PREDICTIVE ANALYTICS

MSC INFORMATION SYSTEMS AND SERVICES
SPECIALIZATION: BIG DATA AND ANALYTICS

R EXERCISES PART 2

6.956

25.001

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Exercise 1

Enter the **rpart** package. Upload kyphosis data. Describe the dataset. Make the boxplot for the "Number" variable and then find the outliers (their values)
Which rows correspond to the specific data (%in% - which)
Repeat the last one with the (Identify) function

Solution

- 1) The "kyphosis" data from the **rpart** package contains the following variables:
 - **Kyphosis** = a factor with "absent, present" levels that indicates whether kyphosis (a type of deformity) was present or absent after surgery.
 - Age = years (in months).
 - Number = the number of vertebrae involved.
 - **Start** = the number of the first (highest) vertebra activated.

Descriptive statistics of the dataset

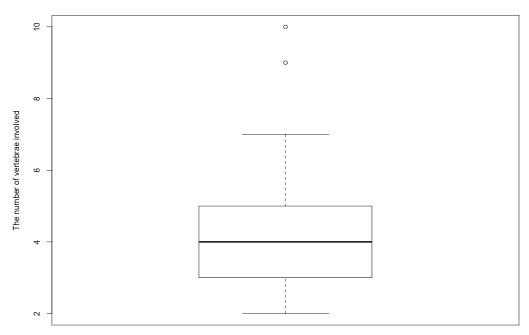
```
summary(df)
  Kyphosis
                                Number
                 Age
                                                Start
                                                  : 1.00
                            Min. : 2.000
                                            Min.
absent :64
            Min.
                  : 1.00
present:17
            1st Qu.: 26.00
                            1st Qu.: 3.000
                                            1st Qu.: 9.00
            Median : 87.00
                            Median : 4.000
                                            Median :13.00
                   : 83.65
                                  : 4.049
                            Mean
                                            Mean
                                                   :11.49
            Mean
                            3rd Qu.: 5.000
                                             3rd Qu.:16.00
            3rd Qu.:130.00
            Max. :206.00 Max. :10.000
                                            Max. :18.00
```

In the descriptive statistics of the data, according to the results that appear from the above code command (summary (df)), out of a total of 81 results, after the operation 17 people show kyphosis while the remaining 64 do not show.

Boxplot for the "Number" variable

>boxplot(df\$Number, main="The Variable: Number", ylab="The number of vert ebrae involved")

The Variable: Number



Outliers

To display the outliers we enter the following 2 commands and display the relevant result.

```
> outliers = df$Number[df$Number>8]
> outliers
[1] 9 10
```

```
> which( df$Number %in% outliers)
[1] 43 53
```

We have two outliers with the values 9 and 10 which correspond to lines 43 and 53 as shown in the above boxplot and from the which & identity commands.

We execute the commands:

```
> plot(df$Number, df$Age)
> identify(df$Number, df$Age)
```

And in this way we execute the identify function with values of x-axis and y-axis as arguments in the scatter plot. With the identify () function by clicking the mouse, above the points in the specific graph, the serial number for the point

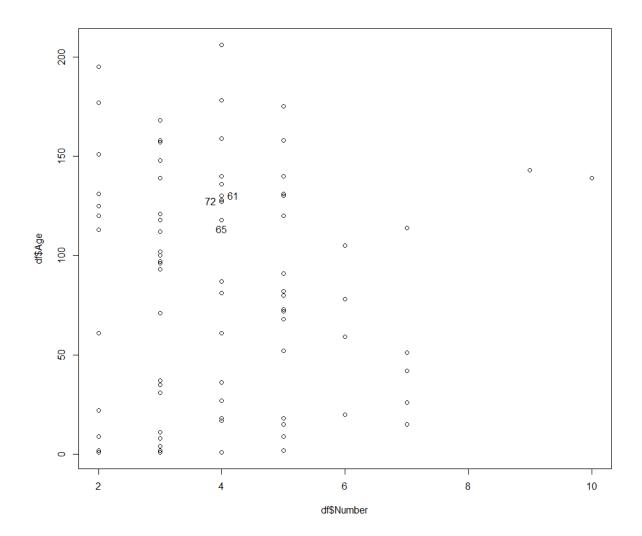
where it was clicked will be displayed. This can continue until we choose to pause.

```
> identify(df$Number, df$Age)
warning: nearest point already identified
warning: nearest point already identified
warning: nearest point already identified
```

In case of clicking on points outside the diagram, the relevant warning will be displayed:

warning: no point within 0.25 inches

The relevant results are shown in the image below.



Exercise 2
Consider the capital.csv dataset

- i. Make the graphs of Balance in relation to Gender (table of relative frequencies, barpie chart)
- ii. The boxplot of our data and the boxplot in relation to "gender"
- iii. Calculate the central trend and deviation measures
- iv. Examine whether our data comes from a normal distribution (e.g. Do Q-Q-plot)

Solutions

dataset capital.csv.

Descriptive Statistics of data:

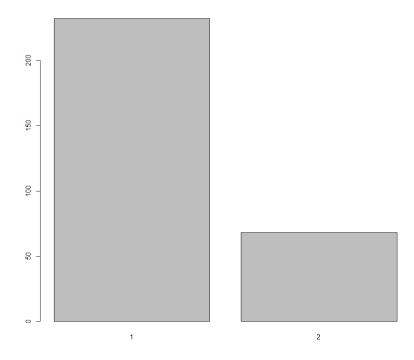
```
> summary(df)
    balance     gender
Min. : 99.0   1:232
1st Qu.: 550.8   2: 68
Median : 737.0
Mean : 753.7
3rd Qu.: 964.2
Max. :1493.0
```

We observe that the capital.csv data file contains a total of 300 people, of which 232 are men and 68 are women..

2 i

table of relative frequencies of Balance in relation to Gender:

> barplot(table(df\$gender))

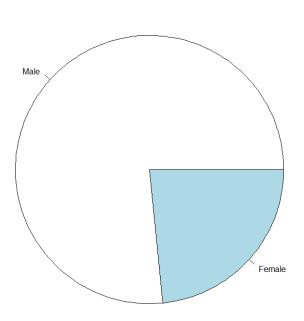


From the command of the above code, we observe that men and women correspond to 77.333% and 22.666% respectively.

Simple Pie Chart

```
> bal_gender <- c(173191, 52913)
> lbls <- c("Male", "Female")
> pie(bal_gender, labels = lbls, main="Balance by gender")
```

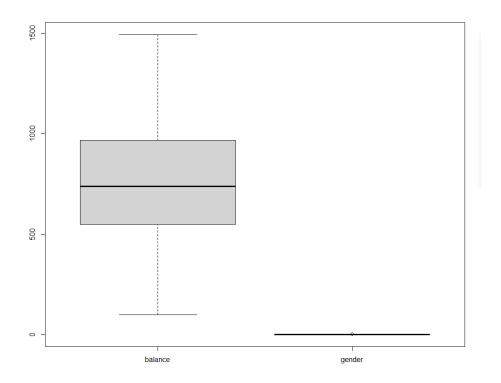
Balance by gender



2 ii

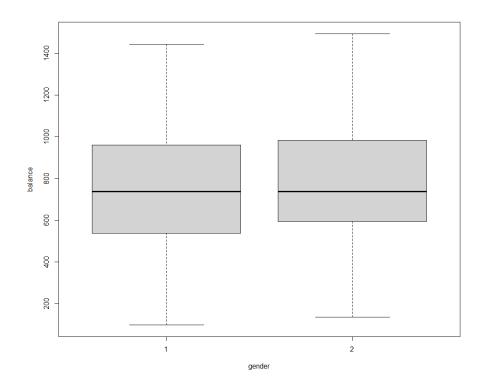
The boxplot of our data is displayed with the following command:

> boxplot(df)



 $\#2\,\text{ii}$ The boxplot in relation to Gender is displayed by the following command:

> boxplot(balance ~ gender, data=df)



2 iii

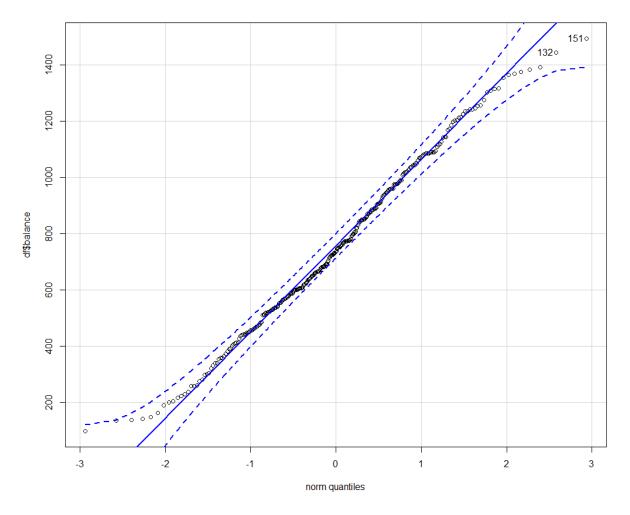
Central Trend and Deviation Measures

To display the results from the central trend and deviation measures, run the describeBy() command.

```
> library(psych)
> describeBy(df$balance, df$gender)
Descriptive statistics by group
group: 1
 vars n mean sd median trimmed mad min max range skew kurtos
is se
X1 1 232 746.51 294.52 738.5 743.88 312.83 99 1443 1344 0.08
group: 2
 vars n mean sd median trimmed mad min max range skew kurtosi
s se
x1 1 68 778.13 295.22 737 773.38 287.62 135 1493 1358 0.21
                                                              -0.3
5 35.8
> summary(df$balance)
  Min. 1st Qu. Median Mean 3rd Qu.
                                      Max.
  99.0 550.8 737.0 753.7 964.2 1493.0
```

2 iv

```
> library("car")
> qqPlot(df$balance)
[1] 151 132
```



From the above graph it appears that the distribution of the "balance" variable seems to follow faithfully the normal distribution with a very small deviation in the queues.

