Artificial Intelligence

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Assignment 2: Causal Inference

Giorgia Adorni (giorgia.adorni@usi.ch)

1 Structure of the Network

The problem modelled is a generic trip by car, influenced by factors such as the strike of public transport, road works or even the weather, and the delay that comes with it. The causal diagram that model this problem includes the following variables:

- Weather: weather during the journey that should be sunny or rainy.
- Strike: true if a strike of public transport takes place, false otherwise.
- RushHour: true if the time it's rush hour, false otherwise.
- RoadConditions: condition of the road floor, that depends on the weather, and should be *dry* or *wet*.
- Humor: humor of the driver, dependent on the weather, that is good or bad.
- RoadWorks: *true* if there are road maintenance works in progress, *false* otherwise. This variable depends on the conditions of the road.
- Speed: driving velocity, that should be *slow* or *fast*, dependent on the road condition, if it's rush hour and if there are road works.
- Danger: danger incurred during the trip, that should be *low* or *high*, dependent on the driving velocity, the road conditions and if it's rush hour.
- Accident: accident risk, that could be *low* or *high*, influenced by the danger, the humour of the driver and if there is a strike of the public transport.
- Delay: true if the trip is delayed, false otherwise.

The objective of the network is highlight hoe weather and humour impacts on travel safety. The graph could provide valuable indications about the correlation between the driver humour and a delayed trip, or for example between the weather and the risk of an accident and also on how the road conditions influences car crashes.

Each node is connected by an arrow to one or more other nodes upon which it has a causal influence. Most of the arcs orientation are self-explaining. An exception was made for the <code>Humor</code> variable, that influences the accident risk and is caused only by the weather and not for example by the delay.

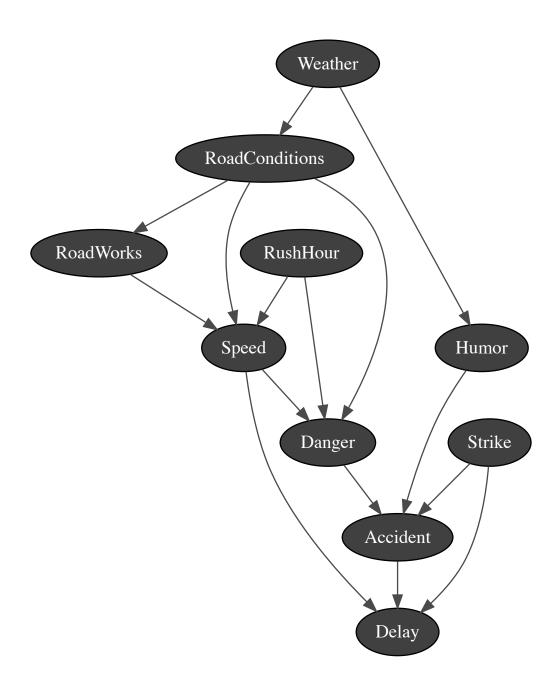


Figure 1: Bayesian Network

An arc can be inverted if and only if no v-structures, i.e. colliders in which the parents are not adjacent, are generated or destroyed in doing so.

In the model there are only two arrow that can be inverted, and these are the one that goes from the variable Weather to Humor and the one that goes from the variable Weather to RoadConditions. In fact, even inverting the two arrows no v-structured are created, therefore the three graphs that are generated by the reversions of the two arcs are equivalent and not distinguishable by any statistical test.

Instead, the arc from RoadWorks to RoadConditions cannot be reverted since doing

this a v-structure is created. Hence, the arc could only be turned on condition of turn also the one between Weather and RoadConditions.

D-Separation

D-Separation tells when two variables are d-separated along a path (blocked), that means independent and when they are d-connected along a path (unblocked) or likely dependent. They are actually independent if they are d-separated along all possible paths. They are likely dependent if there is at least one unblocked path connecting them.

A path is blocked by a set of nodes if and only if the path contains a chain of nodes or a fork such that the middle node is in the set of nodes or if the path contains a collider such that the collision node and every descendant are not in the given set of nodes.

• RushHour and RoadConditions:

Conditioning on one of the variables Strike, RoadWorks Weather or Humor, RushHour and RoadConditions are d-separated since the path from these two variables are all blocked. They are not actually independent since they are not d-separated along the paths that condition on variables Danger, Speed, Accident and Delay since in all this cases the path contains a collider in which the given is a collision node. In fact, all the variables d-connected are dependent in the real problem, for example RushHour, RoadConditions and Danger, while RushHour, RoadConditions and Humor are independent.

• RushHour and Strike:

Conditioning on one of the variables Danger, RoadWorks, Weather, Speed or Humor, RushHour and Strike are d-separated since the path from these two variables are all blocked. Instead, they are not d-separated along the paths that condition on variables Accident and Delay since in both the cases the paths contain a collider in which the given is the collision node. Hence, they are not independent. In the real problem, in fact, the d-connected variables are dependent, for example RushHour, Strike and Danger, while RushHour, Strike and RoadWorks are independent.

