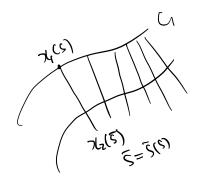
曲设记基本宣禮. K(s) 可粉. T(s) 连续

$$\chi=\chi(S)$$
  
 $\dot{\chi}(S)=T(S)$   
 $\dot{\chi}(S)=T(S)$   
 $\dot{\tau}(S)=\kappa(S)N(S)$   
 $\dot{\eta}(S)=-\kappa(S)T(S)+\tau(S)B(S)$   
 $\dot{\eta}(S)=-\kappa(S)T(S)$   
 $\dot{\eta}(S)=-\kappa(S)T(S)$   
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 $\dot{\eta}(S)=-\kappa(S)T(S)$ 

Bertrand. 曲线



双(5)与双(5)处相图 N (殆线)证对各点间距离相图 对2定协何呈定角 对这点切何呈复角

 $\chi_{2}(\zeta(s)) = \chi_{1}(s) + \chi_{1}(s) \chi_{1}(s)$ 

 $T_2(\bar{\varsigma})\frac{d\bar{\varsigma}}{ds} = T_1(\varsigma) + \dot{\gamma}N_1 + \gamma(-k_1(\varsigma)T_1(\varsigma) + T_1(r)B_1(\varsigma))$ 对5亩量

点来からうの=0+分+の一分からの一分のか多数

$$\frac{d}{ds}\left(T_{1}(s)\cdot T_{2}(\overline{s}(s))\right) = kc)N_{1}(s)\cdot T_{2}(\overline{s}(s)) + T_{1}(s)\cdot N_{2}(\overline{s})\frac{d\overline{s}}{ds} = 0$$

$$= )T_{1}(s)\cdot T_{2}(\overline{s}(s)) = \cos \delta$$

## 曲面记

D.CE D为连通区域 全标为 ul, u2

X: D→E³ 同配

 $\chi(u,v) = (\chi'(u',u^2), \chi'^2(u',u^2), \chi^3(u',u^2))$ 

Ch 由面 M. (422): 满足.① xì(u',u²) 具有作阶连续偏等.

② Jocobi 矩阵.
$$\frac{\partial x^{1}}{\partial u^{2}} \frac{\partial x^{2}}{\partial u^{2}} \frac{\partial x^{3}}{\partial u^{4}}$$

$$\frac{\partial x^{1}}{\partial u^{2}} \frac{\partial x^{2}}{\partial u^{2}} \frac{\partial x^{3}}{\partial u^{2}}$$

$$\frac{\partial x^{1}}{\partial u^{2}} \frac{\partial x^{2}}{\partial u^{2}} \frac{\partial x^{3}}{\partial u^{2}}$$

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$$\frac{\partial x^{1}}{\partial u^{2}} \frac{\partial x^{2}}{\partial u^{2}} \frac{\partial x^{3}}{\partial u^{2}}$$

$$\frac{\partial x^{3}}{\partial u^{2}} \frac{\partial x^{3}}{\partial u^{2}}$$

面 对与双线性观差

 $\chi_{1}(u_{o}^{1},u_{o}^{2})$   $\chi(u_{o}^{1},u_{o}^{2})$   $\chi(u_{o}^{1},u_{o}^{2})$  人  $\chi(u_{o}^{1},u_{o}^{2})$ \x(u', u^2)-u' &

单维信何量、
$$\eta(u',u^2) = \frac{\chi_1 \times \chi_2}{|\chi_1 \times \chi_1|} (u',u^2) \rightarrow 构成何量物(影情)$$

参数表示不够一

参数数换. Ux = Ux(u1, u1)

$$\chi = \chi(u', u^{2}) = \bar{\chi}(\bar{u}', \bar{u}^{2}) = \bar{\chi}(\bar{u}'(u', u^{2}), \bar{u}^{2}(u', u^{2}))$$

$$(\chi_{1}, \chi_{1}) \qquad (\bar{\chi}_{1}, \bar{\chi}_{1}^{2})$$

$$(\frac{\partial \chi}{\partial u'}, \frac{\partial \chi}{\partial u'}) \stackrel{=}{=} \frac{\partial \bar{\chi}}{\partial \bar{u}'}, \frac{\partial \bar{u}'}{\partial \bar{u}'}$$

$$(\frac{\partial \chi}{\partial u'}, \frac{\partial \chi}{\partial u'}) \stackrel{=}{=} \frac{\partial \bar{\chi}}{\partial \bar{u}'}, \frac{\partial \bar{u}'}{\partial \bar{u}'}$$

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$$(\frac{\partial \chi}{\partial u'}, \frac{\partial \chi}{\partial u'}) \stackrel{=}{=} \frac{\partial \chi}{\partial u'}$$

$$(\frac{\partial \chi}{\partial u'}, \frac{\partial \chi}{\partial u'}) \stackrel{$$

動面 M上的-条曲线 C.

