

# Data Intelligence Application

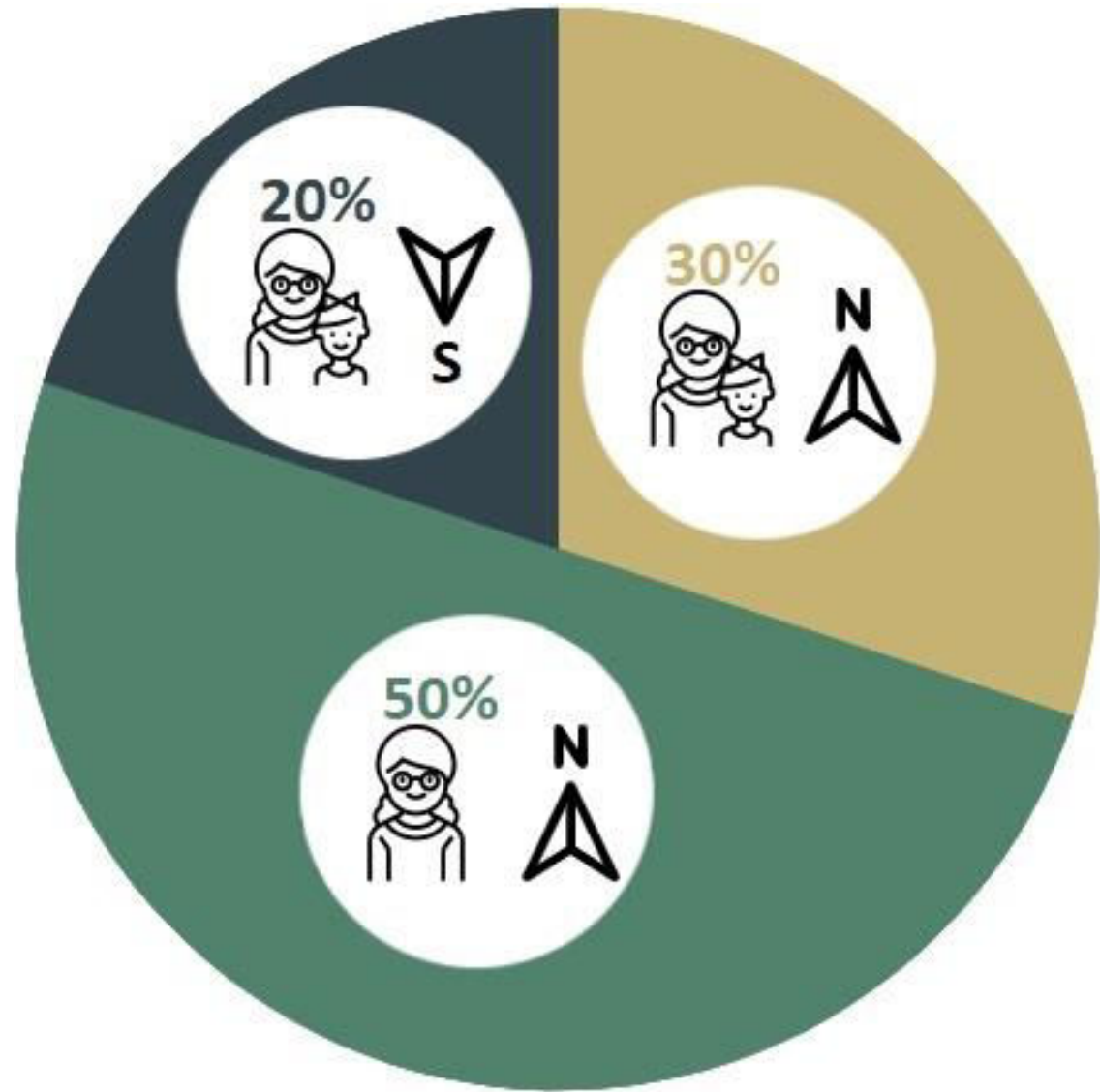
Pricing & Advertising

The Product

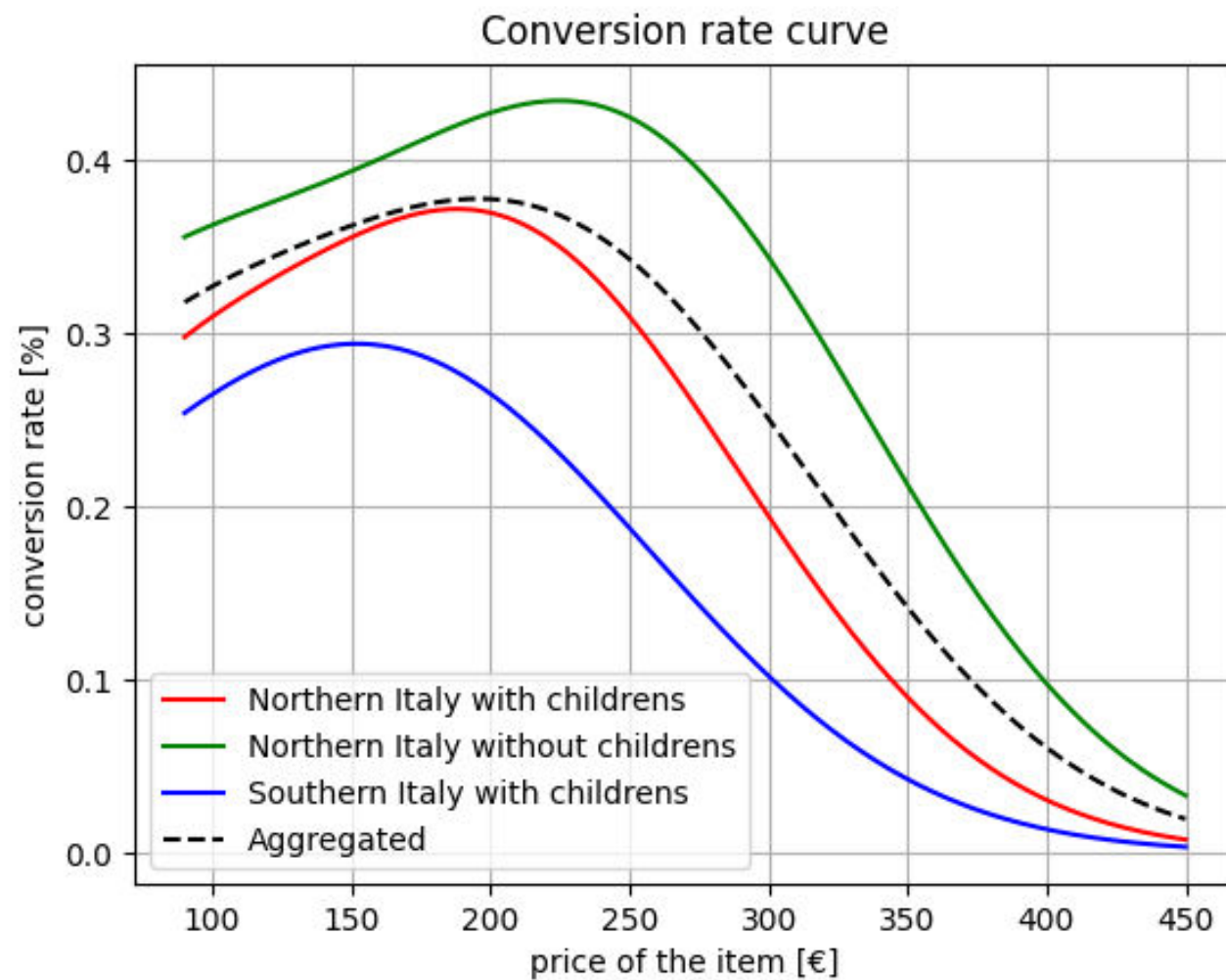


Louis Vuitton Scarf

## The Users



## The Curve



## The Phases



JAN

FEB

MAR