Exercise 3

Consider the mtcars file data that follows a normal distribution.

Find the confidence interval with a confidence interval of 0.95 for the difference of the means corresponding to the fuel consumption variables for the manual and automatic car. (apply the t.test() function)

Solution

This data set describes a number of car models and the am column explains whether the car is manual or automatic.

Descriptive Statistics of data:



```
:10.40 Min.
Min.
                     :4.000 Min. : 71.1 Min. : 52.0
                                                            Min.
                                                                   :2
760
      Min.
            :1.513
                     Min.
                           :14.50
                                    Min.
                                          :0.0000
1st Qu.:15.43
                              1st Qu.:120.8
              1st Qu.:4.000
                                             1st Qu.: 96.5
                                                            1st Qu.:3
      1st Qu.:2.581
                     1st Qu.:16.89
                                    1st Ou.:0.0000
Median :19.20
               Median:6.000
                              Median :196.3
                                             Median :123.0
                                                            Median:3
      Median :3.325
                     Median :17.71
                                    Median :0.0000
       :20.09 Mean
                     :6.188 Mean
                                    :230.7 Mean
Mean
                                                    :146.7
                                                            Mean
                                                                   :3
                     Mean :17.85
597
      Mean :3.217
                                    Mean :0.4375
3rd Qu.:22.80
              3rd Qu.:8.000
                             3rd Qu.:326.0
                                             3rd Qu.:180.0
                                                            3rd Qu.:3
      3rd Qu.:3.610
                    3rd Qu.:18.90
                                    3rd Qu.:1.0000
Max.
      :33.90
              Max.
                     :8.000
                                    :472.0
                             Max.
                                             Max.
                                                    :335.0
                                                            Max.
                                                                   :4
                          :22.90
930
            :5.424
                                          :1.0000
      Max.
                     Max.
                                    Max.
                     gear
                                    carb
      am
               Min.
Min.
       :0.0000
                      :3.000
                               Min.
                                      :1.000
                1st Qu.:3.000
1st Qu.:0.0000
                               1st Qu.:2.000
Median :0.0000 Median :4.000
                              Median :2.000
     :0.4062 Mean
                     :3.688 Mean :2.812
3rd Qu.:1.0000
                3rd Qu.:4.000
                               3rd Qu.:4.000
      :1.0000
                Max. :5.000
                               Max. :8.000
Max.
> str(mtcars)
'data.frame': 32 obs. of 11 variables:
$ mpg : num 21 21 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 ...
$ cyl : num 6646868446...
$ disp: num 160 160 108 258 360 ...
$ hp : num 110 110 93 110 175 105 245 62 95 123 ...
$ drat: num 3.9 3.9 3.85 3.08 3.15 2.76 3.21 3.69 3.92 3.92 ...
$ wt : num 2.62 2.88 2.32 3.21 3.44 ...
$ qsec: num 16.5 17 18.6 19.4 17 ...
$ vs : num 0 0 1 1 0 1 0 1 1 1 ...
\mbox{$\$$ am : num $111000000...}
$ gear: num 4 4 4 3 3 3 3 4 4 4 ...
$ carb: num 4 4 1 1 2 1 4 2 2 4 ...
```

Confidence interval with a confidence interval of 0.95 for the difference of the means corresponding to the fuel consumption variables for the manual and automatic car

```
> t.test( mpg ~ am, data = mtcars,conf.level = 0.95)

Welch Two Sample t-test

data: mpg by am
t = -3.7671, df = 18.332, p-value = 0.001374
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
-11.280194 -3.209684
sample estimates:
mean in group 0 mean in group 1
17.14737 24.39231
```

From the above code it appears that the confidence interval is between -11.280194 and -3.209684.

Exercise 4

Consider the **OctopusF.txt** dataset. Read the data, calculate the descriptive measures of the sample (mean, standard deviation). Plot the histogram. Check the normalization of the data and build the confidence interval.

Solution

We read the OctopusF.txt data file with the command:

```
> df <- read.delim("OctopusF.txt")</pre>
```

Descriptive Statistics of data:

Finding the mean value.

```
> summary(df$Weight)
  Min. 1st Qu. Median Mean 3rd Qu. Max.
  40.0 300.0 545.0 639.6 800.0 2400.0
```

According to the above results, the mean value is 639.6.

To find the standard deviation, we need to install the **pastecs** library. Then with the **stat.desc()** command I find the standard deviation.

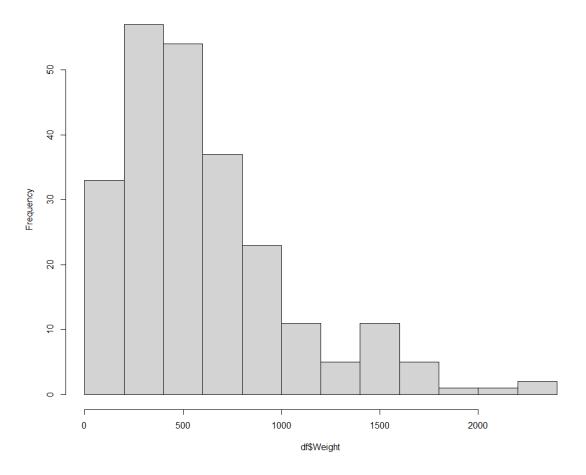
```
library(pastecs)
 stat.desc(df$weight)
                 nbr.null
                                                 min
     nbr.val
                                nbr.na
                       median
                                                 SE.mean
                                      mean
             sum
2.400000e+02 0.000000e+00 0.000000e+00 4.000000e+01 2.400000e+03 2.360000e
+03 1.535100e+05 5.450000e+02 6.396250e+02 2.878250e+01
CI.mean.0.95
                                            coef.var
                      var
5.669977e+01 1.988237e+05 4.458965e+02 6.971218e-01
```

According to the above results, the standard deviation is $4.458965e^{+02}$.

To build the histogram, I execute the code command:

> hist(df\$weight)

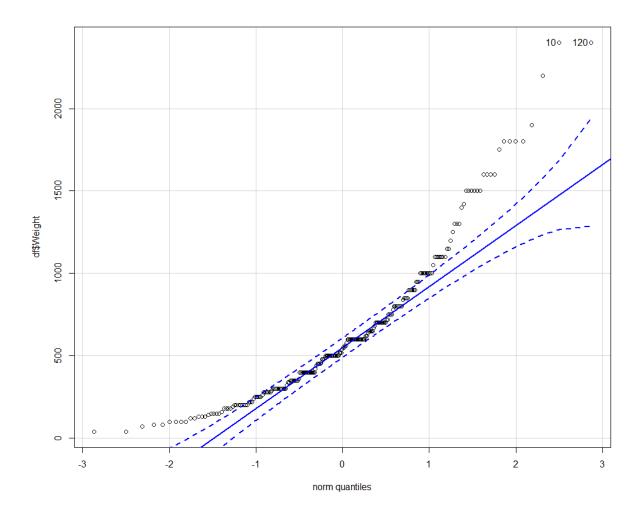
Histogram of df\$Weight



The distribution is oblique to the right and there are no outliers.

To check the normality of the data, we run the $\tt qqPlot$ command in the "car" library.

```
> library("car")
> qqPlot(df$weight)
[1] 10 120
```



From the above graph it appears that the distribution of the "balance" variable does not follow a normal distribution with a very large deviation in the queues.

Calculation of Confidence Interval

The 95% confidence interval is in the points [582.9252,696.3248]

Exercise 5

load the MASS library. in the survey data file, the smoke column shows the degree of smoking of the students, while the Exer column indicates their level of physical activity. Smoking levels are "Heavy", "regul", "Occas" "Never". For the Exer variable these are "Freq", "Some", "None". Examine how much smoking affects physical activity Hint: Contigency table and chi² test

Solution

Contingency Table

```
> contigency_table = table(df$Smoke, df$Exer)
> contigency_table
```

```
Freq None Some
                 1
                      3
  Heavy
          87
                18
                     84
  Never
                 3
          12
                      4
  Regul
           9
                 1
  chisq.test(contigency_table)
        Pearson's Chi-squared test
       contigency_table
X-squared = 5.4885, df = 6, p-value = 0.4828
```

The degree of smoking does not affect physical exercise since the above p-value is greater than 0.05 (p-value>0.05).

