

表演是
$$\overline{T} = \varphi^2(u',u^2) T$$
. $\Rightarrow \sigma \cdot \overline{Z} + \overline{Z} = \alpha T_*(\chi_1) + b T_*(\chi_2)$.

Zim $\overline{Z} = \varphi^2(u',u^2) T$. $\Rightarrow \sigma \cdot \overline{Z} + \overline{Z} = \alpha T_*(\chi_1) + b T_*(\chi_2)$.

下面什么保育 唯

$$\vec{a} = a^{\alpha} \chi_{\alpha}$$

$$\vec{b} = b^{\alpha} \chi_{\beta}$$

$$\vec{\sigma}^{*}(\vec{b}) = b^{\alpha} \vec{\sigma}^{*}(\chi_{\alpha}) = a^{\alpha} \bar{\chi}_{\alpha}$$

$$\vec{\sigma}^{*}(\vec{b}) = b^{\alpha} \vec{\sigma}^{*}(\chi_{\beta}) = b^{\alpha} \bar{\chi}_{\beta}$$

$$\cos \angle \left(\sigma^{*}(\alpha), \sigma^{*}(\beta)\right) = \frac{\left(\sigma^{*}(\alpha), \sigma^{*}(\beta)\right)}{\|\sigma^{*}(\alpha)\| \|\sigma^{*}(\beta)\|}$$

$$= \frac{\alpha^{\alpha} b^{\beta} \bar{x}_{\alpha} \bar{x}_{\beta}}{(\alpha^{\alpha} a^{\gamma} \bar{x}_{\beta} \bar{x}_{\gamma})^{\frac{1}{2}} (b^{\beta} b^{\beta} \bar{x}_{\beta} \bar{x}_{\beta})^{\frac{1}{2}}}$$

$$= \frac{\alpha^{\alpha} b^{\beta} \bar{y}_{\alpha\beta}}{(\alpha^{\alpha} a^{\gamma} \bar{x}_{\beta} \bar{x}_{\gamma})^{\frac{1}{2}} (b^{\beta} b^{\beta} \bar{x}_{\beta} \bar{x}_{\beta})^{\frac{1}{2}}}$$

$$= \frac{\alpha^{\alpha} b^{\beta} \bar{y}_{\alpha\beta}}{(a^{\gamma} a^{\gamma} \bar{x}_{\beta})^{\frac{1}{2}} (b^{\beta} b^{\beta} \bar{x}_{\beta} \bar{x}_{\beta})^{\frac{1}{2}}}$$

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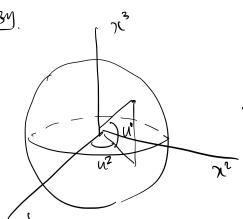
してかる事で中南な不多り

Thm. 任何曲面. 以在局部与平面共形对定即. 任何曲面的第一基本形式. 都可以写成

S.-S. Chern
$$\mathbb{R}^{\frac{1}{2}}$$
, $\mathbb{R}^{\frac{1}{2}}$ $\mathbb{R}^{\frac{$

$$=) |\lambda|^2 ds^2 = du^2 + dv^2$$





$$[x]^2 = r^2$$
. The, $\sum_{i=1}^{3} (x^i)^2 = r^2$

$$\frac{1}{2} \int_{0}^{1/2} |x|^{2} = |x| \cos u^{2} \cos u^{2}$$

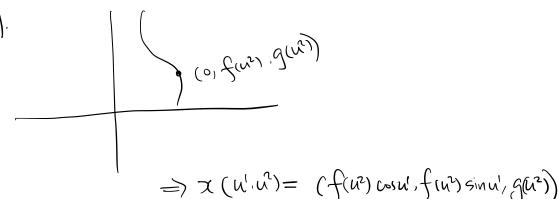
$$\frac{1}{2} \int_{0}^{1/2} |x|^{2} = |x| \cos u^{2} \cos u^{2}$$

$$\frac{1}{2} \int_{0}^{1/2} |x|^{2} dx$$

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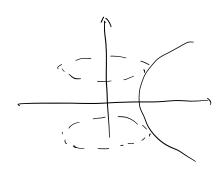
$$(\chi^3 = r \sin u')$$

