

$$L = \int_{a}^{b} ds = \int_{a}^{b} |dx| = \int_{a}^{b} \sqrt{x_{\alpha} dn^{\alpha}} (x_{\beta} dn^{\beta})$$

$$= \int_{a}^{b} \sqrt{g_{\alpha} \beta_{\alpha} \frac{du^{\alpha}}{aut}} du^{\beta} dt$$

$$\frac{\partial x}{\partial t} = \frac{\partial x}{\partial u'} \frac{\partial u'}{\partial t} + \frac{\partial x}{\partial u'} \frac{\partial u'}{\partial t}$$

$$= \chi_1 \frac{\partial u'}{\partial t} + \chi_2 \frac{\partial u'}{\partial t}$$

$$= \alpha' \chi_1 + \alpha' \chi_2$$

$$\overrightarrow{a} = a'x_1 + a^2x_2 = a'x_4$$

$$\overrightarrow{b} = b'x_1 + b'x_2 = b''x_4$$

$$\cos\theta = \frac{\vec{\alpha} \cdot \vec{b}}{|\vec{\alpha}||\vec{b}|} = \frac{(\vec{\alpha}^{\alpha} \lambda \vec{a}) (\vec{b}^{\alpha} \lambda \vec{p})}{|\vec{\alpha}^{\alpha} \lambda \vec{a}||\vec{b}^{\alpha} \lambda \vec{p}|} = \frac{\vec{g}_{\alpha\beta} \vec{a}^{\alpha} \vec{b}^{\beta}}{\sqrt{\vec{g}_{\beta} \vec{a}^{\alpha} \vec{a}^{\beta}} \sqrt{\vec{g}_{\gamma\beta} \vec{a}^{\gamma} \vec{a}^{\beta}}}$$

$$\cos(21...20) = \frac{g_{12}}{Jg_{11}} \qquad \text{If } 3. \quad \cos(0) = 0 \iff g_{12} = 0$$

$$\Rightarrow \text{If } 3\frac{1}{2} \text{ for } 3$$

$$= g_{11}(du_1)^2 + g_{12}(du_2)^2$$

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$$\begin{array}{ll}
1' & \text{Pr} \\
\lambda_1 = (1, 0, 0) \\
\lambda_2 = (0, 1, 0)
\end{array}$$

$$\frac{1}{2} = (0, 1, 0) \\
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\frac{1}$$

本曲面 N=X(u', u2)的考数网的产品线的线的名差,

解 减速和的电视为 C.

$$\overrightarrow{r}(s) = \lambda((u'(s), u^2(s))$$

S 流味考数. $T(s) = \frac{dr}{ds} = \chi_1 \frac{du'}{ds} + \chi_2 \frac{du'}{ds}$ T 5 χ_1 , χ_2 或 5 χ_2 , $-\chi_2$ 紛美角相等.

$$\xi \frac{T \cdot \chi_1}{|\chi_1|} = \frac{T \cdot \chi_2}{|\chi_2|} \qquad \xi = \pm 1$$

$$\frac{2}{\sqrt{g_{11}}} \left(g_{11} \frac{du^{1}}{ds} + g_{12} \frac{du^{2}}{ds} \right) = \frac{1}{\sqrt{g_{12}}} \left(g_{12} \frac{du^{1}}{ds} + g_{21} \frac{du^{2}}{ds} \right)$$

$$\left(\overline{19_{11}} - \frac{9_{12}}{59_{22}}\right) \frac{clu'}{cls} = \left(\overline{19_{22}} - \frac{29_{12}}{59_{11}}\right) \frac{clu'}{cls}$$

$$2\overline{1911}\left(1-\frac{2\overline{912}}{\overline{911}\overline{911}}\right)\frac{du^{1}}{ds} = \overline{1911}\left(1-\frac{2\overline{912}}{\overline{911}\overline{911}}\right)\frac{du^{2}}{ds}$$

$$-\frac{12}{2}70.\left(\frac{7}{2}\right)$$

$$\Rightarrow \xi \widetilde{g_{11}} \frac{ch'}{d\xi} = \overline{g_{22}} \frac{dh'}{d\xi}$$

Ex. 沒曲面上含 du', du2 的=次3% P(du) 3+2Q du/du2+R(du) 3=0.

