



GRAPH-NETS IN HEP: A PRACTICAL TUTORIAL

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LIP Big Data 1st thematic workshop, Online - 12/07/21

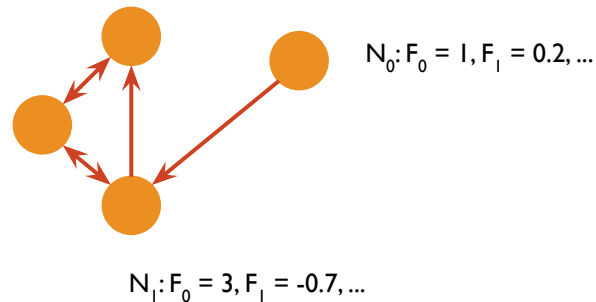


OVERVIEW

1. Graph data and tasks
2. Graph examples in HEP
3. A few architectures
4. Practical tutorial

GRAPHS

- A *graph* consists of:
 - *Nodes/Vertices*, each with a set of features
 - *Edges* which connect vertices together and imply an interaction between the pair of nodes
 - Edges can be unidirectional and not all possible edges have to exist
- Twitter example:
 - People (nodes) with tweets (features) connected by both uni- and bi-directional edges (following & mutual follows)
 - Not everyone is connected to everyone else (some edges don't exist)



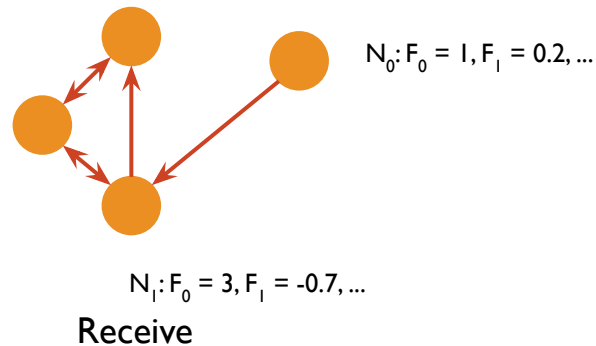
GRAPHS

- Can represent graph as:
 - A matrix of nodes with features (N, F) or (F, N)
 - An (N,N) adjacency matrix of connections between nodes
 - Nodes are also connected to themselves

	F		
N	1	0.2	...
	3	-0.7	...

Send

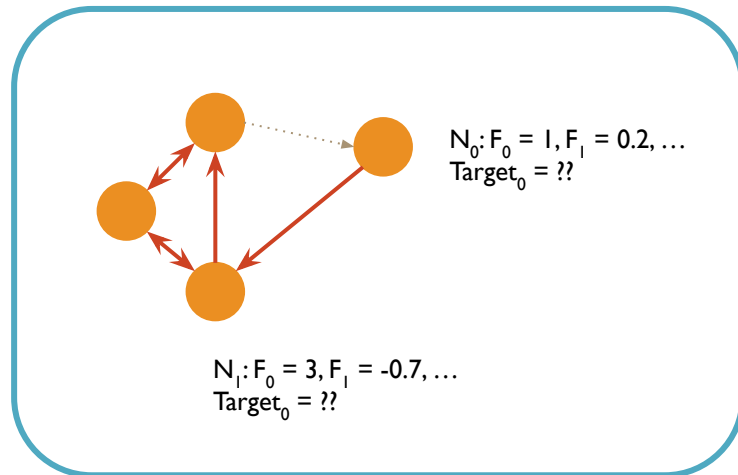
1	1	0	0
0	1	1	1
0	1	1	1
0	0	1	1



GRAPH-TASKS

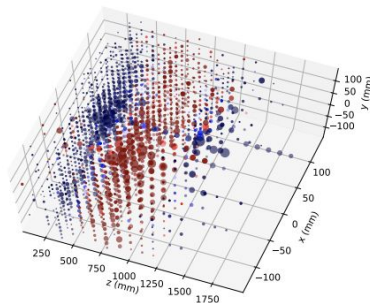
- Three general task categories
- Node-level predictions:
 - Given a graph, predict the values of unknown features for every node
- Edge-level predictions:
 - Given a set of nodes, predict whether each possible edge-connection exists
- Graph-level predictions:
 - Given a graph, predict the values of unknown features for the entire graph

