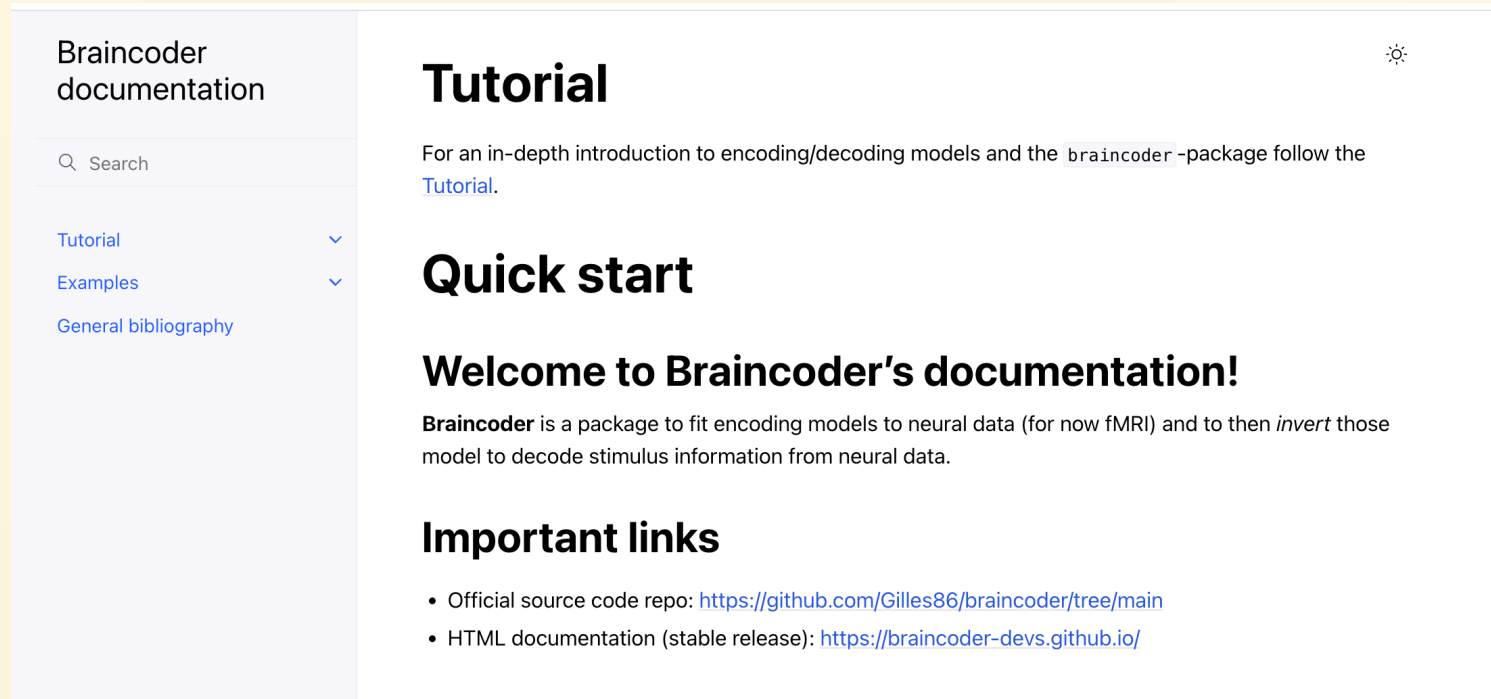


braincoder: (Encoding &) Decoding Neural Data

A screenshot of the Braincoder documentation website. The left sidebar is light blue and contains the text 'Braincoder documentation' at the top, followed by a search bar with a magnifying glass icon and the text 'Search'. Below the search bar are three links: 'Tutorial' with a downward arrow, 'Examples' with a downward arrow, and 'General bibliography'. The main content area is white and features a 'Tutorial' section with a sun icon in the top right corner. The text in the Tutorial section reads: 'For an in-depth introduction to encoding/decoding models and the braincoder -package follow the Tutorial.' Below this is a 'Quick start' section, followed by a 'Welcome to Braincoder's documentation!' section. The welcome section contains a paragraph: 'Braincoder is a package to fit encoding models to neural data (for now fMRI) and to then invert those model to decode stimulus information from neural data.' Below the welcome section is an 'Important links' section with two bullet points: 'Official source code repo: https://github.com/Gilles86/braincoder/tree/main' and 'HTML documentation (stable release): https://braincoder-devs.github.io/'.

