

```
%Studio 00
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%ENME462
%Section 0105
```

Problem 1. Use MATLAB to represent and generate the transfer function

```
% Using Control System Toolbox
'Rational Expression Method, Polynomial Form' %Display Label
s = tf('s'); % Define 's' as an LTI object in polynomial form
G = 5*(s+15)*(s+26)*(s+72)/(s*(s+55)*(s^2+5*s+30)*(s+56)*(s^2+27*s+52))
```

ans =

'Rational Expression Method, Polynomial Form'

G =

$$5 s^3 + 565 s^2 + 16710 s + 140400$$

$$\frac{5 s^3 + 565 s^2 + 16710 s + 140400}{s^7 + 143 s^6 + 6849 s^5 + 123717 s^4 + 788690 s^3 + 3.469e06 s^2 + 4.805e06 s}$$

Continuous-time transfer function.

Problem 2. Use MATLAB to generate partial fraction expansion of the following function

```
% Using Control System Toolbox
'Rational Expression Method, Polynomial Form' %Display Label
s = tf('s'); % Define 's' as an LTI object in polynomial form
F = ((10^4)*(s+5)*(s+70))/(s*(s+45)*(s+55)*(s^2+7*s+110)*(s^2+6*s+95))

% Numerator and Denominator from F(s)
numf = (10^4)*poly([-5 -70]);
demf = conv(poly([0 -45 -55]),conv([1 7 110],[1 6 95]));
% K = residue; p = roots of denominator; k = direct quotient
% Use residue function for expansion
[K,p,k]=residue(numf,demf)

%In Partial Expansion Form
%F = -(0.0018)/(s+55) + (0.0066)/(s+45) + (0.9513+0.0896i)/(s+3.5-9.8869i) + (0.9513-0.0896i)/(s+3.5+9.8869i) + (-1.0213 - 0.1349i)/(s+3-9.2736i) + (-1.0213 + 0.1349i)/(s+3+9.2736i) + (0.1353)/(s)
```

```
disp("F = -(0.0018)/(s+55) + (0.0066)/(s+45) + (0.9513+0.0896i)/(s+3.5-9.8869i) + (0.9513-0.0896i)/(s+3.5+9.8869i) ")
```

```
ans =
```

```
'Rational Expression Method, Polynomial Form'
```

```
F =
```

```
10000 s^2 + 750000 s + 3.5e06
```

```
-----
```

```
s^7 + 113 s^6 + 4022 s^5 + 58200 s^4 + 754275 s^3 + 4.324e06 s^2
```

```
+ 2.586e07 s
```

```
Continuous-time transfer function.
```

```
K =
```

```
-0.0018 + 0.0000i
```

```
0.0066 + 0.0000i
```

```
0.9513 + 0.0896i
```

```
0.9513 - 0.0896i
```

```
-1.0213 - 0.1349i
```

```
-1.0213 + 0.1349i
```

```
0.1353 + 0.0000i
```

```
p =
```

```
-55.0000 + 0.0000i
```

```
-45.0000 + 0.0000i
```

```
-3.5000 + 9.8869i
```

```
-3.5000 - 9.8869i
```

```
-3.0000 + 9.2736i
```

```
-3.0000 - 9.2736i
```

```
0.0000 + 0.0000i
```

```
k =
```

```
[]
```

```
F = -(0.0018)/(s+55) + (0.0066)/(s+45) + (0.9513+0.0896i)/(s+3.5-9.8869i) + (0.9513-0.0896i)/(s+3.5+9.8869i)
```

Problem 3. Use MATLAB and the SYMBOLIC MATH TOOLBOX to find the Laplace Transform of the following functions (1) $f(t)=8t^2\cos(3t+45^\circ)$ (2) $f(t)=3te^{-2t}\sin(4t+60^\circ)$

```
% (1)
syms t % Construct symbolic object for frequency variable 't'
f = 8*t^2*cosd(3*t+45)
F = laplace(f) % Find Laplace transform
%pretty(F) %Pretty Print Laplace
```

f =

$$8t^2 \cos((\pi(3t + 45))/180)$$

F =

$$4 \cdot 2^{1/2} \cdot (\pi / (30 \cdot (\pi^2/3600 + s^2)^2) - (2s^2 \pi) / (15 \cdot (\pi^2/3600 + s^2)^3)) - 4 \cdot 2^{1/2} \cdot ((6s) / (\pi^2/3600 + s^2)^2 - (8s^3) / (\pi^2/3600 + s^2)^3)$$

```
% (2)
syms t % Construct symbolic object for frequency variable 't'
f = 3*t*exp(-2*t)*cosd(3*t+45)
F = laplace(f) % Find Laplace transform
%pretty(F) %Pretty Print Laplace
```

f =

$$3t \cos((\pi(3t + 45))/180) \exp(-2t)$$

F =

$$- (3 \cdot 2^{1/2} \cdot (1 / ((s + 2)^2 + \pi^2/3600) - ((2s + 4) \cdot (s + 2)) / ((s + 2)^2 + \pi^2/3600)^2)) / 2 - (2^{1/2} \cdot \pi \cdot (2s + 4)) / (40 \cdot ((s + 2)^2 + \pi^2/3600)^2)$$

Problem 4. Using MATLAB find and plot the angular velocity response to a unit step input

```
syms s % Construct symbolic object for frequency variable 's'
f = (20.83)/((s+100)*(s+1.71))
F = ilaplace(f) % Find Laplace transform
%With step input
w = (20.83)/(s*(s+100)*(s+1.71))
W = ilaplace(w) % Find Laplace transform

%Using Sys Transfer Function And Step Input
sys = tf([20.83],poly([-100 -1.71]))
step(sys,6);
%Using Solution From Inverse Laplace Transform
figure(2);
```

```
x = [0:0.01:5];
check = (2083*exp(-100*x))/982900 - (208300*exp(-(171*x)/100))/1680759 + 2083/17100;
plot(x,check)
```

f =

$$2083/(100*(s + 100)*(s + 171/100))$$

F =

$$(2083*\exp(-(171*t)/100))/9829 - (2083*\exp(-100*t))/9829$$

w =

$$2083/(100*s*(s + 100)*(s + 171/100))$$

W =

$$(2083*\exp(-100*t))/982900 - (208300*\exp(-(171*t)/100))/1680759 + 2083/17100$$

sys =

$$\frac{20.83}{s^2 + 101.7 s + 171}$$

Continuous-time transfer function.