$G_0: \text{Target}_0 = ??$

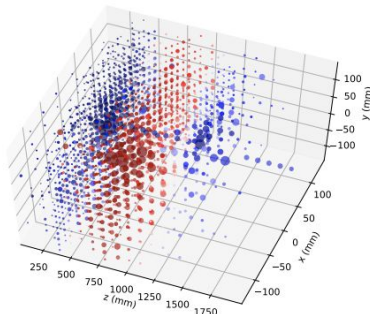


HEP EXAMPLES

- Generally in HEP, assume every node is connected to every other node
 - All edges exist and are bi-directional
- Node-level predictions: Assign detector hits to different showers (e.g. [Qasim et al. 2019](#), right)
 - Hits are nodes with energy & position features
 - Graph is an event
- Graph-level predictions: Jet tagging (e.g. [Qu & Gouskos 2019](#))
 - Particles are nodes with 4-momentum
 - Graph is a jet
- Hybrid: Particle flow (e.g. [Kieseler 2020](#)) - assign hits to objects and predict properties of objects



(a) Truth



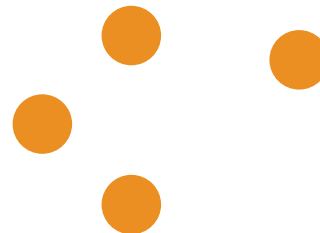
(b) Reconstructed

ADVANTAGES OF GRAPHS

- No assumed regularity of node positions:
 - CNNs rely on grid-layout of pixels, but what if you detector has an irregular layout?
 - Node features allow us to specify node position (or learn a latent-space embedding)
- No assumed ordering of nodes:
 - DNNs, CNNs, & RNNs require inputs to be ordered somehow
 - For some domains ordering is intuitive (start at top-left of image, read text in word-order, etc.)
 - But in HEP recorded particles *exist simultaneously* but we must order them by a criterion and hope it is optimal
 - Graphs also present all nodes simultaneously with no sense of priority
 - N.B. For graph-level predictions, care must be take to retain order-invariance (see next slide)
- Graphs are flexible: nodes and edges can be created or destroyed

SIMPLE APPROACH TO GRAPHS

- Take a single DNN and apply it to every node in the graph:
 - Inputs are node features
 - DNN weights are shared like a CNN
 - Provides set of predictions per node
- Node-level tasks:
 - The DNN predictions are the target features for the node



$N_i: F_0 = 3, F_1 = -0.7, \dots$

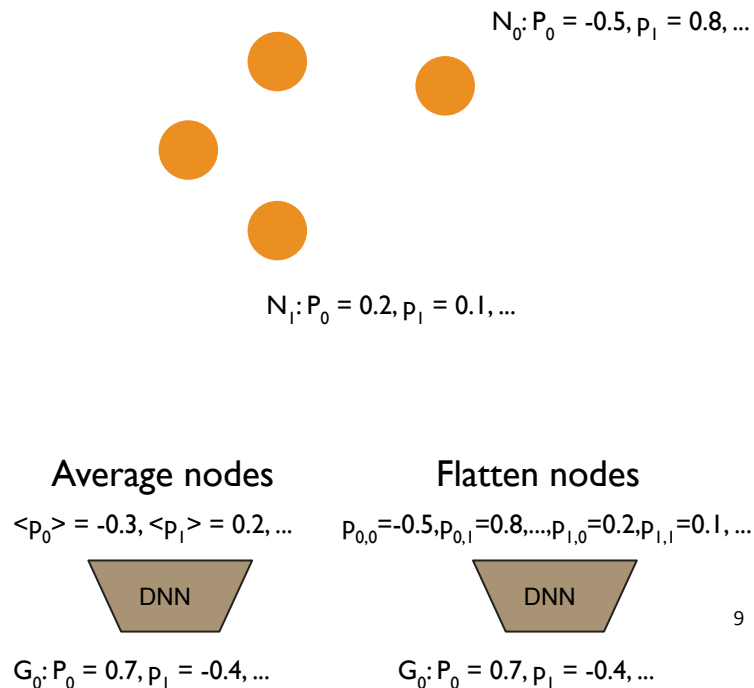


$N_i: P_0 = 0.2, p_1 = 0.1, \dots$

Apply same DNN to every node

SIMPLE APPROACH TO GRAPHS

- Graph-level predictions:
 - Aggregate the node predictions, either:
 - Take the average/maximum of every node prediction - retains order invariance but loses information
 - Reshape node predictions - requires nodes to be ordered but retains information
 - Feed aggregate features through second DNN to get graph-level prediction