Exercise 6

Our data is stored as Concrete_Data.xls. and refer to variables that affect the durability of cement. The durability of cement is a non-linear function of age variables and various components such as blast furnace slag, fly ash, water, super-plasticizer, coarse aggregate. The first 8 are independent quantitative while Concretre compressive strength is the dependent. Use some packages to train the neural network e.g., neuralnet, nnet, RSNNS.

Read the data. Then you standardize your data. Then create the training and test sets. Train your model, plot the neuron and evaluate it. (use the compute() function and see if it works differently and why from the predict() function. See what the cor() function does. Improve your model if you become and see how your model behaves if the number of hidden nodes increases

Solution

#Neural Network
library(neuralnet)

threshold=0.5)
nn\$result.matrix

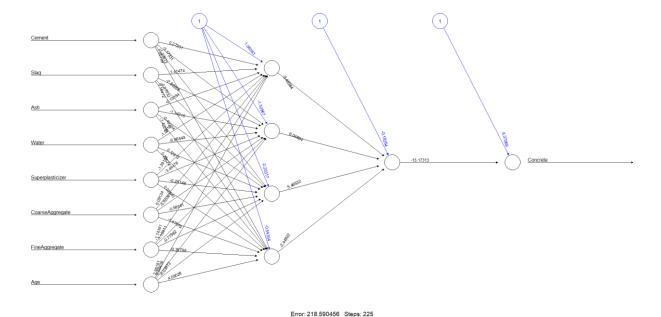
plot(nn)

The Concrete_Data.xls data file refers to variables that affect the strength of the cement. With the str() command we read all our data.

```
str(df)
tibble [1,030 x 9] (S3: tbl_df/tbl/data.frame)
                 : num [1:1030] 540 540 332 332 199 ...
$ Cement
$ Slag
                 : num [1:1030] 0 0 142 142 132 ...
$ Ash
                 : num [1:1030] 0 0 0 0 0 0 0 0 0 0 ...
                  : num [1:1030] 162 162 228 228 192 228 228 228 228 228
$ Water
$ Superplasticizer: num [1:1030] 2.5 2.5 0 0 0 0 0 0 0 0 ...
$ CoarseAggregate : num [1:1030] 1040 1055 932 932 978 ...
                  : num [1:1030] 676 676 594 594 826 ...
$ FineAggregate
                  : num [1:1030] 28 28 270 365 360 90 365 28 28 28 ...
$ Age
                 : num [1:1030] 80 61.9 40.3 41.1 44.3 ...
$ Concrete
We notice that this file consists of 1030 rows and 9 columns.
We split the data file into 70% train set(trainset <-
df[1:721, ]) and 30% test set(testset <- df[722:1030, ]
). Then we install the "neuralnet" library, to create a neural
network, to train it and then to visualize it. The
compute(), predict() and cor() functions were used.
library("readxl")
# xls files
df <- read excel("Concrete Data.xls")</pre>
str(df)
df <-scaleddata<-scale(df)</pre>
# Training and Test Data
set.seed(653)
df <- df[sample(nrow(df)), ]</pre>
trainset <- df[1:721, ]</pre>
testset <- df[722:1030, ]
```

nn <- neuralnet(Concrete ~ Cement + Slag + Ash + Water +
Superplasticizer + CoarseAggregate + FineAggregate + Age,</pre>

data=trainset, hidden=c(4,1), linear.output=FALSE,



```
#Test the resulting output
temp_test <- subset(testset, select = c("Cement", "Slag",
"Ash", "Water", "Superplasticizer", "CoarseAggregate",
"FineAggregate", "Age"))
head(temp_test)
nn.results <- compute( nn, temp_test )
results <- data.frame( actual = testset$Concrete, prediction =
nn.results$net.result )
roundedresults<-sapply(results,round,digits=0)
roundedresultsdf=data.frame(roundedresults)
attach(roundedresultsdf)
table(actual,prediction)</pre>
```

Above we present the optimal model. If the number of hidden nodes increases more (hidden = c (4,1)) then the error of the control set increases.

Exercise 7

Consider the **faithful** data set and estimate the next explosion if the expected time from the last explosion is 80 minutes. Find the R-Squared coefficient and the linear regression line. Check if there is a statistically significant relationship between the two variables in the linear regression model for the two variables of your data with significance level a = 0.05. Build a 95% Confidence Interval for the "eruption duration" variable for a given waiting time 80 min. Build a 95% Confidence prediction of the "eruption duration" variable given standby time 80 min. In addition to make the residual diagram of the linear regression against the

"waiting" variable. Make the diagram of the regularity for the standard residuals of the linear regression

Solution

The faithful.txt data file contains 2 columns, which are the volcanic eruptions and the corresponding standby time. With the str() command we read all our data.

```
> str(df)
'data.frame': 272 obs. of 2 variables:
$ eruptions: num 3.6 1.8 3.33 2.28 4.53 ...
$ waiting : num 79 54 74 62 85 55 88 85 51 85 ...
```

According to the above command, we observe that the specific file consists of 272 rows and 2 columns.

```
reg.lm <- lm(eruptions ~ waiting, data = df)</pre>
> summary(reg.lm)
lm(formula = eruptions ~ waiting, data = df)
Residuals:
     Min
               10
                   Median
                                         Max
-1.29917 -0.37689 0.03508 0.34909 1.19329
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
                        0.160143 -11.70
                                           <2e-16 ***
                        0.002219
                                   34.09
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.4965 on 270 degrees of freedom
 Multiple R-squared: 0.8115, Adjusted R-squared: 0.8108
F-statistic: 1162 on 1 and 270 DF, p-value: < 2.2e-16
```

The regression R-Squared coefficient is 0.81 and the line of regression y: eruptions = -1.87 + 0.0756*waiting

For waiting=80 the next crisis is estimated at 4.17622

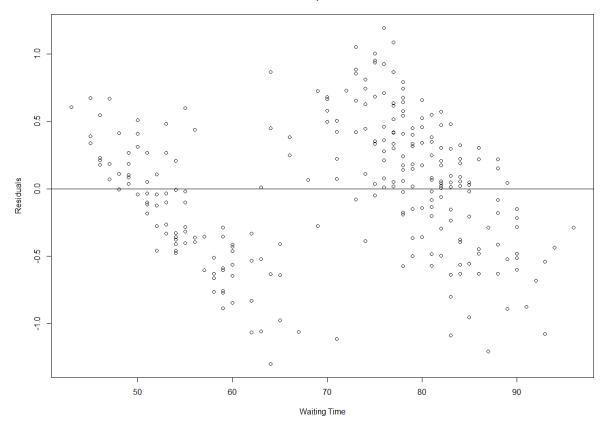
The p-value of the t-test for the coefficient of the variable waiting is $<2e^{-16}$ *** <0.05 and therefore there is a statistically significant relationship between the two variables in the linear regression model for the two variables of your data with a significance level a=0.05

The 95% Confidence Interval for the eruption duration variable for a given waiting time of 80 min is 4.104848 4.247592. A 95% Prediction Interval of the eruption duration variable given a waiting time of 80 min is 3.196089 5.156351.

```
> eruption.res = resid(reg.lm)
> plot(df$waiting, eruption.res, ylab="Residuals", xlab="Waiting Time", ma
in="Eruptions")
> abline(0, 0)
```

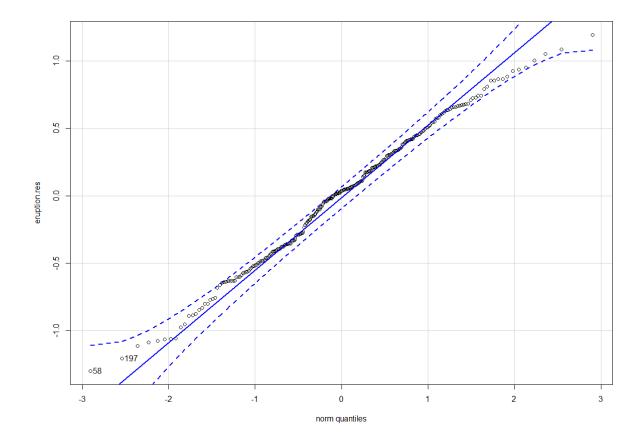
Residual diagram of linear regression versus waiting variable





Normality diagram for standard regression Residuals

```
> library("car")
> qqPlot(eruption.res)
[1] 58 197
```