**High Interest  
No Competitors**

APR

MAY

JUN

**Low Interest  
No Competitors**

JUL

AUG

SEP

**Low Interest  
A New Competitor  
Enters The Market**

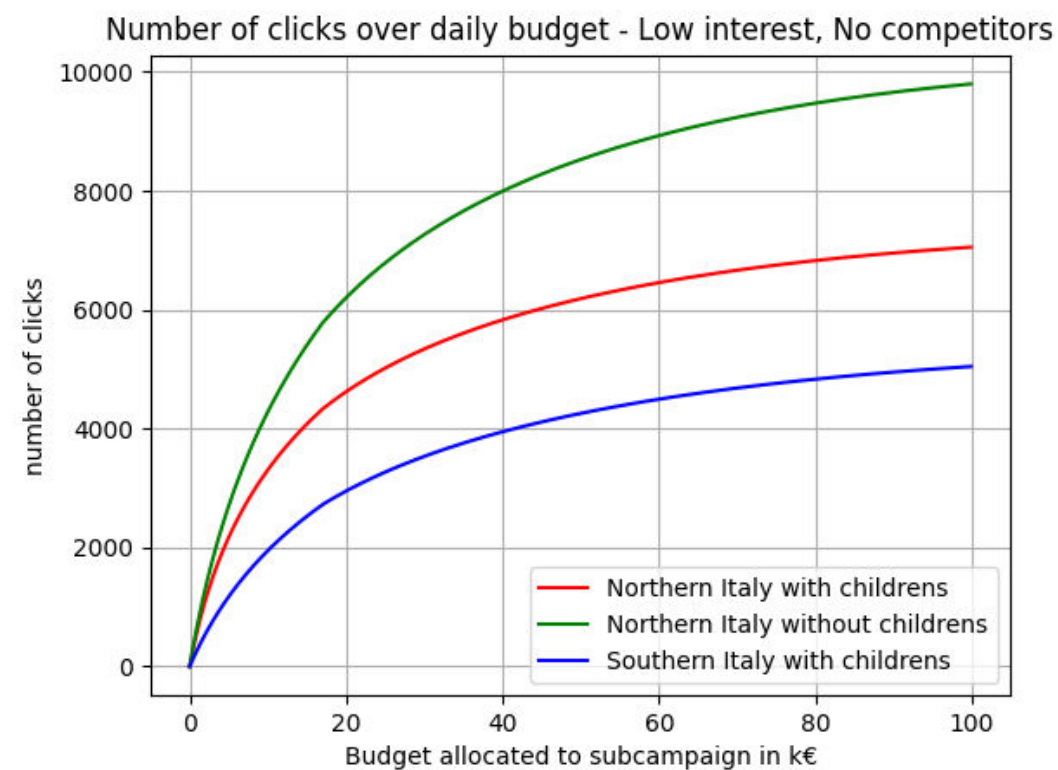
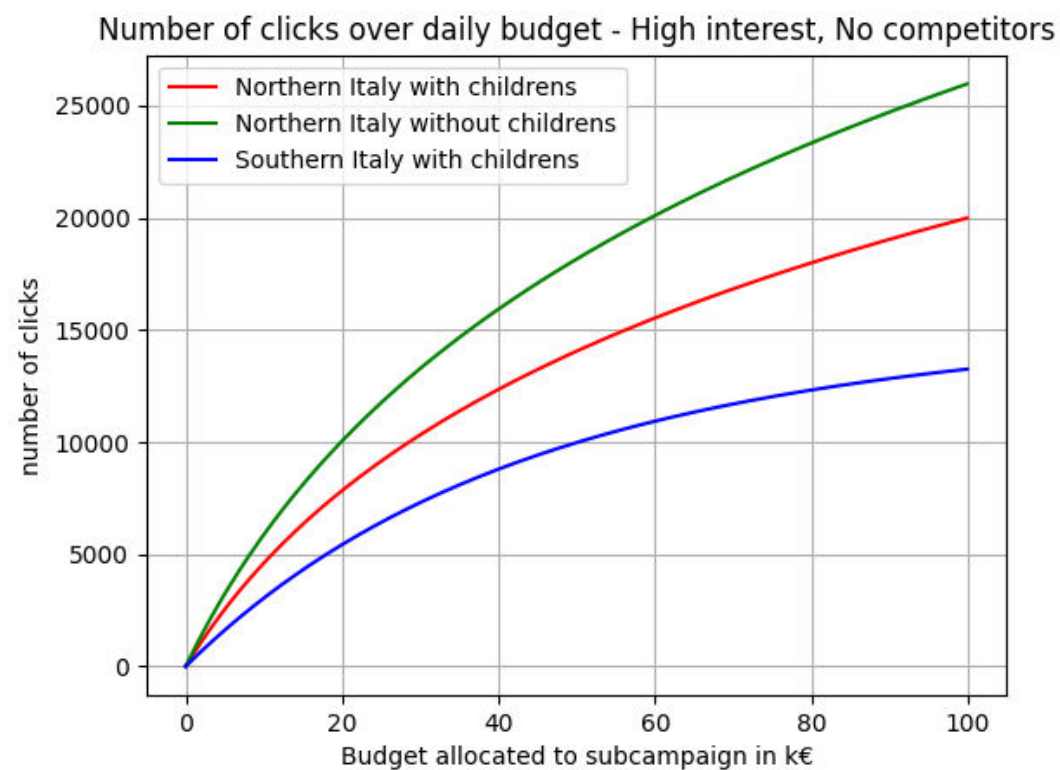
OCT

