu work flow (as in (run_2.sh) are given in Figure 3. The plots are from files ./01-simu/all.out/plot/prxy_roc_ad_fits_pm_5k-10k.pdf and ./01-simu/all.out/plot/prxy_roc_ad_appr_pm_5k-10k.pdf.

5. Utilities

The **cubfits** package provides simplified data input and output utilities that can quickly import sequence and expression values, turn them into R data structures, and dump analysis results in a standard format. As long as data are in this common format, the following functions simplify analysis work flows as in Section 4. Further, the R data structures used in **cubfits** can be converted to different formats after reading in from disk and/or before writing out to disk.

5.1. Data I/O Functions

- read.seq() reads sequence data in FASTA format, and
- write.seq() writes sequence data in FASTA format.

Both functions are simplified wrapper functions of package **seqinr**. The writing function is mainly intended for simulation studies, as described in the section above.

³ This may require up to 30 cores and may take a few hours to finish depending on the number of sequences. Please do some testing and adjust this file and O0-set_env.r accordingly before a hero run.

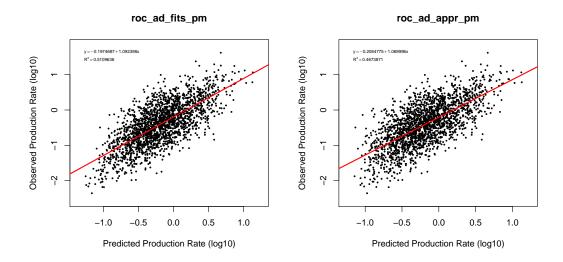


Figure 3: The left plot is predicted expression (MCMC posterior mean of expected expression) from model fits against observed expression (with measurement errors). In the right plot, the predicted expression is approximated from a simulation (no model fits.)

- read.phi() reads in expression values in tsv/csv format, and
- write.phi() writes out expression values in tsv/csv format.

The default data structure for these is an R data.frame. The writing function is mainly for simulation studies.

5.2. Main Data Structures

The main data structures used in **cubfits** are:

- reu13.df (used by REU13 students) contains codon positions and expression levels,
- y (used by REU12 students and Wallace et al. (2013)) contains synonymous codon counts for each sequence,
- n (used by REU12 students and Wallace et al. (2013)) contains total codon count for each sequence,
- reu13.list is a list version of reu13.df (adopted by WCC),
- y.list is a list version of y (adopted by WCC), and
- n.list is a list version of n (adopted by WCC).

These are typically fixed after data input steps and mainly used in the three main functions without further changes. Note that the objects with these data structures are normally sorted by ORF id's or names. The list versions are also useful for some models and speedup model fitting. Some conversion functions between data structures are provided in **cubfits**, see Section 5.3 for details.

Also, there are other data structures for parameters, but those are sometimes model dependent. For example, data structure b may contain model parameters in different dimension. The parameters of each amino acid are $(log(\mu), \Delta t)$ for ROC model, $(log(\mu), \omega)$ for NSEf model, and $(log(\mu), \Delta t, \omega)$ for ROC+NSEf model. See help pages (?cubfits::AllDataFormats) for details.

The following is an example of reu13.df data structure containing three amino acids A, C, and D. Each amino acid is in data.frame with four required columns ORF (sequence id), phi (expression level), Pos (codon position), and Codon, and one optional column Codon.id (created by rearrange.reu13.df() within gen.reu13.df() call.)

Example of reu13.df

```
> str(ex.train$reu13.df)
List of 3
$ A:'data.frame':
                        2682 obs. of
                                      5 variables:
             : chr [1:2682] "YBL023C" "YBL023C" "YBL023C" "YBL023C"
  ..$ ORF
             : num [1:2682] 0.0186 0.0186 0.0186 0.0186 ...
  ..$ phi
              : num [1:2682] 109 353 123 294 1133 ...
             : chr [1:2682] "GCA" "GCA" "GCA" "GCA" ...
  ..$ Codon
  ..$ Codon.id: int [1:2682] 0 0 0 0 0 0 0 0 0 ...
$ C:'data.frame':
                        662 obs. of
                                    5 variables:
             : chr [1:662] "YBL023C" "YBL023C" "YBL023C" "YBL023C"
  ..$ ORF
     . . .
             : num [1:662] 0.0186 0.0186 0.0186 0.0186 ...
  ..$ phi
  ..$ Pos
             : num [1:662] 387 862 813 248 226 40 82 477 922 87 ...
  ...$ Codon : chr [1:662] "TGC" "TGC" "TGC" "TGT" ...
  ..$ Codon.id: int [1:662] 0 0 0 1 1 1 1 1 1 1 ...
                        3164 obs. of
$ D:'data.frame':
                                      5 variables:
             : chr [1:3164] "YBL023C" "YBL023C" "YBL023C" "YBL023C"
  ..$ ORF
     . . .
  ..$ phi
             : num [1:3164] 0.0186 0.0186 0.0186 0.0186 ...
  ..$ Pos
              : num [1:3164] 209 199 255 89 273 141 263 158 112 306
  ..$ Codon
             : chr [1:3164] "GAC" "GAC" "GAC" "GAC"
  ..$ Codon.id: int [1:3164] 0 0 0 0 0 0 0 0 0 ...
```

The following is an example of corresponding y which has only synonymous codon counts for each amino acids and sequences.