我提影
$$\chi' = \frac{2r^2a'}{r^2 + (a')^2 + (a')^2}$$
 $\chi'^2 = \frac{2r^2a^2}{r^2 + (a')^2 + (a')^2 + (a')^2}$ $\chi'^3 = r \frac{(a')^2 + (a')^2 - r^2}{(a')^2 + (a')^2 + (a')^2}$



$$\chi_{i} = \left(-\frac{1}{2}\sin x^{i}, \frac{1}{2}\cos x^{i}, \frac{1}{2}\right)$$

$$= \int_{0}^{2} (du')^{2} + [(5')^{2} + (5')^{2}] (du')^{2}$$



$$\begin{cases}
f(t) = f(w) = a ch \frac{t}{a} \\
g(x) = g(w) = w^{2}
\end{cases}$$

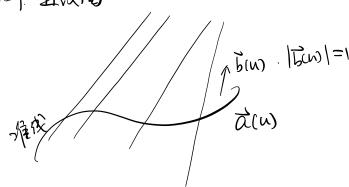
$$\Rightarrow \begin{cases} \int = sh \frac{h^2}{a} \\ g' = 1 \end{cases} \Rightarrow T' = ch^2 \frac{h^2}{a} \left[a(du)^2 + (au^2)^2 \right]$$

唱旋面
$$\chi(\overline{u}',\overline{u}') = (f(\overline{u}^2)\cos\overline{u}', f(\overline{u}^2)\sin\overline{u}', g(\overline{u}^2) + a\overline{u}')$$

$$\frac{1}{2} \int (\overline{u}^2) = \overline{u}^2 \qquad \Longrightarrow \quad \overline{L}_1 = \left(a^2 + (\overline{u}^2)^2\right) \left(d\overline{u}^2\right)^2 + \left(d\overline{u}^2\right)^2 \\
= \int (\overline{u}^2) = 0 \qquad \Longrightarrow \quad \overline{L}_1 = \left(a^2 + (\overline{u}^2)^2\right) \left(d\overline{u}^2\right)^2 + \left(d\overline{u}^2\right)^2 \\
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考定 Ti=u'、Ti=a sh 2 =) 丁=丁,故正版的与思维的 放等版对应,

何 直该面



$$\gamma((u,v) = a(u) + vb(u)$$

$$\Rightarrow bb = 0$$

$$X_{u} = X_{1} = a' + vb'$$

$$X_{v} = X_{2} = b$$

$$J_{u} = \left(a' + vb'\right)$$

$$J_{12} = a'b$$

$$\Rightarrow I = |a'+vb'|^2 (du)^2 + 2a'b dudv + (du)^2$$

In particular 1° bus) is constant => 1/2 %.

2° alu) is constant =) 维初

3° 克/克/ 一切线面.



4° define. 可展曲面. 的着任意一条直再线每一定处的

Thm. 直线面)((n,v)= a(n)+vb(m)(161=1是可居田面()(a1,b,b)=0

图. 任历直升线 (V-线) U=4°

 $\mathcal{P}(\mathcal{W},\mathcal{O})$. $\mathcal{Q}(\mathcal{U},\mathcal{O}+\Delta V)$ $\Delta V \neq 0$

P.Q.两点处的 15何量

 $(a'+Vb')\times b$ $(a'+(V+\Delta V)b')\times b$

to. 可屬会 $0 = [(a'+vb')\times b] \times [(a'+(v+av))b') \times b]$ $\wedge = \Delta V^2 (a' \times b) (b' \times b)$ = - av2 (a1, b, b) b.