NOV

DEC

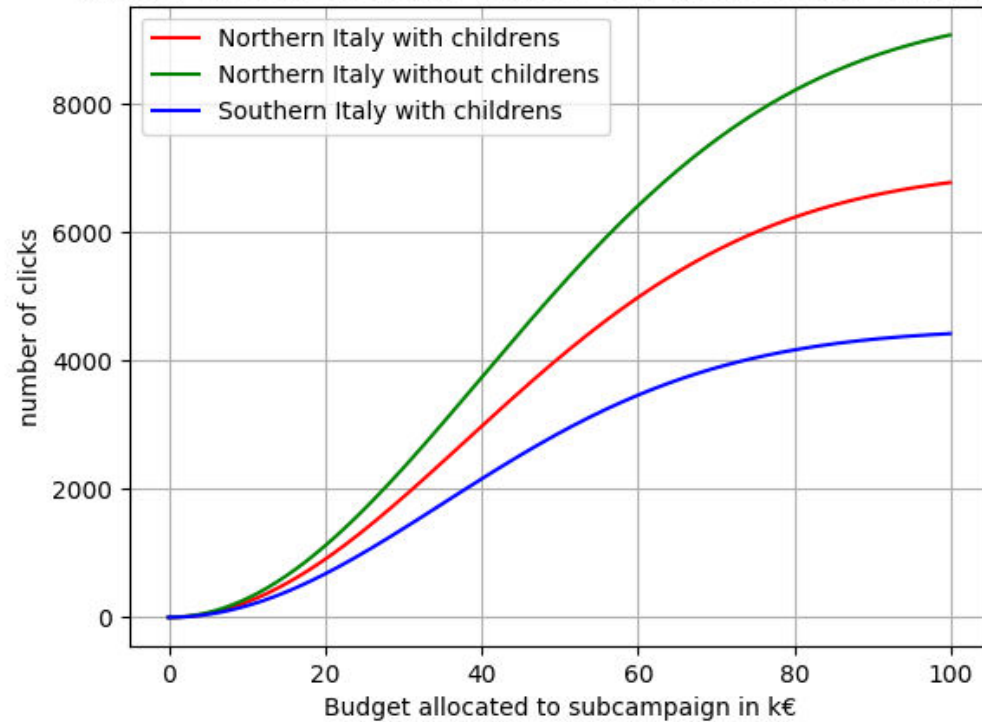
**High Interest  
With Competitors**

# The Phases (1/2)

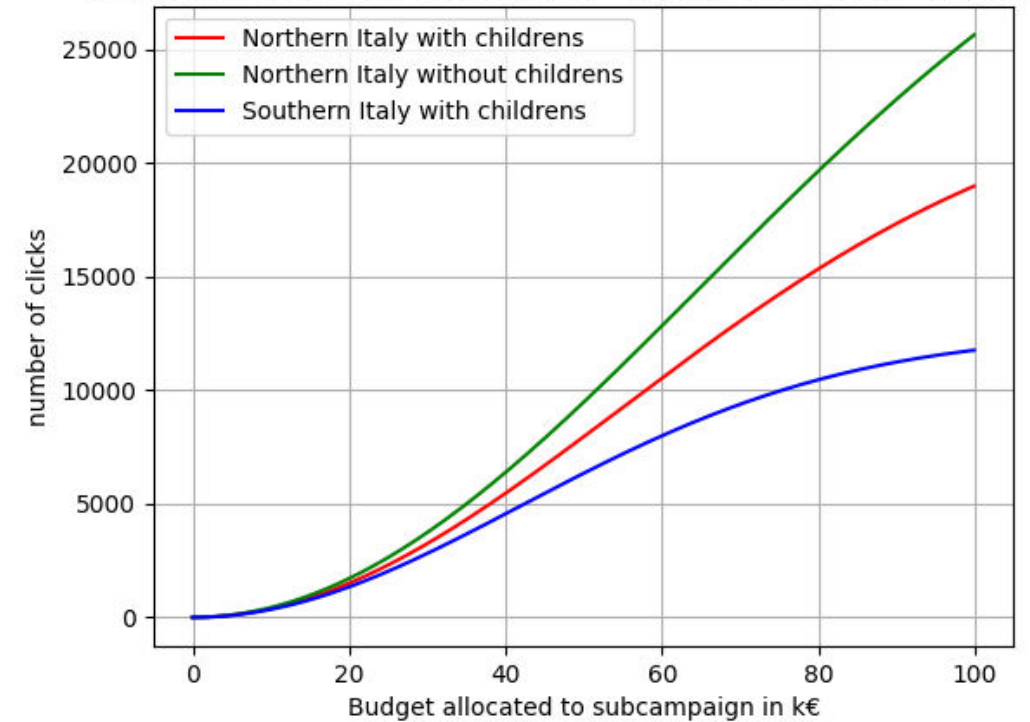


## The Phases (2/2)

Number of clicks over daily budget - Low interest, With competitors



Number of clicks over daily budget - High interest, With competitors



# Budget Allocation

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The first step of our project was focused on the budget allocation over the three subcampaigns and had as goal the maximization of the total number of clicks.

The graphs shows the results the we obtained considering just one phase and considering all the four phases.



# The Algorithm (One Phase)

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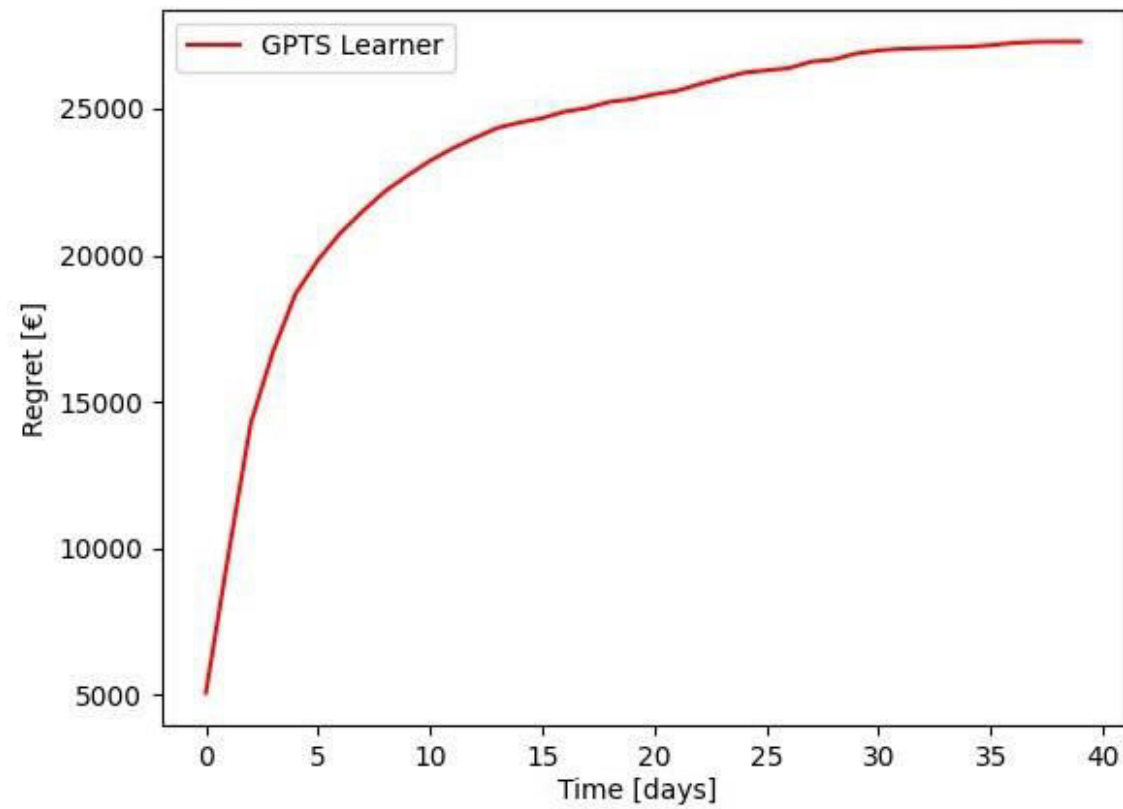
**Algorithm 1** Gaussian Process CMAB