$$M \supset (I) \times (I) \subset M$$

$$t \longrightarrow (u'(t), u^2(t)) \xrightarrow{\chi} \chi(u'(t), u^2(t))$$

$$\frac{C \text{ (b) 3/h} + .}{S(x) = \int_{0}^{t} \left| \frac{dx}{dt} \right| dt}$$

$$\Rightarrow \frac{ds}{dt} = \left| \frac{dx}{dt} \right|$$

$$T = ds^{2} = |dx|^{2} = |x_{1}du + x_{1}zdu^{2}|^{2} = |x_{1}x_{1}|du^{2} + 2x_{1}x_{2}|du^{2}du^{2} + x_{1}x_{1}|du^{2}$$

$$\Rightarrow |x_{0}x_{0}| = |y_{0}x_{0}|^{2} = |y_{1}|du^{2} + 2y_{1}|du^{2} + |y_{1}|^{2}du^{2}$$

$$\Rightarrow |y_{0}x_{0}| = |y_{0}x_{0}|^{2} + |y_{0}x_{0}|^{2} + |y_{0}x_{0}|^{2}$$

$$\Rightarrow |y_{0}x_{0}| = |y_{0}x_{0}|^{2} + |y_{0}x_{0}|^{2}$$

$$g_{11} = E$$
.  $g_{12} = F$   $g_{21} = G$ 

村面.

$$P(x', x'', x'')$$

$$-\frac{\pi}{2} \leq u' \leq \frac{\pi}{2}$$

$$x' \qquad 0 \leq u' \leq 2\pi$$

$$x'' = r \cos u' \cos u'$$

$$x'' = r \cos u' \cos u'$$

$$x'' = r \cos u' \sin u'$$

$$\mathcal{H}_{1} = \left(-r \sin u' \cos u'^{2}, -r \sin u' \sin u^{2}, r \cos u'\right)$$

$$\mathcal{H}_{2} = \left(-r \cos u' \sin u^{2}, r \cos u' \cos u'^{2}, 0\right)$$

$$I = r^{2}(du')^{2} + r^{2}\cos^{2}u'(du^{2})^{2} = I((du',du'),(du',du'))$$

$$X' = \frac{2r^{2}\bar{u}_{1}}{r^{2} + (\bar{u}')^{2} + (\bar{u}')^{2}}$$

$$X' = \frac{2r^{2}\bar{u}_{1}}{r^{2} + (\bar{u}')^{2} + (\bar{u}')^{2}}$$

$$X' = \frac{r((\bar{u})^{2} + (\bar{u}')^{2} - r^{2})}{r^{2} + (\bar{u}')^{2} + (\bar{u}')^{2} + (\bar{u}')^{2}}$$

## 第一基本形式 在考数复换下变化?

$$\overline{\chi}(\overline{u}',\overline{u}^2) = \overline{\chi}(\overline{u}'(u',u^2),\overline{u}^2(u',u^2)) = \chi(u'(\overline{u}',\overline{u}^2),u'(\overline{u}',\overline{u}^2))$$

$$\overline{u}^2 = \overline{u}^2(u',u^2)$$

$$I = g_{\alpha\beta} d\alpha d\alpha = \frac{3}{3} \frac{1}{3} \frac$$

$$\frac{\partial x}{\partial x} = \frac{\partial x}{\partial x} =$$

$$\Rightarrow \widehat{g}_{\alpha \beta} \, \overline{du}^{\alpha} \, \overline{du}^{\beta} = g_{\beta S} \, \frac{\partial u^{\beta}}{\partial \overline{u}^{\alpha}} \, \frac{\partial u^{S}}{\partial \overline{u}^{S}} \, \overline{du}^{S} \, \overline{du}^{S}$$

$$= g_{\delta S} \, du^{\delta} \, du^{S}$$

$$\begin{pmatrix} g_{11} & g_{12} \\ g_{12} & g_{21} \end{pmatrix} = \begin{pmatrix} E & F \\ F & G \end{pmatrix} \quad \text{If } \vec{g}.$$

$$\det \begin{pmatrix} \exists F \\ F \end{pmatrix} = (\chi_{i} \times \chi_{i})(\chi_{1} \cdot \chi_{1}) - (\chi_{i} \cdot \chi_{1})(\chi_{i} \cdot \chi_{2}) = |\chi_{1} \times \chi_{2}|^{2} > 0$$

活动杨梨.

Schmidt IZW
$$\begin{cases}
e_1 = \frac{\chi_1}{|\chi_1|} = \frac{\chi_1}{|g_{11}|} & \chi_1 = \sqrt{g_{11}} e_1 \\
e_2 = \frac{\chi_2 - (\chi_2 \cdot e_1) e_1}{|\chi_2 - (\chi_1 \cdot e_1) e_1|} & \chi_2 = \frac{g_{12}}{|g_{11}|} e_1 + \frac{1}{\sqrt{g_{11}}} \sqrt{g_1 g_{11} - g_1^2} e_2
\end{cases}$$

实际随意已发标学: 
$$\chi_1 = a_1^1 e_1 + a_1^2 e_2$$
  $\chi_2 = a_2^1 e_1 + a_2^2 e_2$ 

70,027 名正

$$dx = \chi_{\alpha} dn^{\alpha} = \left(\alpha_{\alpha}^{\beta} e_{\beta} dn^{\alpha}\right)$$

$$= \frac{\alpha_{\alpha}^{\beta} dn^{\alpha}}{\parallel} e_{\beta} = \omega^{\beta} e_{\beta}.$$

$$\frac{11}{\omega^{\beta}}$$