Exercise 8

Consider the **stackloss** data and estimate the stack loss value if the airflow value =72, the water temperature value =20 and the air concentration value =85. Find the R-Squared coefficient for the multiple linear model. Examine the significance of the model in our data with significance level a = 0.05. Do an 95% Confidence Interval for the mean of the dependent variable when we have values for the variables air flow =72, water temperature =20 and acid concentration =85, also to do 95% Prediction Interval for the dependent variable when we have values for the variable air flow =72, water temperature =20 and acid concentration =85

Solution

We import the stackloss data file via the MASS library.

```
> library(MASS)
> data(stackloss)
> str(stackloss)
'data.frame': 21 obs. of 4 variables:
   $ Air.Flow : num  80  80  75  62  62  62  62  62  58  58 ...
   $ Water.Temp: num  27  27  25  24  22  23  24  24  23  18 ...
   $ Acid.Conc.: num  89  88  90  87  87  87  93  93  87  80 ...
   $ stack.loss: num  42  37  37  28  18  18  19  20  15  14 ...
```

Through the str() command we notice that this data set contains 21 rows and 4 columns.

```
> stackloss.lm <- lm(stack.loss ~ Air.Flow + Water.Temp + Acid.Conc., data</pre>
= stackloss)
> summary(stackloss.lm)
Call:
lm(formula = stack.loss ~ Air.Flow + Water.Temp + Acid.Conc.,
    data = stackloss)
Residuals:
             1Q Median
    Min
                            3Q
                                    Max
<del>-7.2377 -1.7117 -0.4551 2.3614 5.6978</del>
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
                        11.8960 -3.356 0.00375 **
(Intercept) -39.9197
                        0.1349 5.307 5.8e-05 ***
Air.Flow
             0.7156
Water.Temp
             1.2953
                         0.3680 3.520 0.00263 **
                         0.1563 -0.973 0.34405
Acid.Conc.
             -0.1521
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 3.243 on 17 degrees of freedom
 ultiple R-squared: 0.9136, Adjusted R-squared: 0.8983
```

The R-Squared for the multiple linear model is: R-squared: 0.9136.

The significance of the model in our data with significance level a=0.05 is strong since the p-value of the total F-test is **p-value**: $3.016e^{-09}$.

The value of stack loss if the value of airflow=72 and the value of water temperature=20 and the value of air concentration=85 is 24.58173

.

95% of Confidence Interval for the mean of the dependent variable when we have values for the variables air flow=72, water temperature=20 and acid concentration=85: $20.218\ 28.945$

```
> predict(stackloss.lm, newdata = new_data, interval = 'prediction')
    fit lwr upr
1 24.58173 16.4661 32.69736
```

95% of Confidence Interval forecast for the dependent variable when we have values for the variables air flow=72, water temperature=20 and acid concentration=85:

16.466 32.69736

Exercise 9

The sales representative of a product is not satisfied with the sales of the product in his area of responsibility. He finds that the products sold differ from store to store in a price range of 921 to 2604 pieces with an mean price of 1846.8. He wants to know what the reason for this difference is. For that, he randomly selects 37 stores of the same size, observing the sales of the product, the price of the product, the sales costs and the number of arrivals in these stores for a certain time period. The following research should answer the question of whether the sales of product sets are affected by the other sizes chosen.

Examine if

- i. Your model is statistically significant
- ii. If the sizes are statistically significant
- iii. If there is interdependence between the sizes
- iv. Calculate the standardized residuals and find the lowest and highest standardized residual
- v. Examine the distribution of the residuals
- vi. Write the prediction for sales. Where are the best predictions made?
- vii. Write the theory of homoscedasticity and test if there are such in your model

Solution

We read the xls data file through the readxl library.

```
> library("readxl")
> # xls files
> df <- read_xlsx("market.xlsx")
> market.lm <- lm(Sales ~ Preis + Costs + Arrivals, data = df)
> summary(market.lm)

Call:
lm(formula = Sales ~ Preis + Costs + Arrivals, data = df)

Residuals:
```

```
1Q Median
                            30
-261.04 -127.20 -38.65 144.85 229.20
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 730.01652 225.03056 3.244 0.0027 **
                      16.17993 -2.602 0.0138 *
Preis
                       0.05069 10.891 1.83e-12 ***
Costs
Arrivals
                        1.66599 5.792 1.78e-06 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 156.1 on 33 degrees of freedom
Multiple R-squared: 0.8447, Adjusted R-squared: 0.8306
F-statistic: 59.83 on 3 and 33 DF, p-value: 1.953e-13
```

١)

The model is statistically significant since the p-value of the total F-test is <0.05.

F-statistic: 59.83 on 3 and 33 DF, p-value: 1.953e-13

The p-value of the t-test for the coefficient of the «Preis», «Cost», «Arrivals» variable is 0.0138 * < 0.05, 1.83 $^{\rm e-12}$ *** < 0.05 and 1.78 $^{\rm e-06}$ *** < 0.05 respectively, and therefore there is a statistically significant relationship between the two variables in the linear regression model for the two variables

of your data with significance level a=0.05

III)

From the above correlation coefficients we conclude that there is no interdependence between the quantities since the coefficients are very small.

```
> # x-correlation

> cor(df[,2:4])

Preis Costs Arrivals

Preis 1.00000000 0.01400399 0.04289388

Costs 0.01400399 1.00000000 0.14847016

Arrivals 0.04289388 0.14847016 1.00000000
```

```
Residuals:
    Min
            1Q Median
                            3Q
                                   Max
-285.36 -118.59 -26.14 130.36 220.76
Coefficients:
                Estimate Std. Error t value Pr(>|t|)
(Intercept)
              -1.992e+02 1.301e+03 -0.153
                                               0.879
Preis
               7.139e+01 1.081e+02
                                      0.660
                                               0.514
Costs
               2.353e-01 4.712e-01
                                    0.499
                                              0.621
Arrivals
               2.134e+01 1.341e+01
                                     1.592
                                              0.122
Preis:Costs
               1.059e-02 3.137e-02
                                     0.338
Preis:Arrivals -1.413e+00 1.144e+00 -1.235
                                      0.677
Costs:Arrivals 2.462e-03 3.637e-03
Residual standard error: 158.4 on 30 degrees of freedom
Multiple R-squared: 0.8546, Adjusted R-squared: 0.8256
F-statistic: 29.4 on 6 and 30 DF, p-value: 2.771e-11
```

There is no interaction between the values since the p-values of the following t-tests are >0.05.

```
Preis:Costs 1.059e-02 3.137e-02 0.338 0.738

Preis:Arrivals -1.413e+00 1.144e+00 -1.235 0.226

Costs:Arrivals 2.462e-03 3.637e-03 0.677 0.504
```

IV)

Find the standardized residuals with the rstandard()
command.).

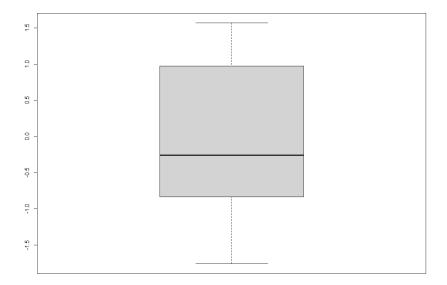
```
> # Standardized Residuals
> market.stdres = rstandard(market.lm)
> summary(market.stdres)
    Min. 1st Qu. Median Mean 3rd Qu. Max.
-1.759975 -0.836211 -0.261024 -0.001757 0.976235 1.570400
```

According to the results of the above code, the smallest and largest standardized residual amounts to -1.759975 and 1.5704 respectively.

V)

To examine the distribution of the residuals, we apply the following code command to visualize our data.

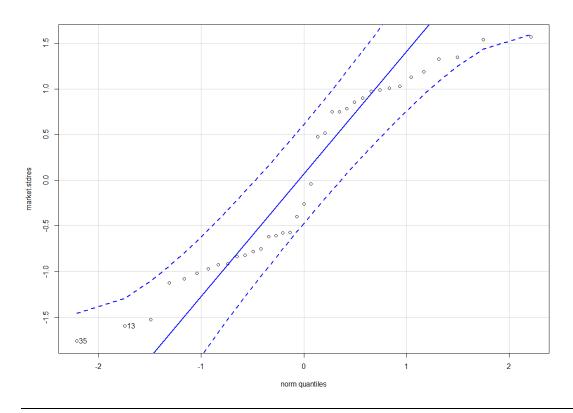
> boxplot(market.stdres, data=df)