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```
1:  $J \leftarrow$  all classes of users
2: for  $day \in T$  do
3:   for  $j \in \{1, \dots, J\}$  do
4:      $s \leftarrow$  Sample  $j$ -th GP-Learner
5:     Add  $s$  row to knapsack matrix
6:   end for
7:   Optimize knapsack matrix
8:   Play selected superarm
9:   Update GP-Learners model
10: end for
```

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# The Result (One Phase)



# The Algorithm (Four Phases)

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**Algorithm 2** Gaussian Process CMAB

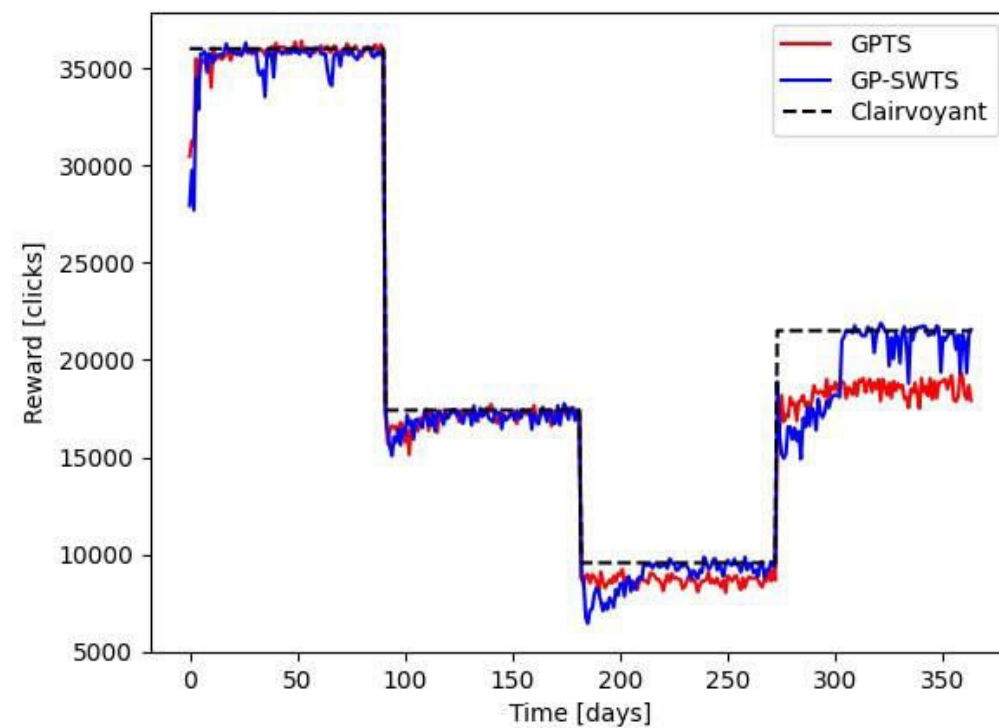
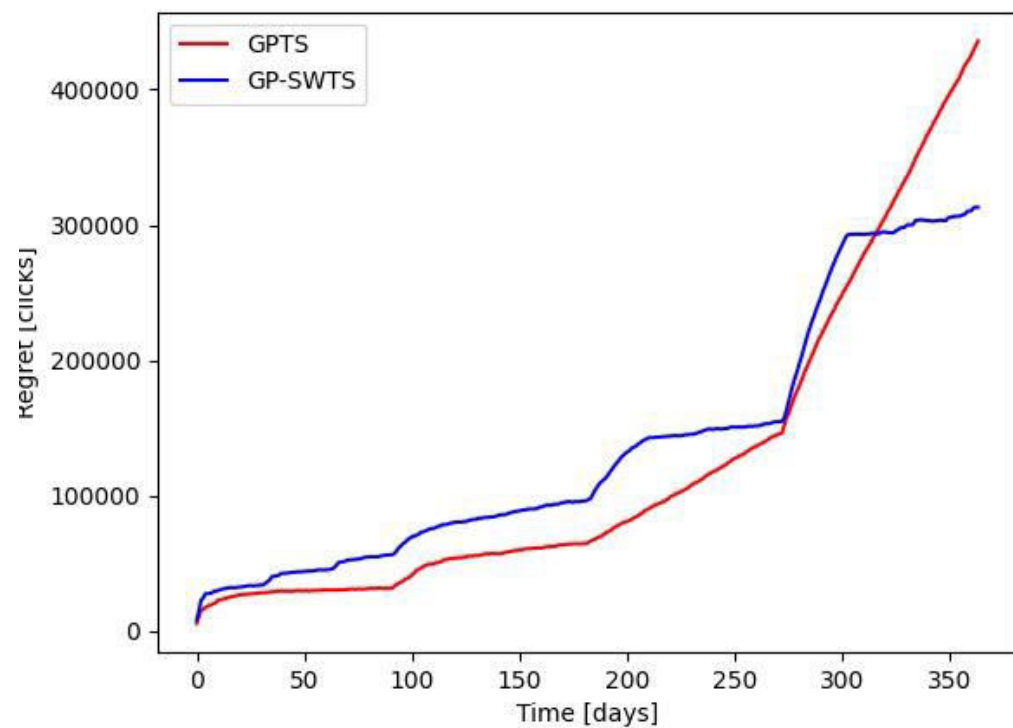
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**Input:**  $\tau$  sliding window size,  $J$  classes of users