Gilles de Hollander

braincoder

- Developed at **University of Amsterdam, Spinoza Centre for Neuroimaging** and **UZH**
- **Maintainer**
 - Gilles de Hollander
- **Contributors**
 - Tomas Knapen (UvA/Spinoza Centre for Neuroimaging)
 - Marco Aqil (UvA/Spinoza Centre for Neuroimaging)
 - Maïke Renkert (UZH)
- Upcoming paper
- Extensive documentation: braincoder-devs.github.io

braincoder

Key features:

- Massive computational optimisation thanks to Tensorflow and GPUs
- Ease-of-use
- All standard models implemented
- **Inversion of encoding models**

1. Encoding Models: Mapping Stimulus → BOLD

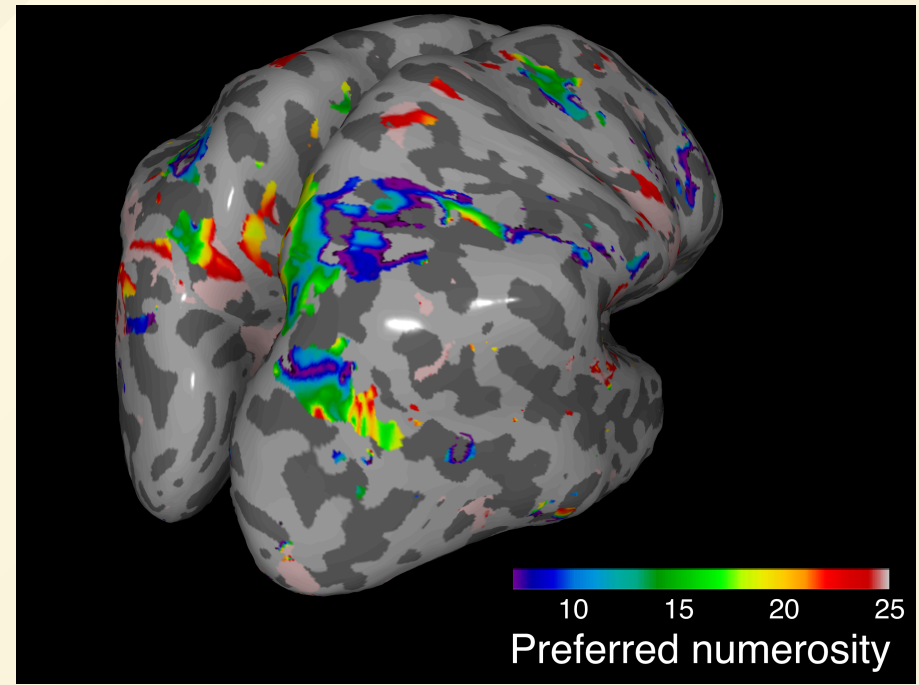
Deterministic mapping:

$$f(s; \theta) : s \mapsto y$$

- s : Stimulus (e.g., orientation, numerosity, 2D image)
- y : BOLD response (single voxel y or pattern Y)
- θ : Parameters (e.g., PRF center/dispersion, amplitude, baseline)

Example: 1D Gaussian PRF

$$f(s; \mu, \sigma, a, b) = a \cdot \mathcal{N}(s; \mu, \sigma) + b$$



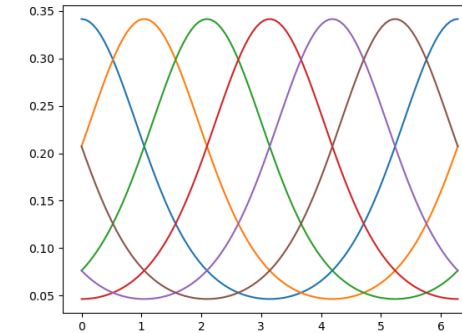
2. Linear Encoding Models

- "Jehee approach"
- Fixed neural populations (fixed θ) + linear weights:

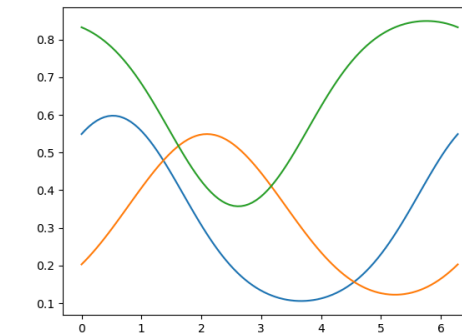
$$x_j = \sum_i W_{i,j} \cdot f_j(\theta_j)$$

- **Advantage:** Fit weights (W) with **linear regression** (fast! Can be done with standard fMRI analyses packages.).
- **Disadvantages:**
 - Parameters are not interpretable
 - Model misspecification?
- **Example:** Von Mises tuning curves for orientation.