• Speed and Accident:

Are not d-separated given any of the variables of the domain.

• RoadConditions and Strike:

In this case the same considerations made for the variables RushHour and Strike in example 2 apply.

• Speed and Humor:

Conditioning on one of the variables RoadConditions or Weather, Speed and Humor are d-separated since the path from these two variables are all blocked. Instead, they are not d-separated along the paths that condition on all the other variables, so they are not independent. The d-connected variables, for example Speed, Humor and Danger, are dependent in the real problem, while Speed, Humor and RoadConditions are not dependent.

2 Conditional Probability Tables

The Conditional Probability Tables (CPTs) of the variables of the model, that show all possible inputs and outcomes with their associated probabilities, are filled sometimes using information retrieved from online survey, other times are estimated based on common sense. In case of the variable Weather, since his prior probability is difficult to estimate because it is dependent on different factors, such as the location, the probabilities correspond to a uniform distribution.



.5000 0.5000



Weather CPT

Strike CPT

RushHour CPT

	Humor		
Weather	Good	Bad	
Sun	0.8000	0.2000	
Rain	0.3000	0.7000	

Humor CPT

 RoadConditions

 Weather
 Dry
 Wet

 Sun
 0.7500
 0.2500

 Rain
 0.4000
 0.6000

RoadConditions CPT

 RoadConditions
 True
 False

 Dry
 0.1000
 0.9000

 Wet
 0.8000
 0.2000

RoadWorks CPT

				Speed	
RoadConditions	RushHour	RoadWorks	Slow	Fast	
	True	True	0.8500	0.1500	
Dry		False	0.8000	0.2000	
	False	True	0.7500	0.2500	
		False	0.1500	0.8500	
Wet False	T	True	0.9500	0.0500	
	True	False	0.8000	0.2000	
	False	True	0.9000	0.1000	
		False	0.6000	0.4000	

Speed CPT

			Danger	
RushHour	Speed	Low	High	
True	Slow	0.8500	0.1500	
	Fast	0.2000	0.8000	
False	Slow	0.9500	0.0500	
	Fast	0.3000	0.7000	
True	Slow	0.4500	0.5500	
	Fast	0.0500	0.9500	
False	Slow	0.5500	0.4500	
	Fast	0.2000	0.8000	
	True False True	True Slow Fast Slow Fast Slow Fast True Slow Fast Slow Fast	RushHour Speed Low True Slow 0.8500 Fast 0.2000 False Slow 0.9500 Fast 0.3000 True Slow 0.4500 Fast 0.0500 False Slow 0.5500	

Danger CPT

		Accident		
Danger	Strike	Humor	Low	High
Low	True	Good	0.1500	0.8500
		Bad	0.7000	0.3000
	False	Good	0.0500	0.9500
		Bad	0.5500	0.4500
High	True	Good	0.8500	0.1500
		Bad	0.9500	0.0500
	False	Good	0.6000	0.4000
		Bad	0.8000	0.2000

Accident CPT

			Delay	
Speed	Strike	Accident	True	False
	True	Low	0.7500	0.2500
Slow		High	0.9800	0.0200
	False	Low	0.6500	0.3500
		High	0.9500	0.0500
Fast	True	Low	0.6000	0.4000
		High	0.9000	0.1000
	False	Low	0.4500	0.5500
		High	0.8500	0.1500

Delay CPT

3 Causal Inference

Choose one pair of variables. The pair must be made up of a variable X with at least one parent and another variable Y of the graph such that there is (at least) a causal path from X to Y. For the pair (X,Y) perform: \bullet Calculate the causal effect of X on Y. \bullet Identify possible confounders between X and Y. \bullet Would it be practically possible in your specific problem to perform also a randomized controlled study to disentangle the causal effect between the variables from their correlation? \bullet Compute the ACE of X on Y. Choose another pair of variable (X,Y) (it can be also the previous one) and: \bullet Choose another variable C such that it is possible to calculate the c-specific effect of X on Y and calculate it. \bullet Identify a minimal set of variables that must be measured in order to estimate the c-specific effect of X on Y. \bullet Choose a function g and compute the effect of the conditional intervention of X=g(C) on Y. Choose another pair of variable (X,Y) (it can be also the previous one) and: \bullet Identify possible mediating variables between X and Y and calculate the CDE of Y changing the value of X.

4 Simulation

Suppose that you can't measure some parents of variable X chosen in every point of "Causal Inference". Repeat the "Causal Inference" part of the exercise considering this new situation.

5 Comment on the Results

What kind of experience have you got with this model? E.g., is the causal model responding in a sensible way to your queries? What should be changed/modified to make it more realistic?