```
1: for  $day \in \{1, \dots, T\}$  do  
2:   for  $j \in \{1, \dots, J\}$  do  
3:     Sample  $j$ -th GP-Learner( $\tau$ )  
4:     Add row to knapsack matrix  
5:   end for  
6:   Optimize knapsack matrix  
7:   Play selected superarm  
8:   Update GP-Learners model( $\tau$ )  
9: end for
```

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# The Results (Four Phases)



# Price Learning

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Next, we describe the learning algorithms that we used to maximize the number of purchases made by users that have reached our website by clicking on ads.

We first consider a normal setup followed by a context generation algorithm.

# The Algorithm (No Context)

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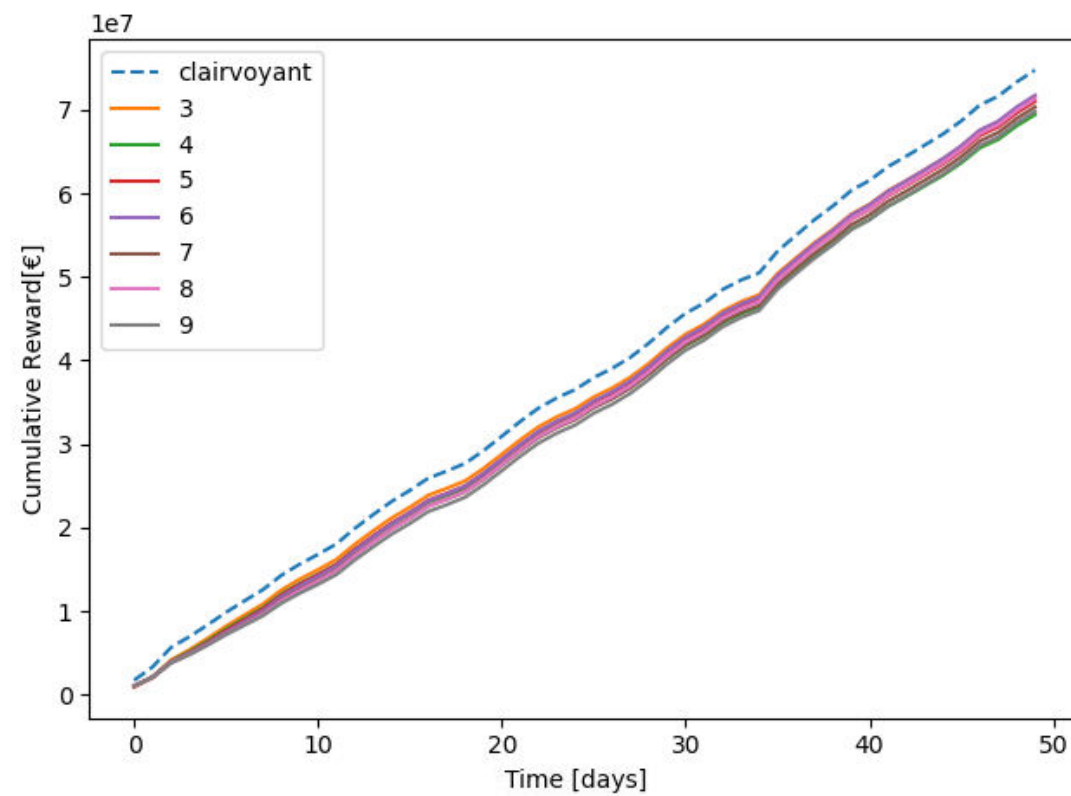
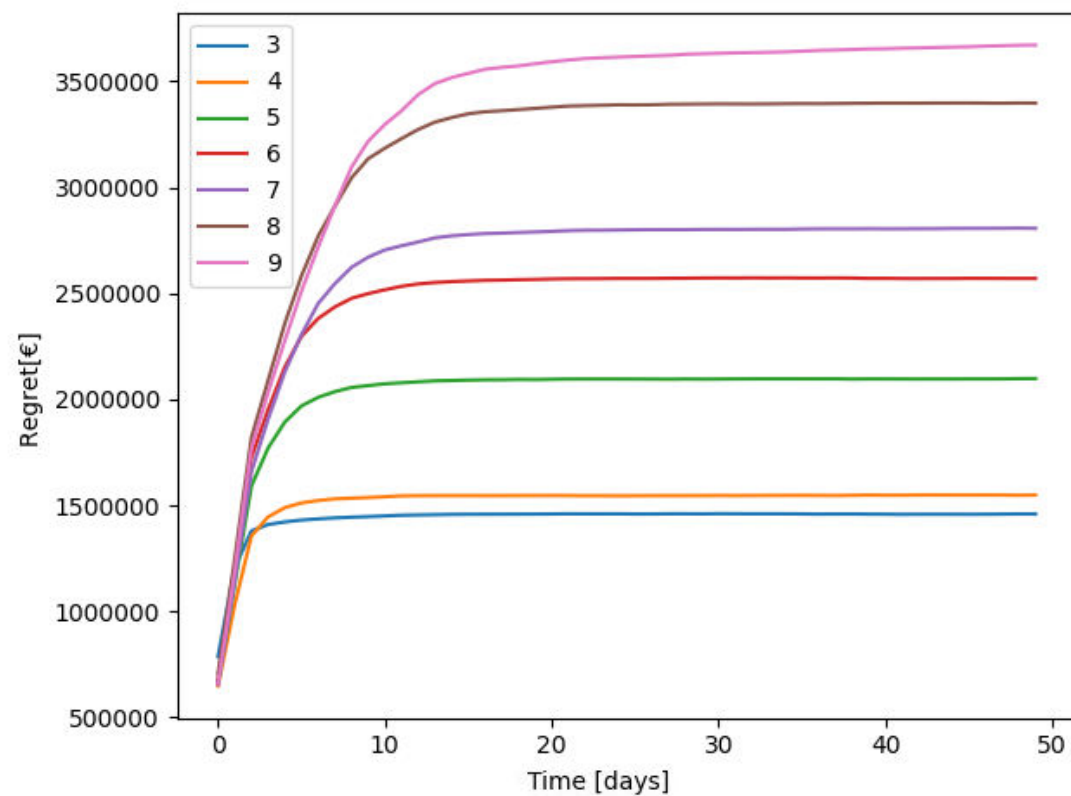
**Algorithm 3** TS learners for pricing

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```
1:  $J \leftarrow$  all classes of users
2:  $T \leftarrow$  45 days
3:  $regret \leftarrow 0$ 
4: for  $day \in T$  do
5:   for  $j \in \{1, \dots, J\}$  do
6:      $price \leftarrow$  Draw a price from the  $j$ -th TS learner
7:      $successes \leftarrow$  play the pulled arm
8:      $failures \leftarrow clicks[j][day] - successes$ 
9:      $reward \leftarrow successes * price$ 
10:     $regret += optimum - reward$ 
11:     $TS[j].update(price, successes, failures)$ 
12:   end for
13: end for
```

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# The Results (No Contexts)



# The Algorithm (With Context)

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**Algorithm 4** Context Generator Algorithm

