

HW1

Haojie Liu

2023-10-05

Problem 1: Suppose X is a geometric random variable with $p = 0.3$, determine the value of k such that $P(X \leq k) \simeq 0.8$

$$X \sim \text{Geometric}(0.3)$$

$$P(X \leq k) = 1 - (1 - p)^k \simeq 0.8$$

$$1 - 0.7^k \simeq 0.8$$

$$0.7^k \simeq 0.2$$

$$k = \frac{\log(0.2)}{\log(0.7)}$$

```
print(paste("k =", log(0.2)/log(0.7)))
```

```
## [1] "k = 4.51233802593815"
```

Problem 2: If two random variables, X and Y , are independent, show $\text{Var}(XY)$ in terms of the expected values and variances of X and Y .