Example of y

```
> str(ex.train$y)
List of 3
$ A: int [1:100, 1:4] 16 4 5 17 5 7 4 0 20 13 ...
..- attr(*, "dimnames")=List of 2
....$ : chr [1:100] "YBL023C" "YBL074C" "YBR060C" "YBR068C" ...
...$ : chr [1:4] "GCA" "GCC" "GCG" "GCT"

$ C: int [1:100, 1:2] 3 0 1 5 4 2 4 2 0 11 ...
..- attr(*, "dimnames")=List of 2
....$ : chr [1:100] "YBL023C" "YBL074C" "YBR060C" "YBR068C" ...
...$ : chr [1:2] "TGC" "TGT"

$ D: int [1:100, 1:2] 15 10 10 11 6 12 8 2 17 27 ...
```

```
..- attr(*, "dimnames")=List of 2
.. ..$ : chr [1:100] "YBL023C" "YBL074C" "YBR060C" "YBR068C" ...
.. ..$ : chr [1:2] "GAC" "GAT"
```

The following is an example of corresponding n which has only total codon counts for each amino acids and sequences.

Example of n

5.3. Conversion of Data Structures

In order to improve performance, simply parallelizing the code is not enough. In R, a good data structure can have massive impact on performance. In practice, it is best that not to change/modify/subset existing data structures within computations/iterations. It can be worth generating extra data structures which are efficient for some specific functions or particular computation, even if the information is at times redundant.

However, managing different data structures could be a nightmare in maintaining consistency across function calls. **cubfits** provides several utilities to generate (gen*()) or convert (convert*()) extended data structures, such as reu13.list, n.list, and y.list. See help pages (?cubfits::DataGenerating and ?cubfits::DataConverting) for details.

Finally, **cubfits** provides a simple demo

```
R Script
```

```
> demo(basic, 'cubfits')
```

and shows how those generating and converting functions work. Note that this demo reads two example files from **cubfits** and turns them into main data structures which can be called by the three main functions introduced in Section 2. The files are seq_200.fasta containing 200 sequences and phi_200.tsv containing the corresponding expression levels. Both files are stored in the package directory cubfits/inst/ex_data/ and installed in \${R_HOME}/library/cubfits/ex_data/.

6. Miscellaneous

6.1. Multinomial Logistic Regression

fitMultinom() is a utility function which can fit an ROC model with ϕ values, assuming no measurement errors as in Shah and Gilchrist (2011). A typical usage is:

```
R Script
demo(fitMultinom, 'cubfit')
```

or

R Script

where fitlist is an object of b data structure containing all estimations of $(log(\mu), \Delta t)$ for each synonymous codon and amino acid. This is a quick fit assuming no measurement error on expression levels. This demo returns plots in Figure 4

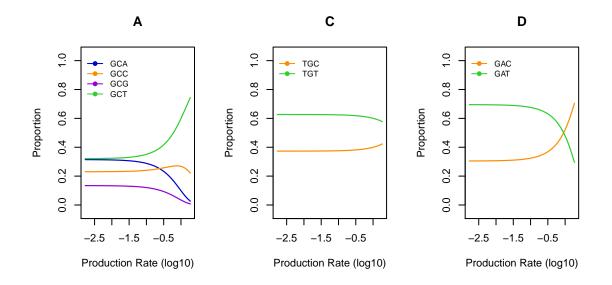


Figure 4: A simple prediction plot, similar to Figure 1 except empirical binning.

Important: Note that init.function(model = "roc") initializes generic functions for the ROC model and fitMultinom() can access corresponding generic functions from the

.cubfitsEnv environment. The generic function then performs multinomial logistic regression on the input summarized statistics, and VGAM::vglm() can fit and return parameter estimations. Therefore, there is only need to initialize once before MCMC iterations, such as the three main function in Section 2. For performance issues, all calls within MCMC iterations should access generic functions, such as via .cubfitEnv\$fitMultinom() regardless of the model. Do NOT access fitMultinom() within any MCMC iteration.

6.2. Asymmetric Laplace Distribution

As with the regular R functions for different distributions (dnorm(), pnorm(), etc.), cubfits provides analogous functions for asymmetric Laplace distribution (ASL) such as rasl(), dasl(), pasl(), and qasl(). See (Kotz et al. 2001) for more details about the ASL distribution. Finding a MLE numerically is possible for ASL random samples and is implemented in the asl.optim().

For example, Yassour dataset (Yassour *et al.* 2009) has 6303 gene expression measurements and four replicates. I took the geometric averaged mean of the replicates for each gene and fitted the ASL model to the means of 6303 genes as suggested by Wallace *et al.* (2013). The data distribution and the ASL fits are shown in Figures 5a which can be done as the next.

