

HEAP-MAXIMUM(A)

```
1  return  $A[1]$ 
```

The procedure HEAP-EXTRACT-MAX implements the EXTRACT-MAX operation. It is similar to the **for** loop body (lines 3–5) of the HEAPSORT procedure.

HEAP-EXTRACT-MAX(A)

```
1  if  $A.heap-size < 1$ 
2      error “heap underflow”
3   $max = A[1]$ 
4   $A[1] = A[A.heap-size]$ 
5   $A.heap-size = A.heap-size - 1$ 
6  MAX-HEAPIFY( $A, 1$ )
7  return  $max$ 
```

MAX-HEAPIFY(A, i)

```
1   $l = \text{LEFT}(i)$ 
2   $r = \text{RIGHT}(i)$ 
3  if  $l \leq A.heap-size$  and  $A[l] > A[i]$ 
4       $largest = l$ 
5  else  $largest = i$ 
6  if  $r \leq A.heap-size$  and  $A[r] > A[largest]$ 
7       $largest = r$ 
8  if  $largest \neq i$ 
9      exchange  $A[i]$  with  $A[largest]$ 
10  MAX-HEAPIFY( $A, largest$ )
```

PARENT(i)

```
1  return  $\lfloor i/2 \rfloor$ 
```

LEFT(i)

```
1  return  $2i$ 
```

RIGHT(i)

```
1  return  $2i + 1$ 
```

MAX-HEAP-INSERT(A, key)

```
1   $A.heap-size = A.heap-size + 1$ 
2   $A[A.heap-size] = -\infty$ 
3  HEAP-INCREASE-KEY( $A, A.heap-size, key$ )
```

HEAP-INCREASE-KEY(A, i, key)

```
1  if  $key < A[i]$ 
2      error “new key is smaller than current key”
3   $A[i] = key$ 
4  while  $i > 1$  and  $A[\text{PARENT}(i)] < A[i]$ 
5      exchange  $A[i]$  with  $A[\text{PARENT}(i)]$ 
6   $i = \text{PARENT}(i)$ 
```