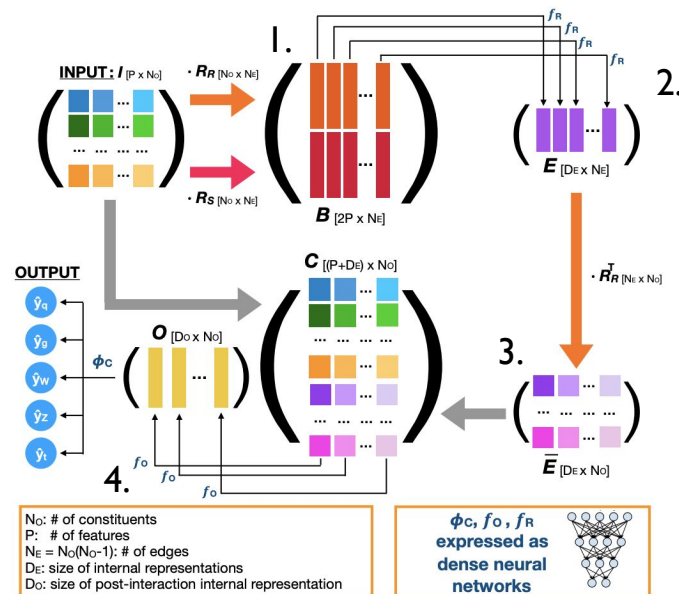


GRAPH-NETS

- The simple approach works but ignores the connections to other nodes in the graph
- A Graph Neural Network still provides predictions per node, but also has a mechanism to consider the features of the other nodes when predicting each node
 - The mechanism (*message passing*) varies according to GNN architecture

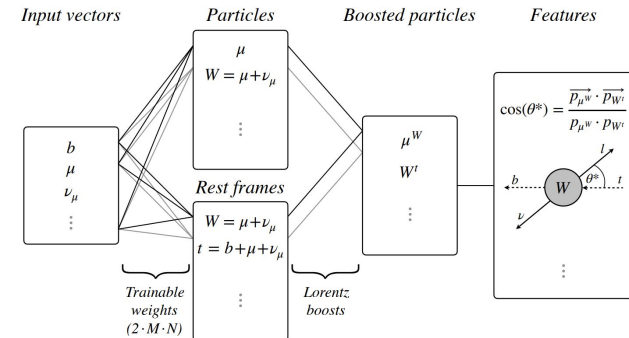
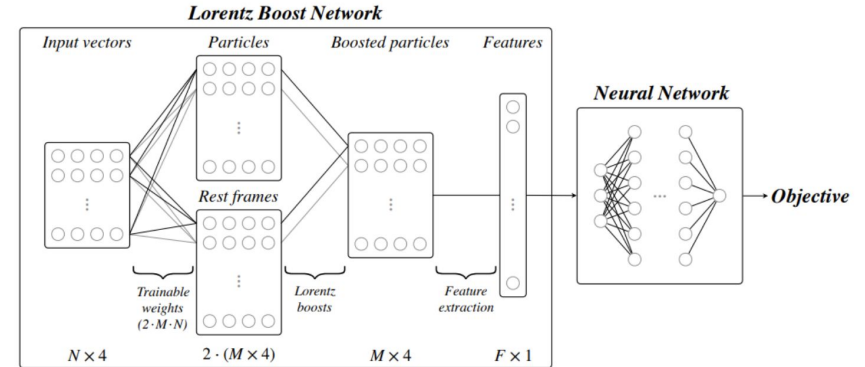
INTERACTION NET

- Originally for physical simulations
([Battaglia et al. 2016](#))
 - Applied to HEP by [Moreno et al. 2019](#)
- 1. Combine features along edges
 - Implemented by fixed sending & receiving matrices
- 2. Apply DNN to learn internal transformation for each node
- 3. Apply transformation to each node and concat with original features
- 4. Apply 2nd DNN to learn output features per node



LORENTZ-BOOST NETWORK

- [Erdmann et al., 2018](#)
- HEP-specific arch for learned feature extraction from 4-momenta
 - Creates new boosted particles by learning both new particles and restframes by combining input particles
 - Particles & restframes are linear combinations of inputs, with learnable coefficients
 - Computes pre-specified high-level features using (combinations of) the boosted particles
 - Lorentz boost requires inputs are *physical*
- Reduces impact of HL-feature selection/specification by providing means to learn optimal particles for the chosen features
 - LUMIN implementation offers a further relaxation by replacing the fixed feature extraction with a pair of DNNs:
 - One extracts N features each particle
 - The other extracts M features from every combination of particle pairs

