## Problem Set #5

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## 1. Estimating the Brock and Mirman (1972) model by GMM

The initial guess for four parameters  $(\alpha, \beta, \rho \text{ and } \mu)$  are 0.9, 0.9, 0.8, and 0.9. The optimal weight matrix is the identity matrix.

GMM crietron function value: 0.0010927458976064087

GMM estimate for  $\alpha$ ,  $\hat{\alpha}_{GMM}$ : 0.94105041259485267

GMM estimate for  $\beta$ ,  $\hat{\beta}_{GMM}$ : 0.9899999979977578

GMM estimate for  $\rho$ ,  $\hat{\rho}_{GMM}$ : 0.80720182684927166

GMM estimate for  $\mu$ ,  $\hat{\mu}_{GMM}$ : 0.90180045556233812

## 2. Estimating the Brock and Mirman (1972) model by SMM

The initial guess for the first four parameters  $(\alpha, \beta, \rho \text{ and } \mu)$  are drawn from the GMM estimates for the parameters. For  $\sigma$ , the initial guess is 0.05. The optimal weight matrix is the identity matrix. I used the percent differences between data moments and model moments for the error vector.

SMM crietron function value = 0.0028188726710878455

SMM estimate for  $\alpha$ ,  $\hat{\alpha}_{SMM}$ : 0.98650781222182915

SMM estimate for  $\beta$ ,  $\hat{\beta}_{SMM}$ : 0.51831095502582225

SMM estimate for  $\rho$ ,  $\hat{\rho}_{SMM}$ : 0.22332759404146543

SMM estimate for  $\mu$ ,  $\hat{\mu}_{SMM}$ : 0.88826262203175477

SMM estimate for  $\sigma$ ,  $\hat{\sigma}_{SMM}$ : 0.050000000000000003

Difference in moments: [ -3.11612795e+05, 2.05802802e+05, 5.78905936e+10,

-3.84043313e+10, -3.40875963e-02, -1.51506126e-02]

Percent difference in moments: [-2.96186011, 1.97030792, 1.02598619,

-0.69052728, -3.40875963, -1.54430575]