Write a function that flips alternate elements of a list.

If  $a=[a_1,\ldots,a_n]$ , the result should be  $a=[a_2,a_1,a_4,,a_3\ldots,a_n]$ . If n is odd,  $a_n$  should remain at the end

# ${\sf Solution}$

Write a function that sorts a list of numbers using Quicksort

Hint: Use an auxiliary function to partition with respect to a pivot  $\boldsymbol{a}$ 

#### Mutual recursion

- ullet Function takes list L and produces list of alternate elements of L
  - o Function take that takes the first element and then calls
  - o Function skip that drops the first element and then calls take
- First attempt

```
fun skip(L) =
  if L = nil then nil
  else take(tl(L));
```

- This doesn't work
- We should use the keyword and

#### Mutual recursion

```
fun take(L) =
   if L = nil then nil
   else hd(L)::skip(tl(L))
and
skip(L) =
   if L = nil then nil
   else take(tl(L));

take[1,2,3,4];
```

Using mutual recursion, write a function to test if a number is even

# ${\sf Solution}$

```
fun even 0 = true
    | even n = odd (n-1)
and odd 0 = false
    | odd n = even (n-1);
```

Test if a list of integers alternates between 1 and 2, not ending with a 1.

# Printing

- print(x) prints a *string*
- What is the type of print?

## Printing

```
print;
val it = fn: string -> unit
print ("ab");
abval it = (): unit
print ("ab\n");
ab
val it = (): unit
fun testZero(0) = print("zero\n")
  | testZero(_) = print("not zero\n");
val testZero = fn: int -> unit
testZero(2);
not zero
val it = (): unit
```

# Printing non-strings

## Characters

```
val c = #"a";
val c = #"a": char

str;
val it = fn: char -> string

print (str(c));
aval it = (): unit
```

#### Other conversions

```
val x = 1.0E50;
val x = 1E50: real
print(Real.toString(x));
1E50val it = (): unit
print(Int.toString(123));
123val it = (): unit
print(Bool.toString(true));
trueval it = (): unit
Statements. We can write compound statements like
(print(x);
print(y); )
```

The type of a compound statement is that of the last statement

Write a function that prints a list of integers

Write a function to compute  $\binom{n}{m}$ , while printing n, m and the result.

```
fun factorial 0 = 1
  | factorial n = n * factorial(n-1);
fun comb n m =
   print ("n is ");
   print(Int.toString(n));
   print ("\n");
   print ("m is ");
   print(Int.toString(m));
   print ("\n");
   print ("Result is ");
   print (Int.toString (factorial(n) div (factorial(m) * factorial(n-m))));
   print ("\n")
);
comb 5 2;
n is 5
m is 2
Result is 10
val it = (): unit
```

Given n, print  $2^n$  X's

```
fun makelist 1 = "X"
  | makelist n = makelist (n-1) ^ makelist (n-1);
val makelist = fn: int -> string

fun printXs n = print(makelist n);
val printXs = fn: int -> unit

printXs 4;
XXXXXXXXVal it = (): unit
```

```
Input
```

```
File

cat test

12
ab

Open the file

val infile = TextIO.openIn ("test");
val infile = ?: TextIO.instream
```

#### Instreams

```
TextIO.endOfStream (infile);
val it = false: bool

TextIO.inputN (infile,4);
val it = "12\na": string

TextIO.inputN (infile,1);
val it = "b": string

TextIO.inputN (infile,1);
val it = "\n": string

TextIO.endOfStream (infile);
val it = true: bool
```

## Reading lines of a file

```
val infile = TextIO.openIn ("test");
val infile = ?: TextIO.instream

TextIO.inputLine (infile);
val it = SOME "12\n": string option

TextIO.inputLine (infile);
val it = SOME "ab\n": string option

TextIO.inputLine (infile);
val it = NONE: string option
```

# Reading complete files

```
val infile = TextIO.openIn ("test");
val infile = ?: TextIO.instream

val s = TextIO.input (infile);
val s = "12\nab\n": string
```

# Read a single character

TextIO.input1

Reads a single character. Type

val it = fn: TextIO.instream -> char option

## Lookahead

TextIO.lookahead;
val it = fn: TextIO.instream -> char option

Reads the next character, but leaves it in the input stream

## Are there n characters left?

TextIO.canInput(f,n);

Are there at least n characters available on instream f?