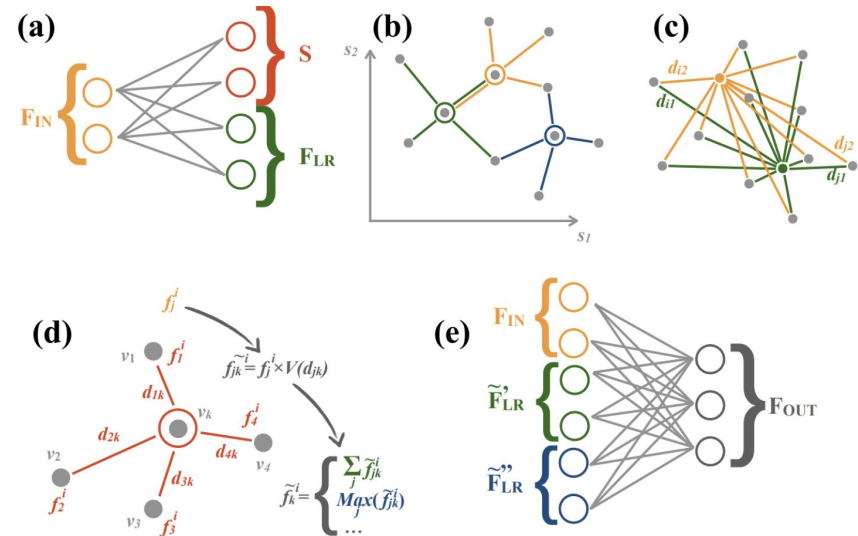


DEALING WITH LARGE GRAPHS

- Typical problem with graphs: slow to evaluate with many nodes
- Greedy approach: prediction of a single node depends on all connected nodes + self
- Heuristic approach: learn which other nodes are actually required

GRAVNET

- [Quasim et al., 2019](#)
- A) Initial DNN learns new features (F_{lr}) + latent-space coords (S) per node based on node features (F_{IN})
- B) Graph constructed by only connecting each node to its k -nearest neighbours in latent-space (Euclidean separation in S)
- D) Node features (f_j^i) “seen” by a given node are:
 - Weighted by a potential according to Euclidean distance, e.g. $\exp(-10 \cdot d_{jk}^2)$ (f_{jk}^i)
 - Aggregated by order-invariant functions, e.g. average & maximum (\tilde{f}_k^i)
 - The neighbour-features are then concatenated with the original features of the node
- E) A second DNN computes the output features per node based on the F_{IN} & \tilde{f}_k^i features





PRACTICAL TUTORIAL - GILES

TOP TAGGING

- Binary classification of jets (0=QCD, 1=Top)
 - Inputs are 4-momenta of 1st 200 sub-jets (p_t ordered)
 - [Full details](#)
- For GNN task:
 - Sub-jets are nodes
 - 4-momenta are features
 - Jets are graphs
 - Graph-level classification problem

	AUC	Acc	$1/\epsilon_B$ ($\epsilon_S = 0.3$)			#Param
			single	mean	median	
CNN [25]	0.981	0.930	914±14	995±15	975±18	610k
ResNeXt [40]	0.984	0.936	1122±47	1270±28	1286±31	1.46M
TopoDNN [27]	0.972	0.916	295±5	382± 5	378 ± 8	59k
Multi-body N -subjettiness 6 [33]	0.979	0.922	792±18	798±12	808±13	57k
Multi-body N -subjettiness 8 [33]	0.981	0.929	867±15	918±20	926±18	58k
TreeNiN [52]	0.982	0.933	1025±11	1202±23	1188±24	34k
P-CNN	0.980	0.930	732±24	845±13	834±14	348k
ParticleNet [56]	0.985	0.938	1298±46	1412±45	1393±41	498k
LBN [28]	0.981	0.931	836±17	859±67	966±20	705k
LoLa [31]	0.980	0.929	722±17	768±11	765±11	127k
LDA [63]	0.955	0.892	151±0.4	151.5±0.5	151.7±0.4	184k
Energy Flow Polynomials [30]	0.980	0.932	384			1k
Energy Flow Network [32]	0.979	0.927	633±31	729±13	726±11	82k
Particle Flow Network [32]	0.982	0.932	891±18	1063±21	1052±29	82k
GoaT	0.985	0.939	1368±140		1549±208	35k

RUNNING THE TUTORIAL

- Dedicated software repo:
https://github.com/GilesStrong/workshop_LIP_GNN
- Either run-locally, or use Google Colab:
https://colab.research.google.com/github/GilesStrong/workshop_LIP_GNN/blob/main/GravNet_for_top_tagging.ipynb
- Subsampled, preprocessed data available from
<https://cernbox.cern.ch/index.php/s/YsKrkmIM6rBcnfG/download>
 - Link will be deactivated on 18/07/21 - afterwards use official source (notebook contains the preprocessing code, but the full dataset is large)