First Problem Set

October 22, 2024

Instructions

- Due to 12th of November.
- Print outs:
 - Results for both questions plus computer codes used to estimate the results.

Data and Model

- Panel: 50 products in 20 geographic markets.
- For each product we have:
 - Market share (for each market).
 - 4 characteristics (X1-X4) and prices.
 - 6 instrumental variables (IV1-IV6).
- Consumer utility is:

$$U_{ijm} = -\alpha p_{jm} + \sum_{k=1}^{3} \beta_k x_{jmk} + \beta_{4i} x_{jm4} + \xi_j + \xi_{jm} + \varepsilon_{ijm},$$

- where, *i* denotes individuals, *j* choices and *m* markets, $\beta_{4i} = \beta_4 + \sigma_1 v_i$ and $v_i \stackrel{iid}{\sim} N(0,1)$, ξ_j is a product fixed-effect, ξ_{jm} denotes characteristics of product *j* at market *m* that is observed by consumers and firms (but not by the econometrician) and ε_{ijm} is iid EV across (i, j, m).
- Assume that there is an outside good such that $U_{im0} = \varepsilon_{im0}$ for each m.

Problem 1: Multinomial Logit.

Assume that $\sigma_1 = 0$ and $\varepsilon_{ijm} \stackrel{iid}{\sim} EV\left(\mu,\theta\right)$ where $\mu > 0$ is the scale parameter and θ is the location parameter of the distribution, i.e. $F_{\varepsilon}\left(x\right) = \exp\left\{-\exp\left[-\mu\left(x-\theta\right)\right]\right\}$.

- 1. Derive the share of each choice in each market.
- 2. Is μ identified? Why? And θ ?
- 3. Suppose that $\mu = 1$, $\theta = 0$. Suppose that you want to estimate the model using OLS.

- (a) Derive the equation you will use to estimate the model.
- (b) Under what conditions the OLS estimator is consistent?
- 4. Assume that $\xi_j = 0$. Estimate the parameters of the model by OLS and IV. Compare the estimates of α . Does the OLS bias have the expected sign? Explain.
- 5. Based on the IV parameters estimated above compute own- and cross-price elasticities for each good in market one. Discuss the results.

Problem 2: Random Coefficients Logit.

Assume that $\sigma_1 \neq 0$ and $\varepsilon_{ijm} \stackrel{iid}{\sim} EV(1,0)$. Assume that prices are correlated with ξ_{jm} .

- 1. Derive the choice probabilities.
- 2. Assume for simplicity that $\xi_j = 0$. Estimate the parameters of the model (including σ_1 and a constant) using a consistent estimator.
- 3. Compute own- and cross-price elasticities for each good in market one. Compare with the elasticities obtained in 1.5.