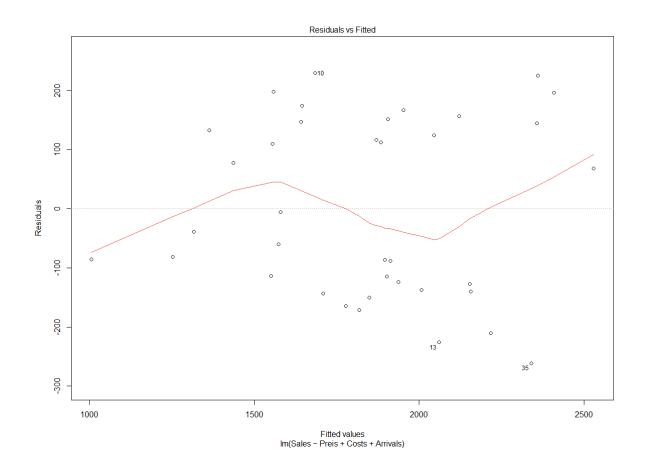


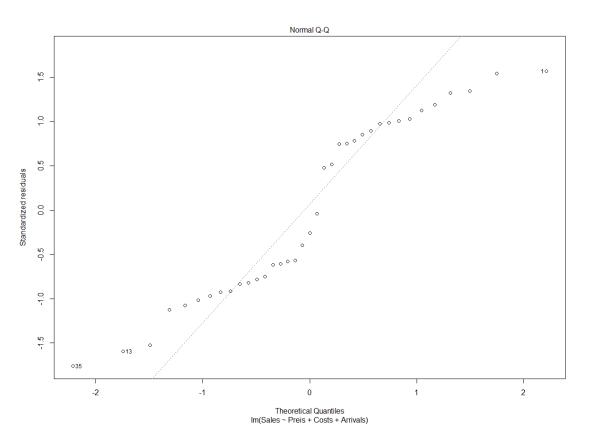
According to the above pictogram, the distribution is oblique to the right and there are no outliers.

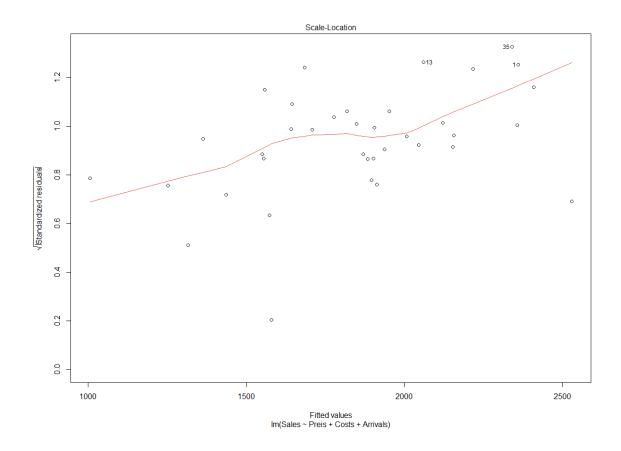
```
> qqPlot(market.stdres)
[1] 35 13
> plot(market.lm)
Hit <Return> to see next plot:
```

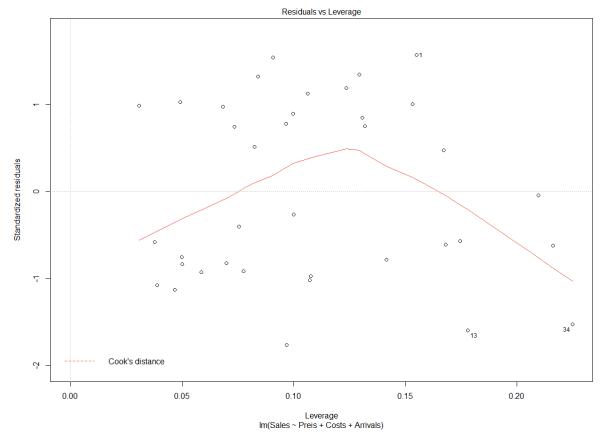
Pressing the Enter button shows the following relevant results.











VI)

The forecast for sales is as follows: Sales=730-42.09*Preis + 0.55*Costs + 9.65*Arrivals

The best predictions are made in the observations with the smallest residuals.

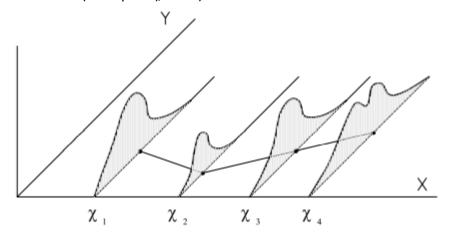
The most important variable is "costs", then "Arrivals" and finally "Preis" based on t-test values.

VII)

Based on the Breusch-Pagan test p-value which is <0.05, there is heteroscedasticity.

Conditions-assumptions for the application of the Simple Linear Model Y = α + β . X + ϵ

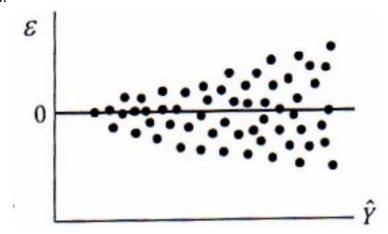
The general assumption we make for a regression model (linear or not) is that the variable X is measured without error and that Y, for every level i x of X, is a random variable with finite mean and scatter ($\Pi\alpha$ váρετος, 2003).



For the simple linear model we also make the following assumptions:

- 1. Linearity.
- 2. Homoscedasticity Variance Stability.
- 3. Independence.
- 4. Normality.

A first check of the stability or non-dispersion of Y (or e) for the various levels of X can be made with the dispersion diagram and the rest diagrams. If, for example, the residual diagram is in the form of a trapezoid (open fan), as follows, the most probable cause of this disturbance7 is the instability of the scattering of random errors e. X or Y gives diagrams of trapezoidal remainders (increasing by X or Y, increases by 2 σ or vice versa). This is because such applications follow multiplication models where 2 2 2 σ Y = [E (Y)] $\cdot \sigma$ and 2 σ the scatter of errors ε (why?) 8. Also, corresponding balance diagrams give variables that measure the number of events in the unit of time, space, length, etc., ie variables that follow a Poisson distribution.



If the rest diagrams suggest that we do not have constant dispersions, we can statistically check whether there is a significant difference in the dispersions or not if we have more than one observation for the different levels of X. We can also classify the observations in ascending order of X, divide them into two or more groups, and statistically check whether

the groups have a significant difference in dispersions or not. When dispersion instability is detected we can, in several cases, address the problem with appropriate transformations in the variables.

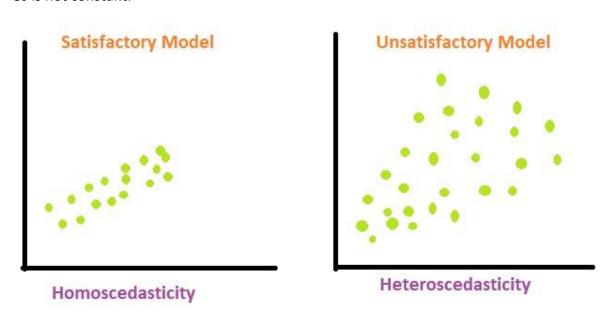
One of the basic assumptions of the classical linear model is that the perturbation term εt (of the population) is a random variable having mean $\mathbf{E}(\varepsilon t) = \mathbf{0}$ and constant variance for all values of the dependent variable $\mathbf{Y}t$. When the variance of the disturbing term is constant, then the pattern is characterized by homoskedasticity:

Var $(\varepsilon t) = \sigma \varepsilon 2 = \text{constant}$, for t = 1,..., T

Otherwise, when the variance of the disturbing term is not constant, then there is heteroskedasticity in the model:

Var
$$(\varepsilon t) = \sigma t 2$$
, for $t = 1,..., T$

where all the fluctuations σt . are not equal to each other, so we say that there is heterosexuality in the disturbing terms. Heteroseedasticity refers to the case where in different observations of the independent variable Xt, the variance of the disturbing term εt is not constant.



Consequences of heteroscedasticity

Suppose the model $\Upsilon t = \beta 0 + \beta 1Xt + ut$ and assume that all the basic assumptions of the classical linear model are valid, except homoscedasticity (Stock & Watson, 2017), (Xp $\dot{\eta}$ $\sigma\tau o\nu$, 2007). That is, we assume that: $Var(\varepsilon t) = 22$, for t = 1,..., T.

The estimators of the coefficients of the above model, which result from the least squares method, when the disturbing term is heterosexual, are still linear and unbiased. The problem that arises is mainly related to the estimates of their fluctuations and their effectiveness.

That is, least squares estimators do not have the slightest variation (usually fluctuations are underestimated). Due to the underestimation of the fluctuations, higher values of the statistics t and F are estimated.

- Confidence Intervals are unreliable and model predictions are ineffective.
- Our conclusions about the parameters of the population will be unreliable.

• Appraisers, however, remain impartial and consistent. This is because none of the interpretive variables is associated with the error term. Thus, the values of the estimated coefficients will be very close to the actual parameters.

Ways to determine heteroscedasticity

There is a large number of tests to determine the problem of heteroscedasticity, depending on the available statistics. If for each value of the interpretive variable there are several observations for the dependent variable, or if the sample size is large enough to be divided into groups, the heterosexuality test can be done with the standard homogeneity test. Many tests are based on the analysis of residues resulting from the least squares method. Some basic heteroscedasticity tests are as follows:

- a. Barlett criterion.
- b. Spearman correlation coefficient.
- c. Goldfeld-Quandt control.
- d. Breusch-Pagan-Godfrey control.
- e. White control.

