

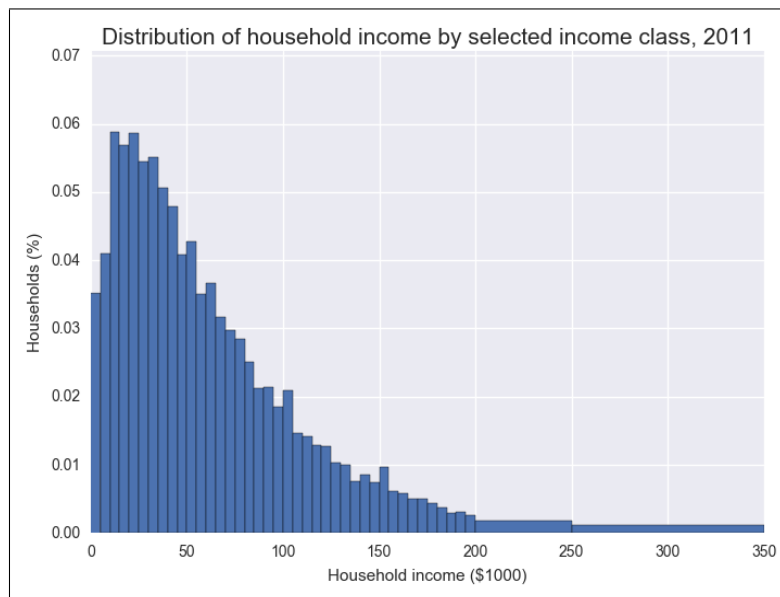
Problem Set #4

MACS 40200, Dr. Evans

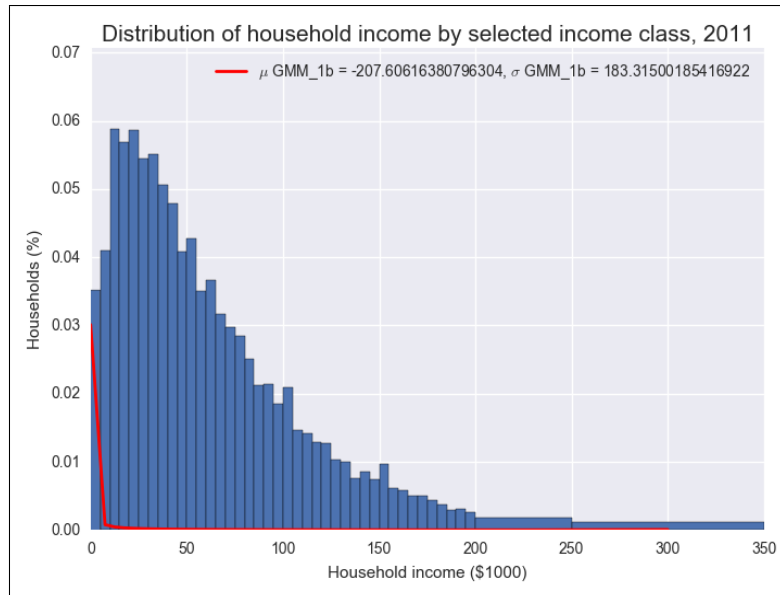
Bobae Kang

1. Matching the U.S. income distribution by GMM.

- (a) Plot the histogram implied by the moments in the tab-delimited text file `usincmoms.txt`.



- (b) Using GMM, fit the lognormal $\text{LN}(x; \mu, \sigma)$ distribution defined in the MLE notebook to the distribution of household income data using the moments from the data file. Report your estimated values for $\hat{\mu}$ and $\hat{\sigma}$, as well as the value of the minimized criterion function. Plot the histogram from part (a) overlaid with a line representing the implied histogram from your estimated lognormal (LN) distribution.



GMM crietron function value = 39.49333133

GMM estimate for μ , with $\mathbf{W} = \mathbf{I} = -207.606163808$

GMM estimate for σ , with $\mathbf{W} = \mathbf{I} = 183.315001854$

- (c) Using GMM, fit the gamma $GA(x; \alpha, \beta)$ distribution defined in the MLE notebook to the distribution of household income data using the moments from the data file. Report your estimated values for $\hat{\alpha}$ and $\hat{\beta}$, as well as the value of the minimized criterion function. Plot the histogram from part (a) overlaid with a line representing the implied histogram from your estimated gamma (GA) distribution.