Basis Functions



Voxel Predictions



3. Building the Likelihood

- **Add Gaussian noise** to deterministic models:

$$p(x|s; \theta) = f(s; \theta) + \epsilon, \quad \epsilon \sim \mathcal{N}(0, \Sigma)$$

- **Covariance matrix (Σ):**
 - Regularized estimate (shrinkage + neural population overlap).
 - Accounts for voxel-to-voxel noise correlations.

Key:

- Enables **Bayesian inversion** (stimulus decoding).

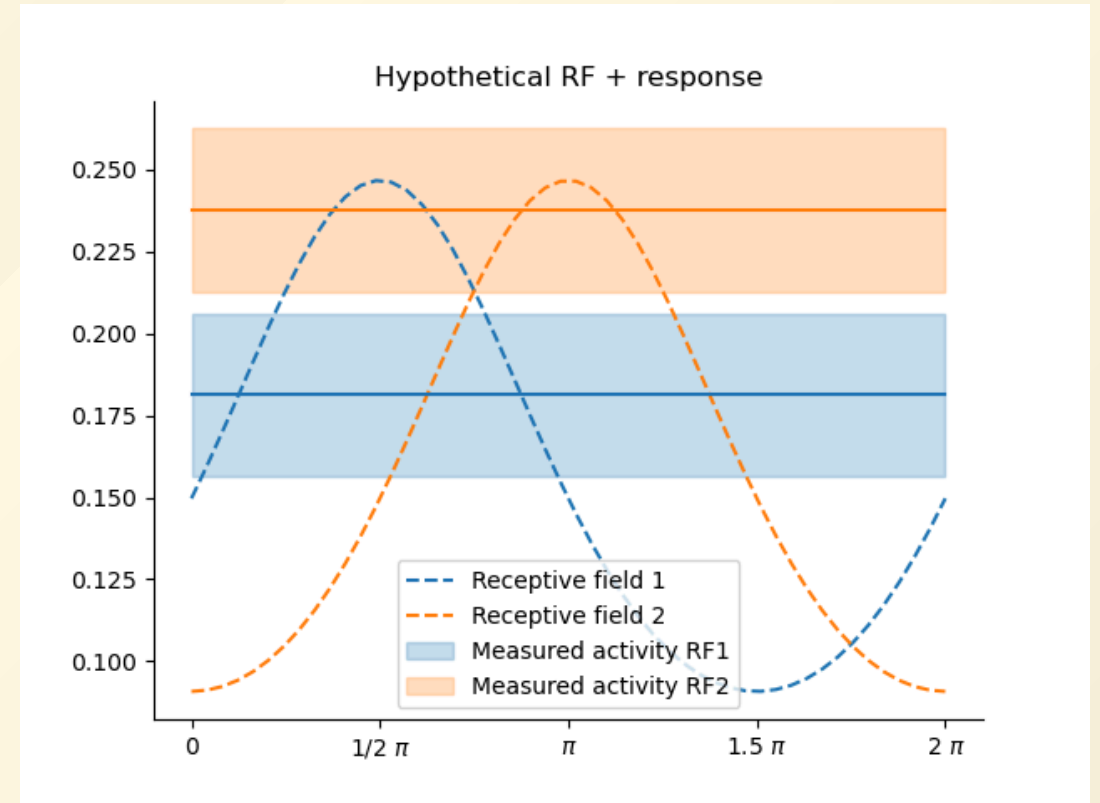
4. From Neural Responses → Stimulus Features

Bayes' Rule:

$$p(s|x, \theta) = \frac{p(x|s, \theta)p(s)}{p(x)}$$

Approach:

- Keep θ and s fixed, and evaluate/estimate/sample over s .