Exercise 10

Consider the insurance.csv data. Our purpose is to study how these variables affect expenses

Do:

- i. Reading the data
- ii. Control of variables (use the "psych" package)
- iii. Create the appropriate model to answer the above question

Solution

1)

We read the insurance.csv file with the command

```
> df = read.csv("insurance.csv", sep = ',')
```

Then with the str() command we observe the data file data.

```
data.frame':
             1338 obs. of 7 variables:
                19 18 28 33 32 31 46 37 37 60 ...
          : int
$ age
                "female" "male" "male" ...
$ sex
          : chr
                27.9 33.8 33 22.7 28.9 ...
          : num
$ children: int
                0 1 3 0 0 0 1 3 2 0 ...
                "yes" "no" "no" "no"
$ smoker
          : chr
                "southwest" "southeast" "southeast" "northwest"
          : chr
 charges : num 16885 1726 4449 21984 3867
```

This data set consists of 1338 rows and 7 column.

```
> df$sex = as.factor(df$sex)
> df$sex
Levels: female male
```

With the above command it shows me in total how many different types of sexes there are in this column.

```
> df$smoker = as.factor(df$smoker)
> df$smoker
```

Levels: no yes

With the above command it shows me if there are smokers in the specific column.

```
> df$region = as.factor(df$region)
> df$region
```

Levels: northeast northwest southeast southwest

```
library(psych)
>library(psychTools) #additional tools and data are here
> describe(df) #basic descriptive statistics
                                 sd median trimmed
                                                                 min
         vars
                n
                      mean
                                                         mad
       range skew kurtosis
max
                                se
            1 \ 1338
                              14.05
                                      39.00
                                                39.01
                                                       17.79
                                                               18.00
age
                      39.21
4.00
        46.00 0.06
                      -1.25
                              0.38
                                       2.00
sex
            2 1338
                       1.51
                               0.50
                                                1.51
                                                        0.00
                                                                1.00
2.00
         1.00 -0.02
                       -2.00
                              0.01
bmi
            3 1338
                      30.66
                               6.10
                                      30.40
                                               30.50
                                                        6.20
                                                               15.96
3.13
        37.17 0.28
                      -0.06
                              0.17
children
           4 1338
                       1.09
                               1.21
                                       1.00
                                                0.94
                                                        1.48
                                                                0.00
5.00
         5.00 0.94
                       0.19
                              0.03
                               0.40
            5 1338
smoker
                       1.20
                                       1.00
                                                1.13
                                                        0.00
                                                                1.00
         1.00 1.46
                       0.14
2.00
                              0.01
region
            6 1338
                               1.10
                                        3.00
                                                2.52
                                                        1.48
                       2.52
                                                                1.00
4.00
         3.00 -0.04
                       -1.33
                              0.03
            7 1338 13270.42 12110.01 9382.03 11076.02 7440.81 1121.87 6377
0.43 62648.55 1.51 1.59 331.07
```

 Π

```
> corr.test(df)
Call:corr.test(x = df)
Correlation matrix
                sex bmi children smoker region charges
age
          1.00 -0.02 0.11
                              0.04
                                    -0.03
                                            0.00
                                                    0.30
         -0.02 \quad 1.00 \quad 0.05
                                     0.08
                                            0.00
                                                    0.06
sex
                              0.02
bmi
          0.11 0.05 1.00
                              0.01
                                     0.00
                                            0.16
                                                    0.20
children 0.04 0.02 0.01
                                     0.01
                              1.00
                                            0.02
                                                    0.07
                                                    0.79
         -0.03 0.08 0.00
                              0.01
                                     1.00
                                            0.00
smoker
region
          0.00 0.00 0.16
                              0.02
                                     0.00
                                            1.00
                                                   -0.01
                                     0.79 - 0.01
         0.30 0.06 0.20
                              0.07
                                                    1.00
charges
Sample Size
Γ17 1338
Probability values (Entries above the diagonal are adjusted for multiple t
ests.)
          age sex bmi children smoker region charges
         0.00 1.00 0.00
                           1.00 1.00 1.00
                                                 0.00
```

```
0.08
                                          1.00
sex
         0.45 0.00 1.00
                            1.00
                                                  0.51
         0.00 0.09 0.00
                            1.00
                                   1.00
                                          0.00
                                                  0.00
bmi
children 0.12 0.53 0.64
                            0.00
                                   1.00
                                          1.00
                                                  0.19
         0.36 0.01 0.89
                            0.78
                                   0.00
                                          1.00
                                                  0.00
smoker
region
         0.94 0.87 0.00
                                   0.94
                            0.54
                                          0.00
                                                  1.00
```

From the p-values of the tests for the correlation coefficients, we see that all the variables are significantly correlated with the expenses except the "region". In the regression model, however, all variables are statistically significant, which is shown in question III.

|||)

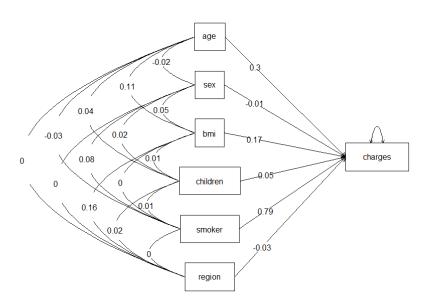
```
> setCor(y = 7,x=1:6, data = df)
Call: setCor(y = 7, x = 1:6, data = df)
Multiple Regression from raw data
DV = charges
                             p lower.ci upper.ci VIF
           slope
                   se
                        t
(Intercept) 0.00 0.01 0.00 1.0e+00
                                     -0.03
                                               0.03 1.00
            0.30 0.01 21.65 2.8e-89
                                               0.33 1.02
                                      0.27
           -0.01 0.01 -0.39 6.9e-01
                                     -0.03
                                               0.02 1.01
sex
           0.17 0.01 12.00 1.5e-31
bmi
                                     0.14
                                               0.19 1.04
children
           0.05 0.01 3.48 5.1e-04
                                      0.02
                                              0.07 1.00
            0.79 0.01 57.84 0.0e+00
                                               0.82 1.01
smoker
                                      0.77
           -0.03 0.01 -2.33 2.0e-02
                                     -0.06
                                              -0.01 1.03
region
Residual Standard Error = 0.5 with 1331 degrees of freedom
Multiple Regression
          R R2 Ruw R2uw Shrunken R2 SE of R2 overall F df1 df2 p
charges 0.87 0.75 0.57 0.32
                                         0.01
                                                 668.12
                                                          6 1331 0
                                 0.75
              R2 Ruw R2uw Shrunken R2 SE of R2 overall F df1 df2 p
charges 0.87 0.75 0.57 0.32 0.75 0.01 668.12 6 1331 0
```

The important variables that affect costs are reported in the following model:

Charges = 0.3*age - 0.01*sex + 0.17*bmi + 0.05 *children + 0.79*smoker - 0.03*region

, as shown in the diagram below.

Regression Models



Exercise 11

MF is an electronics company. If the company has a good quality assurance system of its products there are cases of return. During its operation it created a database. In the first column there are the compensations for each return, in the second the shifts construction of the goods, in the third the types of complaints and in the fourth the part of production. The company's quality manager studied a random sample of 110 returns (mf.xls)

- Present the data with contingency tables looking at the sizes in pairs (compensation for the rest as well as type of complaints against a shift or place of production).
 Comment on the data.
- ii. The person in charge wants to give an answer to his suspicion that there is a relationship between the types of complaints and the place of production. Calculate the expected values in each cell. Indicate a way to have an expected value =5 in each cell. Is the suspect's suspicion valid at a significance level of 0.01?
- iii. The sales representative wants to know if there is a difference in the compensation between production sites (Boise and Salt Lake City). Check it at significance level a = 0.02

Solution

> library(readx1) > # xls files > df <- read_excel("mf.xls")

```
> # I)
> df$amount_cut = cut(df$`Dollar Claim Amount`,3)
1)
With the table() command calculates the Contigency tables of
the following variables of each category.
> tb1 = table(df$amount_cut, df$Shift)
> tb1
            1 2 3
 (146,228] 15 8 0
 (228,311] 41 16 3
 (311,393] 19 6 2
> chi2_1 = chisq.test(tb1)
> chi2_1$p.value
[1] 0.6727148
  tb2 = table(df$amount_cut, df$`Complaint Code`)
> tb2
            1 2 3 4
 (146,228] 7 8 5 3
 (228,311] 20 23 13 4
 (311,393] 8 14 5 0
> chi2_2 = chisq.test(tb2)
> chi2_2$p.value
[1] 0.5915626
tb3 = table(df$amount_cut, df$`Manufacturing Plant`)
> tb3
            1 2 3
 (146,228] 18 5 0
  (228,311] 43 11 6
  (311,393] 17 8 2
> chi2_3 = chisq.test(tb3)
chi2_3$p.value
[1] 0.4342091
 tb4 = table(df$`Complaint Code`, df$Shift)
> tb4
    1 2 3
 1 23 11
          1
 2 32 12 1
 3 16 4 3
 4 4 3 0
> chi2_4 = chisq.test(tb4)
> chi2_4$p.value
[1] 0.3574079
```

```
> tb5 = table(df$`Complaint Code`, df$`Manufacturing Plant`)
```

```
> tb5

    1 2 3
    1 30 3 2
    2 31 11 3
    3 13 8 2
    4 4 2 1
> chi2_5 = chisq.test(tb5)
> chi2_5$p.value
[1] 0.2755304
```

II)

Based on the following π -value of the chi2-test (π -value = 0.2755> 0.05) there is no relationship between the types of complaints and the place of production.