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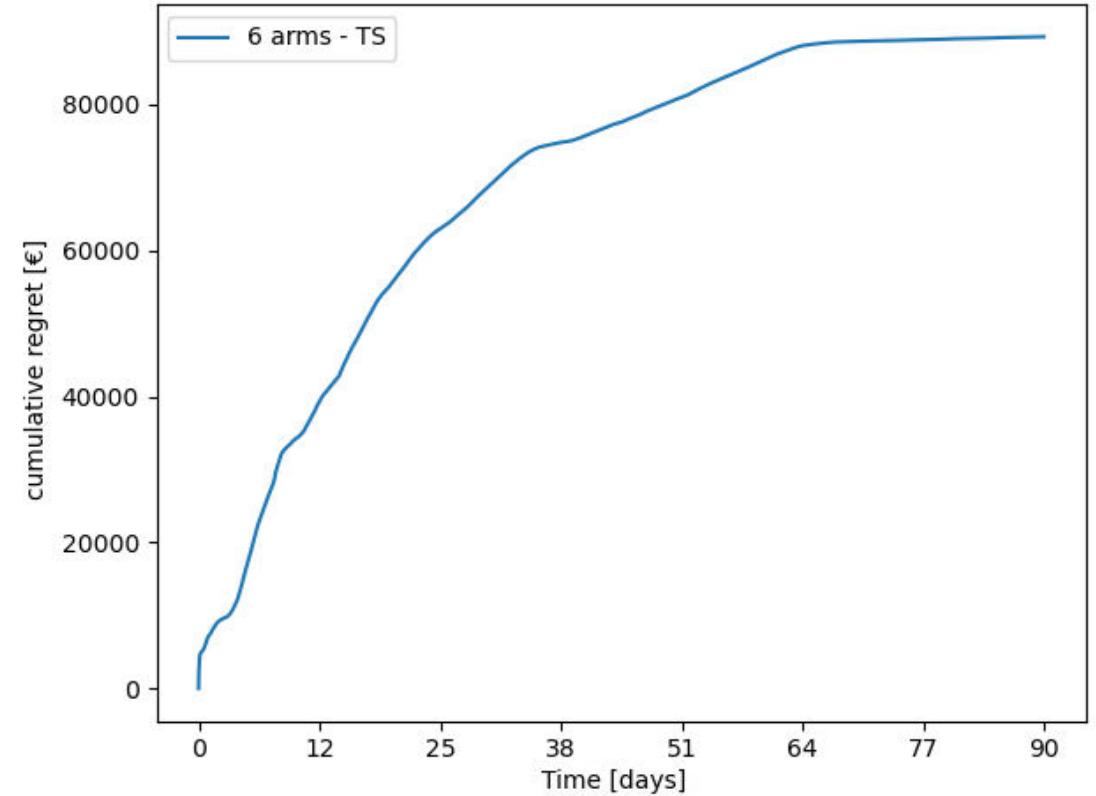
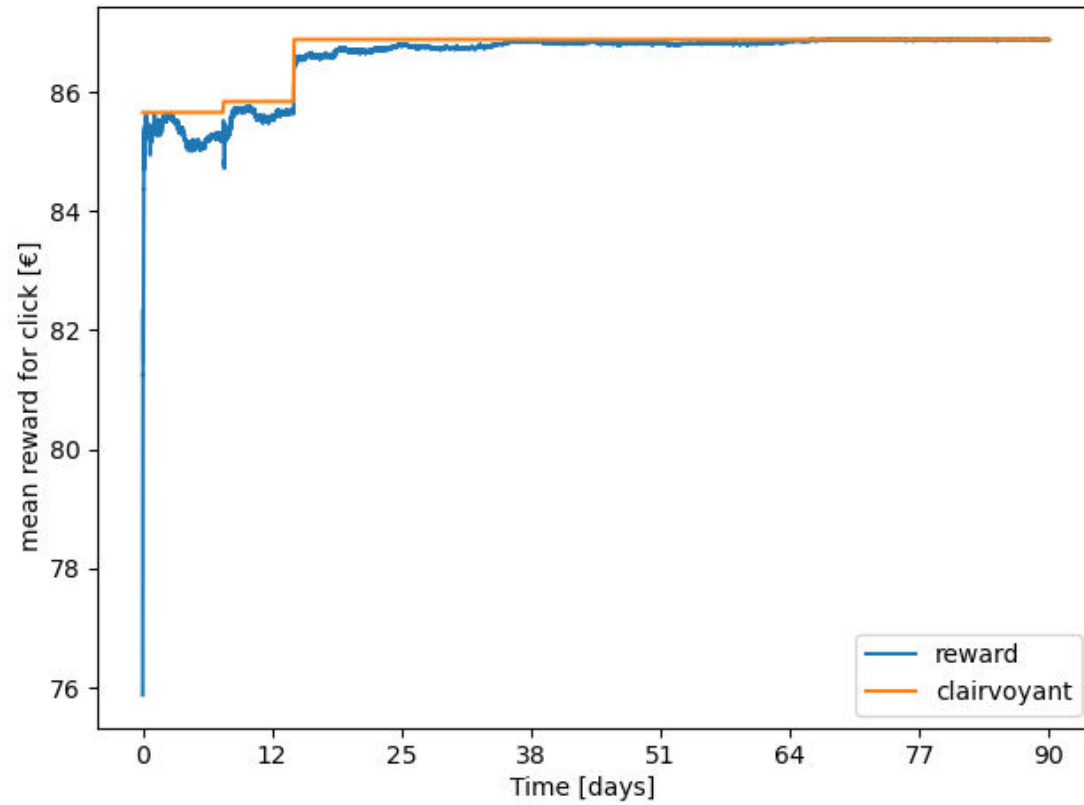
**Input:**  $T$  : time span of the experiment,  $C$  : number of clicks per day

```
1: for  $1 \leq t \leq T$  do
2:   for  $1 \leq c \leq C$  do
3:     for  $context \in Contexts$  do
4:       for  $usertype \in context$  do
5:          $sort \leftarrow$  Draw the choice of the user from the binomial
6:          $successes \leftarrow$  Update the number of successes for that user and
           context
7:          $failures \leftarrow$  Update the number of failures for that user and
           context
8:       end for
9:        $reward \leftarrow$  Update the reward value for the day
10:    end for
11:     $rewards \leftarrow$  Append the reward value for the day
12:  end for
13:  if  $t \bmod 7 == 0$  then
14:    for  $context \in Contexts$  do
15:      for  $usertype \in context$  do
16:        if split condition achieved then
17:           $c1, c2 \leftarrow$  Perform the split
18:        end if
19:      end for
20:    end for
21:  end if
22: end for
```

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# The Results (With Contexts)



# Optimization

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After studying the budget allocation and the pricing scenario separately, we imagined the union of the two, used in a real application of the selling of our scarf.

We first considered an environment without constraints, to later focus on a constrained variation.