R Script

```
> demo(yassour.asl, 'cubfits')
```

Further, I also used normal mixture models to fit the same data using the EM algorithm implemented in the **EMCluster** (Chen *et al.* 2012a) package. Figure 5b shows the fits for K = 1, 2, ..., 6 components of normal mixture models, which can be done via a call to

R Script

```
> demo(yassour.mixture, 'cubfits')
```

Table 1 provides some details for model comparison. Note that K=6 has a smaller log likelihood than K=5. This means that the EM algorithm converges to local optimum and may indicate an overestimated number of components. K=4 is the best choice among all models by the smallest BIC.

Model	p	$\log L$	AIC	BIC
ASL	3	-10739.84	21485.68	21505.93
Normal / $K = 1$	2	-11033.55	22071.10	22084.60
K = 2	5	-10820.47	21650.93	21684.68
K = 3	8	-10687.06	21390.12	21444.11
K = 4	11	-10655.55	21333.10	21407.34
K = 5	14	-10649.69	21327.38	21421.87
K=6	17	-10653.19	21340.38	21455.11

Table 1: K is the number of components for the mixture normal model and K=1 is equivalent to normal model. p is the number of parameters for the fitted model, $\log L$ is the log likelihood, $AIC = -2 \log L + 2p$, and $BIC = -2 \log L + p \log(n)$ where n = 6303 is the number of samples.

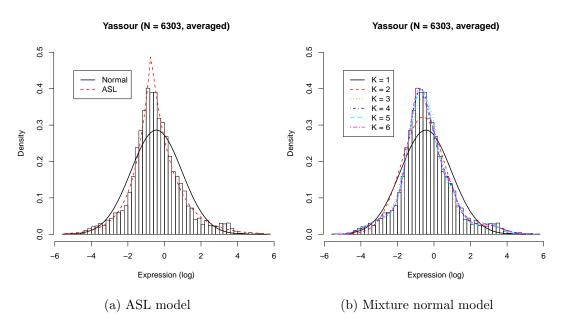


Figure 5: Different distribution fits to Yassour dataset.

References

Charif D, Lobry J (2007). "SeqinR 1.0-2: a contributed package to the R project for statistical computing devoted to biological sequences retrieval and analysis." In U Bastolla, M Porto, H Roman, M Vendruscolo (eds.), Structural approaches to sequence evolution: Molecules, networks, populations, Biological and Medical Physics, Biomedical Engineering, pp. 207–232. Springer Verlag, New York. ISBN: 978-3-540-35305-8.

Chen WC, Maitra R, Melnykov V (2012a). "EMCluster: EM Algorithm for Model-Based Clustering of Finite Mixture Gaussian Distribution." R Package, URL http://cran.r-project.org/package=EMCluster.

Chen WC, Ostrouchov G, Schmidt D, Patel P, Yu H (2012b). "pbdMPI: Programming with Big Data – Interface to MPI." R Package, URL http://cran.r-project.org/package=pbdMPI.

Chen WC, Ostrouchov G, Schmidt D, Patel P, Yu H (2014a). A Quick Guide for the pbdMPI package (Ver. 0.2-2). R Vignette, URL http://cran.r-project.org/package=pbdMPI.

Chen WC, Zaretzki R, Howell W, Schmidt D, Gilchrist M (2014b). "cubfits: Codon Usage Bias Fits." R Package, URL http://cran.r-project.org/package=cubfits.

Gilchrist M (2007). "Combining Models of Protein Translation and Population Genetics to Predict Protein Production Rates from Codon Usage Patterns." Mol. Biol. Evol., 24, 2362 – 2373.

Gropp W, Lusk E, Skjellum A (1994). Using MPI: Portable Parallel Programming with the Message-Passing Interface. Cambridge, MA, USA: MIT Press Scientific And Engineering Computation Series.

- Kotz S, Kozubowski T, Podgorski K (2001). The Laplace distribution and generalizations: a revisit with applications to communications, economics, engineering, and finance. Boston: Birkhauser.
- R Core Team (2012). "parallel: Support for Parallel Computation in R." R Package.
- R Core Team (2013). R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing, Vienna, Austria. URL http://www.R-project.org.
- Shah P, Gilchrist M (2011). "Explaining Complex Codon Usage Patterns with Selection for Translational Efficiency, Mutation Bias, and Genetic Drift." *Proc. Natl. Acad. Sci. U.S.A.*, **108**, 10231 10236.
- Wallace E, Airoldi E, Drummond D (2013). "Estimating Selection on Synonymous Codon Usage from Noisy Experimental Data." Mol. Biol. Evol., 30(6), 1438 1453.
- Yassour M, Kaplan T, Fraser H, Levin J, Pfiffner J, Adiconis X, Schroth G, Luo S, Khrebtukova I, Gnirke A, Nusbaum C, Thompson D, Friedman N, Regev A (2009). "Ab initio construction of a eukaryotic transcriptome by massively parallel mRNA sequencing." *Proc. Natl. Acad. Sci. U.S.A.*, **106**, 3264 3269.
- Yee T (2013). "VGAM: Vector Generalized Linear and Additive Models." R Package version 0.9-3, URL http://CRAN.R-project.org/package=VGAM.