Expected values:

In the Complaint Code variable, I apply merge in groups 3 & 4 and in the Manufacturing Plant variable I apply merge in groups 2 & 3

To have expected values $\!\!\!> 5$, we join rows of columns with low frequencies to achieve this goal.

|||)

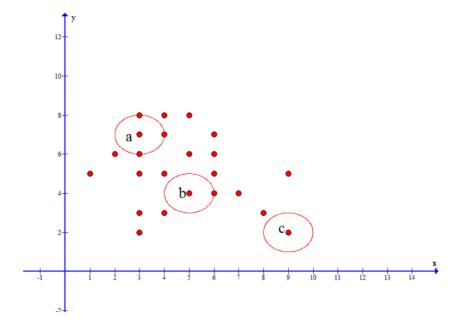
```
sample estimates:
mean in group 1 mean in group 2
268.4359 277.3333
```

We apply Two Sample t-test and based on the p-value=0.53 > 0.02 we find that there is no difference in the amount of compensation between the production sites (Boise and Salt Lake City) with a level of significance a=0.02

Exercise 12

Apply the DBSCAN algorithm with ϵ = 1 and MinPts = 3. To which category do points a, b, c belong?

Apply K-means and find the best possible number of k clusters



Solution

#question a

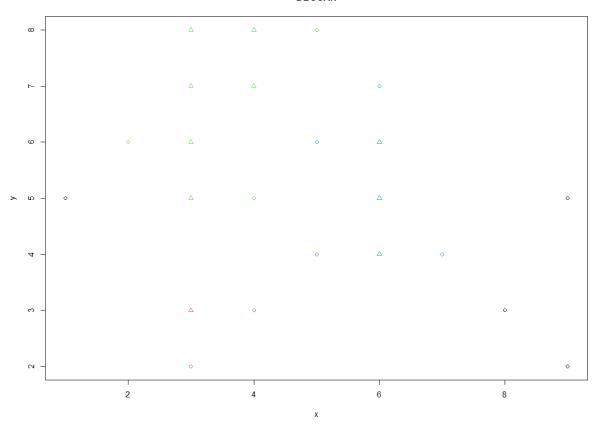
Point ${\bf a}$ is a central point, because in its neighborhood there are 3 points. Point ${\bf b}$ has in its neighborhood 1 point which is accessible from the point with coordinates (6,4). Finally, point ${\bf c}$ is extreme since there is no other point in its neighborhood.

#question b

```
> library("fpc")
> library("dbscan")
> x <- c(1, 2, 3, 3, 3, 3, 3, 4, 4, 4, 4, 5, 5, 5, 6, 6, 6, 6, 7, 8, 9,
9)
> y <- c(5, 6, 2, 3, 5, 6, 7, 8, 3, 5, 7, 8, 4, 6, 8, 4, 5, 6, 7, 4, 3, 2,
5)</pre>
```

```
> data <- data.frame(x=x, y=y)
> db <- fpc::dbscan(data , eps = 1, MinPts = 3)
> plot(db, data , main = "DBSCAN")
```

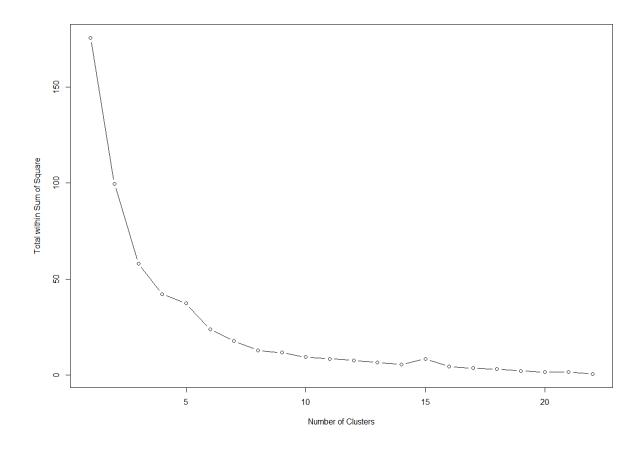
DBSCAN



#question c

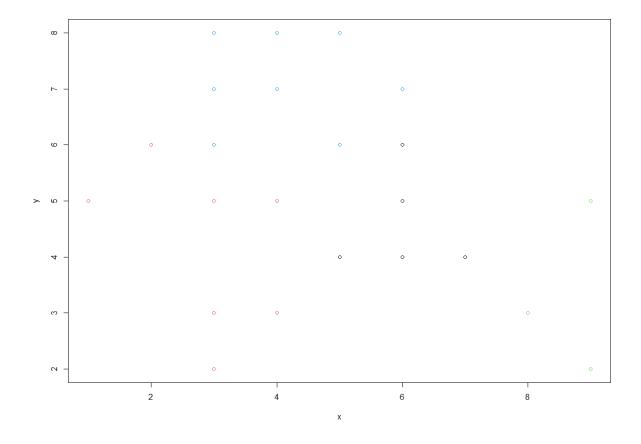
We will try with the elbow rule to find the ideal number of clusters

```
> plot_fun <- function(data, nc){
+  wss <- (nrow(data)-1) * sum(apply(data,2,var))
+  for(i in 2:nc){wss[i] <- sum(kmeans(data,centers=i)$withinss)}
+  plot(1:nc, wss, type = "b" ,xlab="Number of Clusters",ylab="Total with in Sum of Square")}
> plot_fun(data, nrow(data)-1)
```



Where the elbow bends is the best number for k, that is where k = 4 will come out

```
> kc <- kmeans(data, 4)
> plot(data, col=kc$cluster)
```



we take out the same clusters with kmeans

Exercise 13

The table is given:

	Х	Υ
1	0.4005	0.5306
2	0.2148	0.3854
3	0.3457	0.3156
4	0.2652	0.1875
5	0.0789	0.4139
6	0.4548	0.3022

Find the dendrogram and the exact values of the distances at which the corresponding clusters are created during the cumulative hierarchical clustering, such as resulting from the application of Euclidean distance in combination with its technique: a) single link, and b) full link

Solution

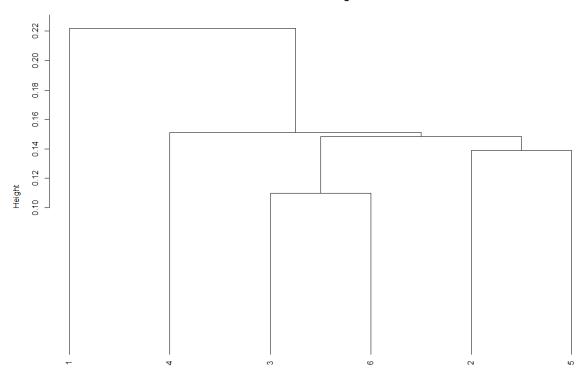
First we make the table for Euclidean distance with the points \boldsymbol{x} and \boldsymbol{y} .

```
> x <- c(0.4005, 0.2148, 0.3457, 0.2652, 0.0789, 0.4548)
> y <- c(0.5306, 0.3854, 0.3156, 0.1875, 0.4139, 0.3022)
```

a)

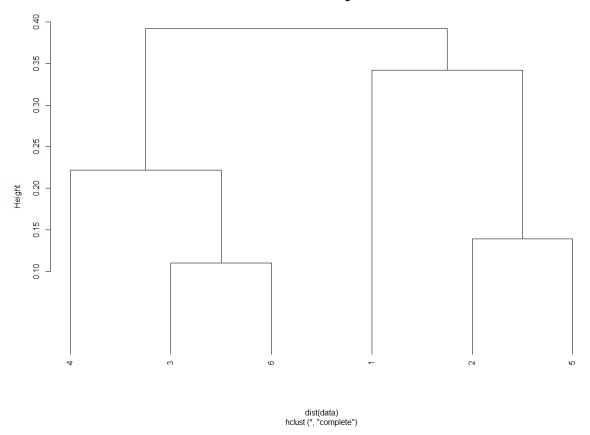
```
> hc <- hclust(dist(data ), method = "single" )
> plot(hc,hang = -1)
```

Cluster Dendrogram



dist(data) hclust (*, "single") b)