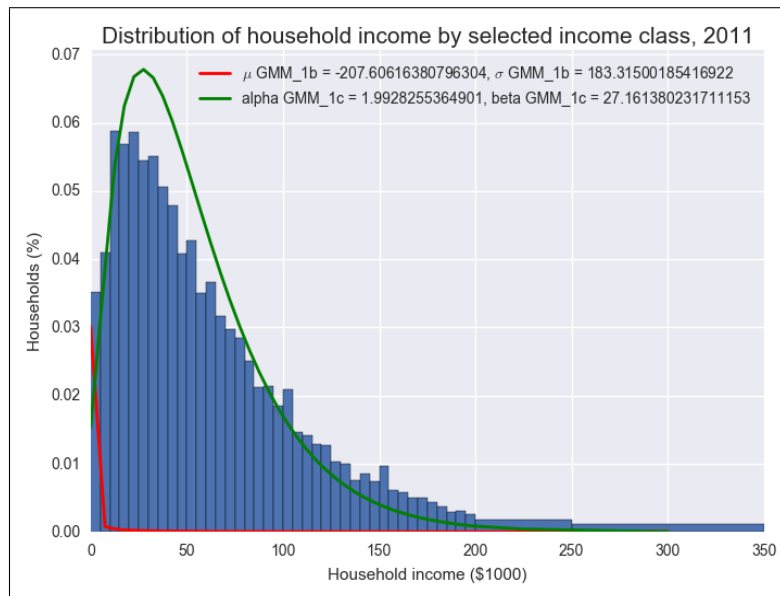


GMM crietron function value = 6.70630637

GMM estimate for α , with $\mathbf{W} = \mathbf{I} = 1.99282553649$

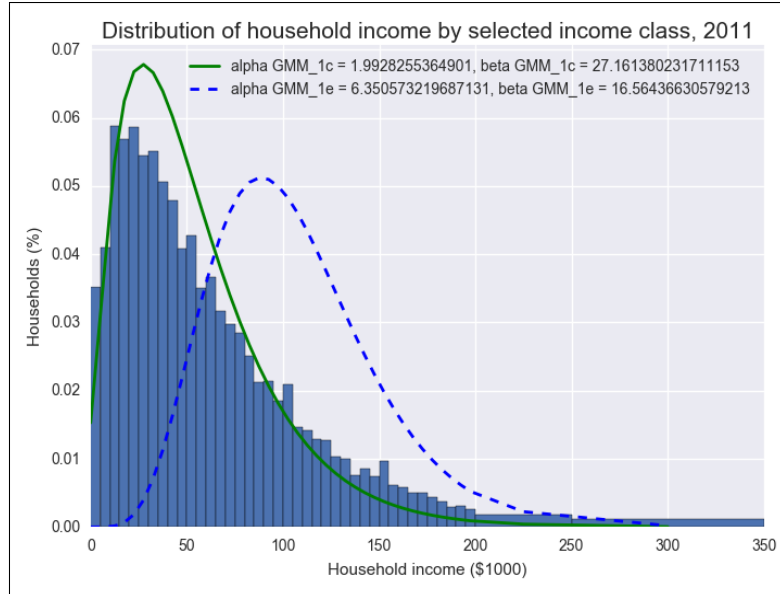
GMM estimate for β , with $\mathbf{W} = \mathbf{I} = 27.1613802317$

- (d) Plot the histogram from part (a) overlaid with the line representing the implied histogram from your estimated lognormal (LN) distribution from part (b) and the line representing the implied histogram from your estimated gamma (GA) distribution from part (c). What is the most precise way to tell which distribution fits the data the best? Which estimated distribution—LN or GA—fits the data best?



As illustrated by the plot above, the GA distribution fits the data with greater precision than the LN distribution.

- (e) Repeat your estimation of the GA distribution from part (c), but use the two-step estimator for the optimal weighting matrix. Do your estimates for α and β change much? How can you compare the goodness of fit of this estimated distribution versus the goodness of fit of the estimated distribution in part (c)?



GMM crietron function value = 2.93161087e-13

GMM estimate for α , with $\hat{\mathbf{W}}_{twostep} = 6.35057321969$

GMM estimate for β , with $\hat{\mathbf{W}}_{twostep} = 16.5643663058$

The plot suggests that the first GMM estimates of α and β with the weighting matrix $\mathbf{W} = \mathbf{I}$ better fits the distribution to the data than the second estimates of parameters with the two-step weighting matrix.