⇒确定了两个方向、当征运动方向正支⇔ ER-2FQ+GP=0

$$|\chi_1 \times \chi_2|^2 = (\chi_1 \times \chi_1)(\chi_1 \times \chi_1) = (\chi_1 \times \chi_1)(\chi_2 \cdot \chi_1) - (\chi_1 \cdot \chi_1)^2$$

$$= \Im g_{12} - \Im g_{12}$$

$$= \det(g_{dp})$$

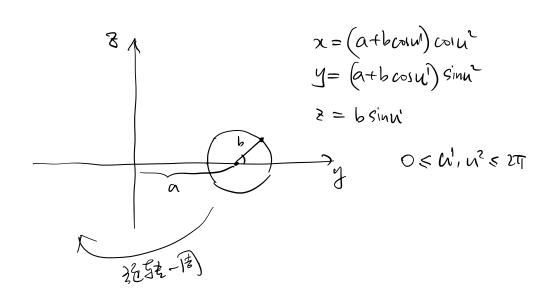
$$M \approx 2$$
 $A(M) = \int dA = \int darg_{ap} du' du^2$

而殺与考数元美?

$$\overline{\chi}:\overline{D}\longrightarrow \overline{\chi}(\overline{D})=M\in\mathbb{R}^3$$

$$\frac{\partial (u_1, v_2)}{\partial (u_1, v_2)} \neq 0$$

$$\begin{aligned}
& \left\{ \begin{array}{l} \left(\overline{\chi}_{1} \times \overline{\chi}_{2} \right) d\overline{u} d\overline{u} \\
\overline{\chi}_{1} = \overline{\chi}_{1} \frac{\partial u^{1}}{\partial \overline{u}_{1}} + \overline{\chi}_{1} \frac{\partial u^{2}}{\partial \overline{u}_{2}} \\
\overline{\chi}_{2} = \overline{\chi}_{2} \frac{\partial u^{1}}{\partial \overline{u}_{2}} + \overline{\chi}_{2} \frac{\partial u^{2}}{\partial \overline{u}_{2}} \\
& \left[\overline{\chi}_{1} \times \overline{\chi}_{2} \right] = \left[\chi_{1} \times \chi_{2} \right] \frac{\partial (u^{1}, u^{2})}{\partial (\overline{u}_{1}, \overline{u}_{2})} \end{aligned}$$



$$\chi_{1} = \left(-b\sin n'\cos n^{2}, -b\sin n'\sin n^{2}, b\cos n^{2}, b\cos n^{2}\right)$$

$$\chi_{2} = \left(-(a+b\cos n')\sin n^{2}, (a+b\cos n')\cos n^{2}, o\right)$$

$$g_{11} = b^{2} \quad g_{12} = 0 \quad g_{22} = (a+b\cos n')^{2}.$$

$$det \quad g_{13} = b^{2} \quad (a+b\cos n')^{2}$$

内蕴的几何是(第一基本形式所次定位)

$$M_1$$
 $\gamma c = \chi^1(\omega^1, \omega^2)$

老两面的参数之间存在有1-1对名。

$$M_{2}$$
 $\chi = \tilde{\chi} (\tilde{u}', \tilde{u}')$

 $(u',u') \longrightarrow (\overline{u}',\overline{u}')$

$$\overline{\mathcal{W}} = \overline{\mathcal{W}}(\mathcal{W}, \mathcal{W})$$

$$\overline{\mathcal{U}}^2 = \overline{\mathcal{W}}^1 \left(\mathcal{U}_1, \mathcal{U}^2 \right)$$

游音 o: M, -> M2, 1-1 対を

一定们第一基本形式工工

满足 $\overline{T} = \varphi^2(u',u^2)$ 工. $\varphi \neq 0$

M新Mi. Mi 到的的对应是安积的(Conformal得南)

I = gas du due

I = gas du dus

Jag du du = y'(n'. n') Jag du dus

 $\text{HF} \quad du^{\alpha} \neq dt^{\alpha} \quad \text{th} \quad \widehat{g}_{\alpha\bar{e}} \neq y^2 g_{\alpha\bar{e}}$

12. 57 x3 9 at did at 12 12 th 9 at due due

= 929 at 1

$$\overline{g}_{\overline{\alpha}\overline{\beta}} = \overline{\chi}_{\overline{n}} \overline{\chi}_{\overline{n}\xi}$$

$$= (\overline{\chi}_{y} \frac{\partial u^{y}}{\partial \overline{n}^{y}}) (\overline{\chi}_{\sigma} \frac{\partial u^{\sigma}}{\partial \overline{n}^{\xi}})$$

$$= \overline{g}_{y\sigma} \frac{\partial u^{y}}{\partial \overline{n}^{\alpha}} \frac{\partial u^{\sigma}}{\partial \overline{n}^{\xi}}$$