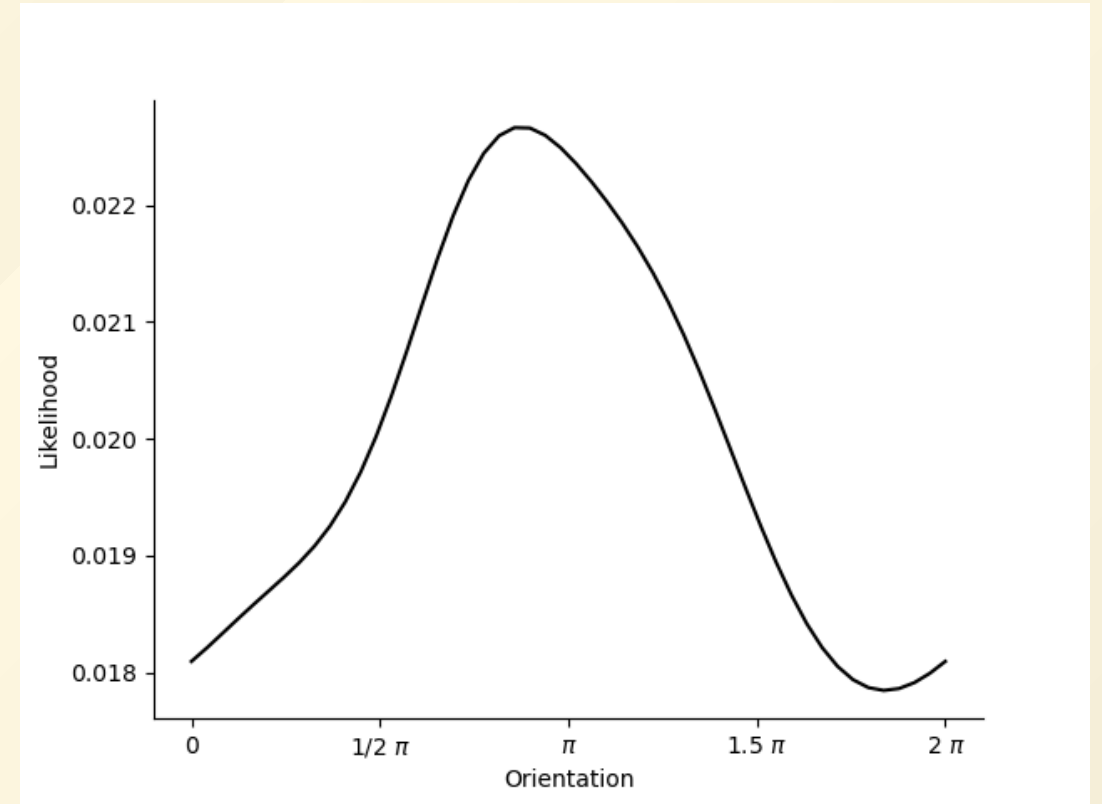
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Approach:

- Keep θ and s fixed, and evaluate/estimate/sample over s .



5. Decoding Noisy Neural Data

Steps:

1. Fit encoding model (θ) (grid + gradient descent).
2. Estimate noise covariance (Σ).
3. Compute **posterior** ($p(s|x; \theta)$).
4. Extract **mean posterior** or **MAP estimate**.
5. (Extract **uncertainty** surrounding posterior)

Key Takeaways

- **Encoding:** Map stimuli to BOLD (linear/non-linear models).
- **Decoding:** Invert models using Bayesian inference + noise modeling.
- **Tools:**
 - `braincoder` can do all of this and leverages **TensorFlow** for fast, GPU-accelerated fitting.

Your Turn:

- Try fitting a PRF model to your own data!

Example code for PRF fit

```
from braincoder.models import GaussianPRF2DWithHRF
from braincoder.hrf import SPMHRFModel
from braincoder.optimize import ParameterFitter

# Set up model, including HRF
hrf_model = SPMHRFModel(tr=1.7)
model = GaussianPRF2DWithHRF(grid_coordinates=grid_coordinates, hrf_model=hrf_model)

# Set up fitter
fitter = ParameterFitter(data=v1_ts, model=model, paradigm=stimulus)

# Define grid search parameters
mu_x = np.linspace(-3, 3, 20, dtype=np.float32)
mu_y = np.linspace(-3, 3, 20, dtype=np.float32)
sigma = np.linspace(0.1, 5, 20, dtype=np.float32)
baselines = [0.0]
amplitudes = [1.0]

# Do grid search using correlation cost (so baseline and amplitude do not matter)
grid_pars = fitter.fit_grid(mu_x, mu_y, sigma, baselines, amplitudes, use_correlation_cost=True)

# Refine baseline and amplitude using OLS
grid_pars = fitter.refine_baseline_and_amplitude(grid_pars)
gd_pars = fitter.fit(init_pars=grid_pars)
```

Assignment 4: Decoding visual stimuli

Open `notebooks/4_decode.ipynb`.