# The Algorithm (No Constraints)

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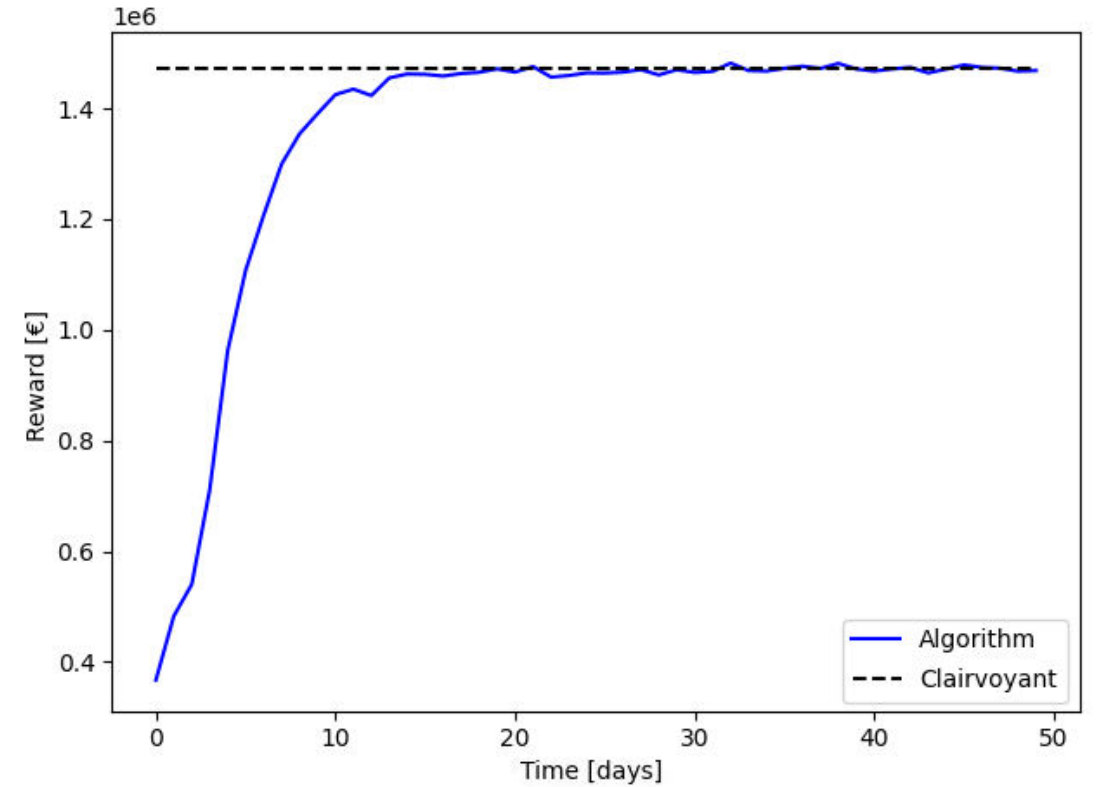
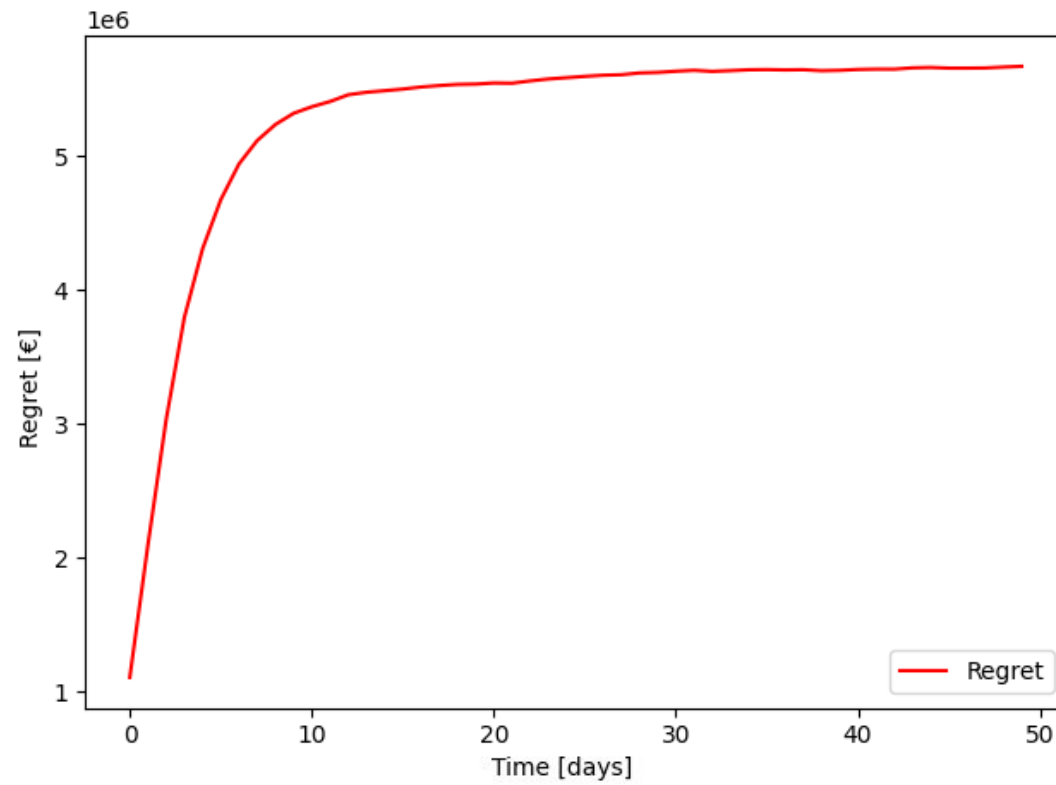
**Algorithm 5** Optimization Algorithm

