

Given clauses ( $c_i$  are the names of the clauses).

$c_1 : \neg x_1 \vee x_2$

$c_2 : \neg x_1 \vee x_3 \vee x_9$

$c_3 : \neg x_2 \vee \neg x_3 \vee x_4$

$c_4 : \neg x_4 \vee x_5 \vee x_{10}$

$c_5 : \neg x_4 \vee x_6 \vee x_{11}$

$c_6 : \neg x_5 \vee \neg x_6$

$c_7 : x_1 \vee x_7 \vee \neg x_{12}$

$c_8 : x_1 \vee x_8$

$c_9 : \neg x_7 \vee \neg x_8 \vee \neg x_{13}$

Draw the implication graph for assignment  $\neg x_9, \neg x_{10}, \neg x_{11}, x_{12}, x_{13}, x_1$ .

Using graphviz

```
digraph G {
    rankdir=TB;

    node [shape=ellipse];

    x1 [label="x1 (Decision)", shape=doublecircle, style=bold];
    n_x9 [label="¬x9 (Assign)", shape=doublecircle, style=bold];
    n_x10 [label="¬x10 (Assign)", shape=doublecircle, style=bold];
    n_x11 [label="¬x11 (Assign)", shape=doublecircle, style=bold];
    x12 [label="x12 (Assign)", shape=doublecircle, style=bold];
    x13 [label="x13 (Assign)", shape=doublecircle, style=bold];

    // default ellipse
    x2 [label="x2"];
    x3 [label="x3"];
    x4 [label="x4"];
    x5 [label="x5"];
    x6 [label="x6"];
```

```
// Conflict --> box
conflict [label="⊥ (Conflict)", shape=box];
```

```
// Implications
```

```
x1 -> x2 [label="c1"];
x1 -> x3 [label="c2"];
¬x9 -> x3 [label="c2"];
x2 -> x4 [label="c3"];
x3 -> x4 [label="c3"];
x4 -> x5 [label="c4"];
¬x10 -> x5 [label="c4"];
x4 -> x6 [label="c5"];
¬x11 -> x6 [label="c5"];
x5 -> conflict [label="c6"];
x6 -> conflict [label="c6"];
```

```
}
```