Bibliography

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Appendix of R codes

```
setwd('C:/Users/Giorgos/Desktop/ergasies metaptxiakwn/ergasia
filippaki (predictive
analytics)/ergasia examinou/ergasia mfilip 2021/ergasia mfilip
2021/dataset merous 1 kai 2')
# 1)
# install.packages("rpart")
library("rpart")
# Kyphosis
# a factor with levels absent present indicating if a kyphosis
(a type of deformation) was present after the operation.
# Age
# in months
# Number
# the number of vertebrae involved
# Start
# the number of the first (topmost) vertebra operated on.
df = kyphosis
summary(df)
# Boxplot of the variable NUMBER
boxplot(df$Number, main="The Variable: Number", ylab="The
number of vertebrae involved")
outliers = df$Number[df$Number>8]
outliers
which ( df$Number %in% outliers)
plot(df$Number, df$Age)
identify(df$Number, df$Age)
df = read.csv("capital.csv", sep = ';')
summary(df)
#df$gender <- as.factor(df$gender)</pre>
# 2i) πίνακας σχετικών συχνοτήτων
xtabs(balance ~ gender , data=df)
with(df, discretePlot(gender, scale="frequency"))
barplot( table(df$gender) )
prop.table(table(df$gender))
# Simple Pie Chart
bal gender <- c(173191, 52913)
lbls <- c("Male", "Female")</pre>
pie(bal gender, labels = lbls, main="Balance by gender")
```

```
# 2ii) Boxplot by Group
boxplot(balance ~ gender, data=df)
# 2iii)
library(psych)
describeBy(df$balance, df$gender)
summary(df$balance)
library(pastecs)
stat.desc(df$balance)
# 2iv)
library("car")
qqPlot(df$balance)
# 3)
data(mtcars)
head (mtcars)
summary(mtcars)
str(mtcars)
#df = read.csv("mtcars.csv", sep = ',')
t.test( mpg ~ am, data = mtcars,conf.level = 0.95)
# 4)
df <- read.delim("OctopusF.txt")</pre>
summary(df$Weight)
library(pastecs)
stat.desc(df$Weight)
hist(df$Weight)
library("car")
qqPlot(df$Weight)
# Calculate the mean and standard error
l.model <- lm(df$Weight ~ 1, df)</pre>
# Calculate the confidence interval
confint(l.model, level=0.95)
# 5)
library(MASS)
df = survey
contigency table = table(df$Smoke, df$Exer)
contigency table
chisq.test(contigency table)
```

```
# 6)
# Loading
library("readxl")
# xls files
df <- read excel("Concrete Data.xls")</pre>
str(df)
df <-scaleddata<-scale(df)</pre>
# Training and Test Data
set.seed(653)
df <- df[sample(nrow(df)), ]</pre>
trainset <- df[1:721, ]</pre>
testset <- df[722:1030, ]
#Neural Network
library(neuralnet)
nn <- neuralnet(Concrete ~ Cement + Slag + Ash + Water +
Superplasticizer + CoarseAggregate + FineAggregate + Age,
data=trainset, hidden=c(4,1), linear.output=FALSE,
threshold=0.5)
nn$result.matrix
plot(nn)
#Test the resulting output
temp test <- subset(testset, select = c("Cement", "Slag",</pre>
"Ash", "Water", "Superplasticizer", "CoarseAggregate",
"FineAggregate", "Age"))
head(temp test)
nn.results <- compute( nn, temp test )</pre>
results <- data.frame( actual = testset$Concrete, prediction =
nn.results$net.result )
roundedresults<-sapply(results, round, digits=0)</pre>
roundedresultsdf=data.frame(roundedresults)
attach (roundedresultsdf)
table (actual, prediction)
# 7)
library(ggplot2)
df <- read.delim("faithfull.txt")</pre>
str(df)
summary(df$Weight)
reg.lm <- lm(eruptions ~ waiting, data = df)</pre>
summary(reg.lm)
x80.dat <- data.frame(waiting = 80)
predict(req.lm, newdata = x80.dat, interval = 'confidence')
predict(reg.lm, newdata = x80.dat, interval = 'prediction')
eruption.res = resid(reg.lm)
```

```
plot(df$waiting, eruption.res, ylab="Residuals", xlab="Waiting
Time", main="Eruptions")
abline (0, 0)
library("car")
qqPlot(eruption.res)
# 8)
library (MASS)
data(stackloss)
str(stackloss)
stackloss.lm <- lm(stack.loss ~ Air.Flow + Water.Temp +</pre>
Acid.Conc., data = stackloss)
summary(stackloss.lm)
new data = data.frame(Air.Flow=72, Water.Temp=20,
Acid.Conc.=85)
predict(stackloss.lm, new data)
predict(stackloss.lm, newdata = new data, interval =
'confidence')
predict(stackloss.lm, newdata = new data, interval =
'prediction')
# 9)
# Loading
library("readxl")
# xls files
df <- read xlsx("market.xlsx")</pre>
market.lm <- lm(Sales ~ Preis + Costs + Arrivals, data = df)</pre>
summary(market.lm)
# x-correlation
cor(df[,2:4])
# Interactions
market inter.lm <- lm(Sales ~ Preis + Costs + Arrivals +</pre>
Preis*Costs + Preis*Arrivals + Costs*Arrivals, data = df)
summary(market inter.lm)
# Standardized Residuals
market.stdres = rstandard(market.lm)
summary(market.stdres)
# Residuals
market.res = residuals(market.lm)
summary(market.res)
# Boxplot()
# 2ii) Boxplot by Group
boxplot(market.stdres, data=df)
# QQ-plot
gqPlot(market.stdres)
plot(market.lm)
```

```
lmtest::bptest(market.lm) # Breusch-Pagan test
# 10)
# I)
df = read.csv("insurance.csv", sep = ',')
df$sex = as.factor(df$sex)
df$smoker = as.factor(df$smoker)
df$region = as.factor(df$region)
df <- sapply(df, unclass)</pre>
# II)
library(psych)
library(psychTools) #additional tools and data are here
describe(df) #basic descriptive statistics
corr.test(df)
# III)
setCor(y = 7, x=1:6, data = df)
#11)
# Loading
library("readxl")
# xls files
df <- read excel("mf.xls")</pre>
# I)
df$amount cut = cut(df$`Dollar Claim Amount`,3)
tb1 = table(df$amount cut, df$Shift)
chi2 1 = chisq.test(tb1)
chi2 1$p.value
tb2 = table(df\amount cut, df\amount Code\)
chi2 2 = chisq.test(tb2)
chi2 2$p.value
tb3 = table(df$amount cut, df$`Manufacturing Plant`)
chi2 3 = chisq.test(tb3)
chi2 3$p.value
tb4 = table(df$`Complaint Code`, df$Shift)
chi2 4 = chisq.test(tb4)
chi2 4$p.value
tb5 = table(df$`Complaint Code`, df$`Manufacturing Plant`)
chi2 5 = chisq.test(tb5)
chi2 5$p.value
# II)
tab1 = table(df$`Complaint Code`, df$`Manufacturing Plant`)
```

```
chi2 = chisq.test(tab1)
chi2$expected
chi2$p.value
# III)
df1 = df[,c(1,4)]
df1 = df1[ df1$`Manufacturing Plant` < 3, ]</pre>
t.test(df1$`Dollar Claim Amount` ~ df1$`Manufacturing Plant`,
data = df1
#12)
#II)
library("fpc")
library("dbscan")
6, 7, 8, 9, 9)
y \leftarrow c(5, 6, 2, 3, 5, 6, 7, 8, 3, 5, 7, 8, 4, 6, 8, 4, 5, 6,
7, 4, 3, 2, 5)
data <- data.frame(x=x, y=y)</pre>
db <- fpc::dbscan(data , eps = 1, MinPts = 3)</pre>
plot(db, data , main = "DBSCAN")
#III)
plot fun <- function(data, nc) {</pre>
  wss <- (nrow(data)-1) * sum(apply(data,2,var))</pre>
  for(i in 2:nc) {wss[i] <-
sum(kmeans(data,centers=i)$withinss)}
  plot(1:nc, wss, type = "b" ,xlab="Number of
Clusters", ylab="Total within Sum of Square") }
plot fun(data, nrow(data)-1)
kc <- kmeans(data, 4)</pre>
plot(data, col=kc$cluster)
#13)
x \leftarrow c(0.4005, 0.2148, 0.3457, 0.2652, 0.0789, 0.4548)
y \leftarrow c(0.5306, 0.3854, 0.3156, 0.1875, 0.4139, 0.3022)
data \leftarrow cbind(x,y)
#πίνακας για ευκλειδεια αποσταση
dist(data, method = "euclidean", diag = TRUE, upper = TRUE)
#α ερωτημα
hc <- hclust(dist(data), method = "single")</pre>
plot(hc, hang = -1)
#β ερωτημα
hc <- hclust(dist(data), method = "complete")</pre>
plot(hc, hang = -1)
```