

$$C_{ij} = \frac{1}{2} (C_{i \rightarrow j} + C_{j \rightarrow i})$$

$$P_{ij} = \frac{C_{ij}}{100f_i} = \frac{C_{ij}}{\sum_b \sum_{b \neq i} C_{ib}}$$

$$P_{ii} = 1 - \sum_{j \neq i} P_{ij}$$

$$f = A = 0,2083 \quad D = 0,25 \quad N = 0,0278$$

$$E = 0,2083 \quad B = 0,1528 \quad R = 0,1528$$

| | A | C | D | E | N | R |
|---|------|------|------|------|------|------|
| A | 0.91 | 0 | 0 | 0 | 0 | 0 |
| C | 0 | 0.91 | 0 | 0 | 0 | 0 |
| D | 0 | 0 | 0.91 | 0 | 0 | 0 |
| E | 0 | 0 | 0 | 0.91 | 0 | 0 |
| N | 0 | 0.01 | 0.01 | 0.01 | 0.85 | 0 |
| R | 0 | 0 | 0 | 0 | 0 | 0.98 |

$\times 10000 \Rightarrow$

| | A | C | D | E | N | R |
|---|------|------|------|------|------|------|
| A | 9918 | 21 | 21 | 7 | 7 | 2 |
| C | 21 | 9904 | 27 | 27 | 14 | 7 |
| D | 17 | 23 | 9931 | 6 | 11 | 1 |
| E | 9 | 37 | 9 | 9897 | 19 | 28 |
| N | 51 | 103 | 103 | 103 | 9837 | 10 |
| R | 37 | 9 | 19 | 28 | 19 | 9858 |

$$S(i,j) = \log_2 \left(\frac{P_{ij}}{f_i} \right) \Rightarrow$$

| | A | C | D | E | N | R |
|---|----|----|----|----|----|----|
| A | 2 | -7 | -7 | -8 | -5 | -6 |
| C | -7 | 2 | -7 | -6 | -4 | -8 |
| D | -7 | -7 | 2 | -8 | -5 | -7 |
| E | -8 | -6 | -8 | 3 | -4 | -6 |
| N | -5 | -4 | -5 | -4 | 5 | -4 |
| R | -6 | -8 | -7 | -6 | -4 | 3 |

PAM 250 day off to log 10

| | A | C | D | E | N | R |
|---|----|----|----|----|---|----|
| A | 1 | 0 | -1 | -1 | 0 | 0 |
| C | 0 | 1 | 0 | 0 | 0 | -1 |
| D | -1 | 0 | 1 | -1 | 0 | 0 |
| E | -1 | 0 | -1 | 1 | 0 | 0 |
| N | 0 | 0 | 0 | 0 | 0 | 0 |
| R | 0 | -1 | -1 | 0 | 0 | 1 |

Is this solid?
 No. Coherent under assumption,
 but the extrapolation over 250
 magnifies estimation of error

- How to get PAM 250 from PAM 1
- Consider PAM 1 as a time-homogeneous Markov matrix of one-step sub
 - Compute P^{250} (matrix power)
 - Convert to a scoring matrix via log odds against frequencies S_{ij} (base 2 or 10)

Rationale?

- Assume evolution is a first order, time homogeneous Markov process. $1\text{M} = 1\%$ accepted mutations
- Powers of P model "longer evolutionary time"