## Write expressions to

- 1. Open a file zap for reading
- 2. Close the file whose instream is in1
- 3. Read 5 characters from the instream in2
- 4. Read a line of text from the instream in3
- 5. Read the entire file from instream in4
- 6. Find the first character waiting on the in1, without consuming it

```
1. val IN = TextIO.openIn("zap")
2. TextIO.closeIn(in1);
3. TextIO.inputN(in2,5);
4. TextIO.inputLine(in3);
5. TextIO.input(in4);
6. TextIO.lookahead(in1);
```

Assume that we have a file with the following contents

```
abd
de
f
```

What does each command return, if issued repeatedly

```
val x = input (infile);
val x = input1 (infile);
val x = inputN (infile,2);
val x = inputN (infile,5);
val x = inputLine (infile);
val x = lookahead (infile);
```

# ${\sf Solution}$

- 1. First time abc\nde\nf\n, Subsequent times, the empty string
- 2. a, b, c, n, d, e, n, f, then empty string
- 3. ab,  $c\n$ , de,  $\n$ f, enpty string
- 4. abc\nd, e\nf then empty string
- 5.  $abc\n$ ,  $de\n$ ,  $f\n$ , then empty string
- 6. Always a

What are the types of the following expressions

```
1. SOME()
```

- 2. SOME 123
- 3. SOME NONE
- 4. fun f() = SOME true;
- 5. fun f(NONE) = 0 | f(SOME i) = 1;

# ${\sf Solution}$

- 1. unit option
- 2. int option
- 3. 'a option option
- 4. fn:unit -> bool option
- 5. fn : 'a option -> int

Read a file of characters, treating it as a sequence of words (consecutive, non-white space characters). Return a list of the words in the file

```
(* test if a character is white space *)
    fun white(" ") = true
        white("\t") = true
       white("\n") = true
        white(_) = false;
    fun getWord(file) = (* read one word *)
    if TextIO.endOfStream(file) then ""
    else
    let
    val c = TextIO.inputN(file,1)
    in
    if white(c) then ""
    else c^getWord(file)
    end;
```

### Solution, continued

```
fun getList1(file) = (* read all words from an instream *)
if TextIO.endOfStream(file) then nil
else getWord(file) :: getList1(file);

(* read all words from a file given the file name *)
fun getList(filename) = getList1(TextIO.openIn(filename));
```

# Exceptions

```
5 div 0;
Exception- Div raised

hd (nil: int list);
Exception- Empty raised

tl (nil: real list);
Exception- Empty raised

chr (500);
Exception- Chr raised
```

# User-defined exceptions

```
exception Foo;
exception Foo
raise Foo;
Exception- Foo raised
```

## Another example

```
exception BadN;
exception BadM
fun comb(n,m)=
   if n<O then raise BadN
   else if m<0 orelse m>n then raise BadM
   else if m=0 orelse m=n then 1
   else comb(n-1,m) + comb(n-1,m-1);
val comb = fn: int * int -> int
comb(5,2);
val it = 10: int
comb(~1,0);
Exception- BadN raised
comb(5,6);
Exception- BadM raised
```

## Exceptions with parameters

```
exception Foo of string;

raise Foo ("bar");
Exception- Foo "bar" raised

raise Foo(5);
poly: : error: Type error in function application.

raise Foo;
poly: : error: Exception to be raised must have type exn.
```

## Handling exceptions

```
exception OutOfRange of int * int;

fun comb1(n,m)=
   if n <= 0 then raise OutOfRange (n,m)
   else if m<0 orelse m>n then raise OutOfRange (n,m)
   else if m=0 orelse m=n then 1
   else comb1 (n-1,m) + comb1 (n-1,m-1);

val comb1 = fn: int * int -> int
```

### Exceptions, continued

```
fun comb (n,m) = comb1 (n,m) handle
   OutOfRange (0,0) => 1 |
   OutOfRange (n,m) => (
          print ("out of range: n=");
          print (Int.toString(n));
          print (" m=");
          print (Int.toString(m));
          print ("\n");
          0
     );
val comb = fn: int * int -> int
comb (4,2);
val it = 6: int
comb (3,4);
out of range: n=3 m=4
val it = 0: int
comb (0,0);
val it = 1: int
```

# Exercise

Write a program to return the third element of a list of integers

#### Solution

```
exception shortList of int list;
fun returnThird1 L =
   if length(L) < 3 then raise shortList (L)
   else hd(tl(tl(L)));
val returnThird1 = fn: int list -> int
fun returnThird L = returnThird1 L handle
    shortList L => (
       print ("List too short\n");
       0
val returnThird = fn: int list -> int
returnThird [1,2,3,4];
val it = 3: int
returnThird [1,2];
List too short
val it = 0: int
```

# Exercise

Write a factorial function that produces 1 when its argument is 0, 0 for a negative argument, with an error message

#### Solution

```
exception Negative of int;
     fun fact1(0) = 1
         fact1(n) =
             if n>0 then n*fact1(n-1)
             else raise Negative(n);
val fact1 = fn: int -> int
     fun fact(n) = fact1(n) handle Negative(n) => (
         print("Warning: negative argument ");
         print(Int.toString(n));
         print(" found\n");
     );
val fact = fn: int -> int
```

# Solution, continued

```
fact 5;
val it = 120: int

fact 0;
val it = 1: int

fact ~2;
Warning: negative argument ~2 found
val it = 0: int
```