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```
1:  $J \leftarrow$  all classes of users
2: for  $day \in T$  do
3:   for  $j \in \{1, \dots, J\}$  do
4:      $p \leftarrow$  Sample(j-th TS)           // Price
5:      $a \leftarrow$  Get predicted conversion-rate given the pulled arm
6:      $c \leftarrow$  Sample(j-th GPTS)         // Number of clicks
7:      $b \leftarrow$  Budget(j-th GPTS)         // Budget spent
8:      $v \leftarrow \frac{p \cdot a \cdot c - b}{c}$  // Value per click
9:     Add row  $v \cdot c$  to knapsack matrix
10:  end for
11:   $a \leftarrow$  Optimize knapsack matrix
12:   $rew \leftarrow$  Play selected superarm  $a$ 
13:  Update GPTS-Learners model
14:  Update TS-Learners model
15: end for
```

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# The Results (No Constraints)



# The Algorithm (With Constraints)

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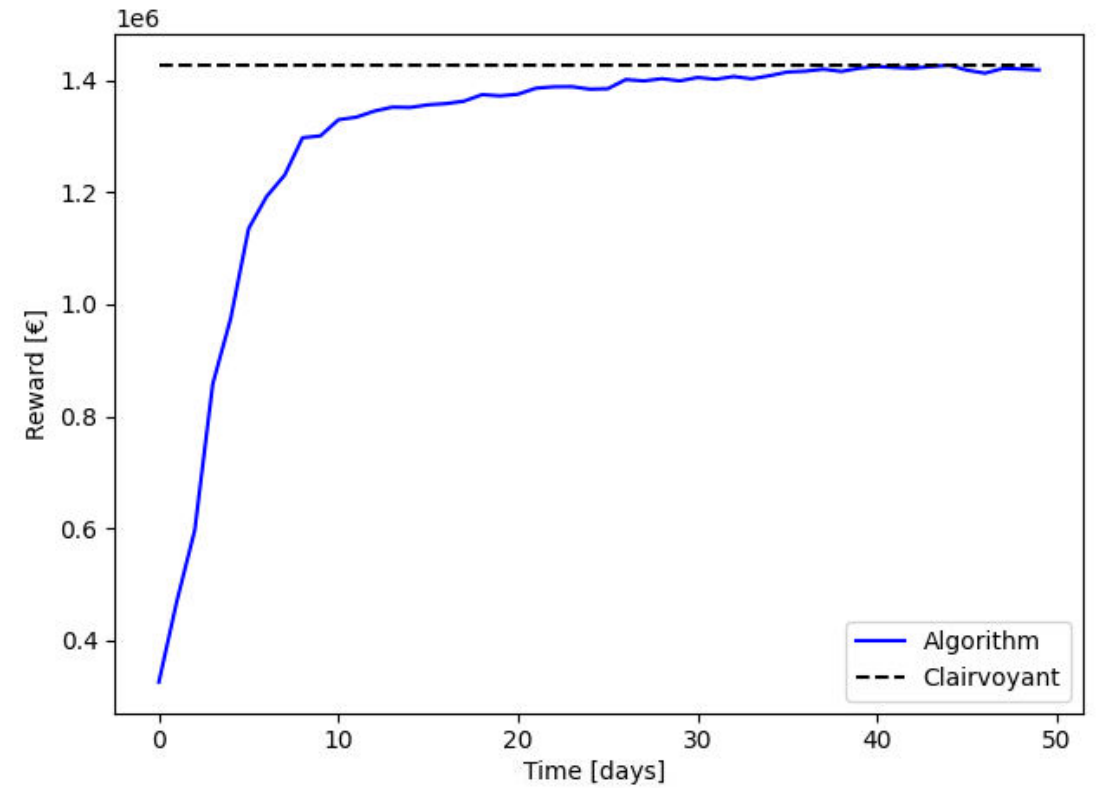
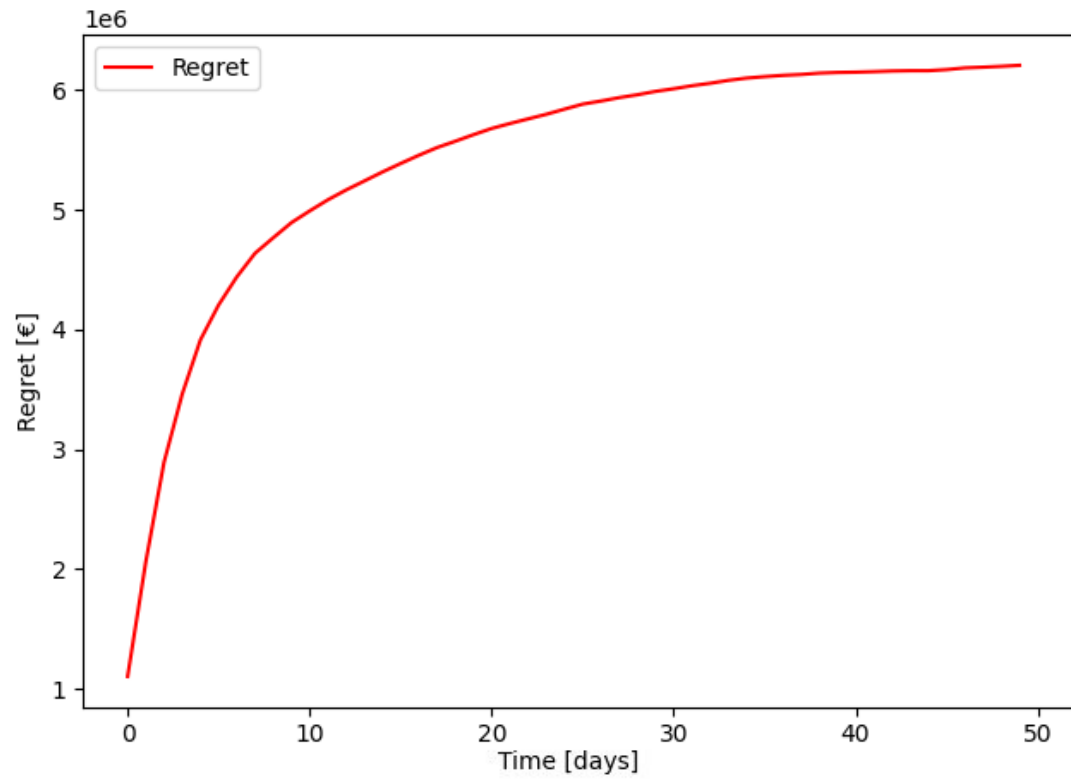
**Algorithm 6** Budget and Pricing optimization with fixed price


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```
1: for  $1 \leq t \leq T$  do
2:    $\theta \leftarrow$  draw a sample from all TS Learners
3:   for  $p \in \theta$  do
4:      $d_p \leftarrow \text{demand}(p)$ 
5:     for  $1 \leq c \leq C$  do
6:       for  $1 \leq b \leq |B|$  do
7:          $\text{clicks}_{c,b} \leftarrow$  Estimate clicks from GPTS learners
8:          $\text{vpc}_{c,b} \leftarrow$  Estimate values per click
9:       end for
10:    end for
11:     $b_{\text{best}_p} \leftarrow$  Use CMAB optimizer to get best budget allocation
12:     $r_{\text{exp}_p} \leftarrow$  Use CMAB optimizer to get expected revenues
13:  end for
14:   $r_{\text{max}} \leftarrow \max r_{\text{exp}}$ 
15:   $(\bar{p}, \bar{b}_c) \leftarrow$  Select best price and budgets associated with  $r_{\text{max}}$ 
16:  for  $1 \leq c \leq C$  do
17:     $(\bar{c}, \bar{b}, \bar{r}) \leftarrow$  Test with env and get real clicks, buys and revenue
18:    Update TS and GPTS learners
19:  end for
20: end for
```

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# The Results (With Constraints)





Thanks  
for your  
attention!!