

1 Theorem

The sum of the n th roots of unity is always 0, for $n \geq 2$.

2 Proof

We will denote the n th root of the complex number z with ζ_n .

Then, it follows that:

$$\begin{aligned} w &= n \\ \zeta_1 &= \sqrt[n]{r} \left(\sin \frac{\theta + 2\pi(1)}{n} + i \cos \frac{\theta + 2\pi(1)}{n} \right) \\ \zeta_2 &= \sqrt[n]{r} \left(\sin \frac{\theta + 2\pi(2)}{n} + i \cos \frac{\theta + 2\pi(2)}{n} \right) \\ \zeta_3 &= \sqrt[n]{r} \left(\sin \frac{\theta + 2\pi(3)}{n} + i \cos \frac{\theta + 2\pi(3)}{n} \right) \end{aligned}$$