

Write a program to estimate the value of the percolation threshold via Monte Carlo simulation

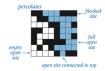
After following these instructions, the commands javac-algs4 and java-algs4 will classpath in algs4.jar , which contains Java classes for I/O and all of the algorithms in the textbook. To access a class in algs4.jar, you need an import statement, such as the ones below:

```
import edu.princeton.cs.algs4.StdRandom;
import edu.princeton.cs.algs4.StdStats;
import edu.princeton.cs.algs4.WeightedQuickUnionUF;
```

Note that your code must be in the default package; if you use a package statement, the autograder will reject your submission.

Percolation. Given a composite systems comprised of randomly distributed insulating and metallic materials: what fraction of the materials need to be metallic so that the composite system is an electrical conductor? Given a porous landscape with water on the surface (or oil below), under what conditions will the water be able to drain through to the bottom (or the oil to gush through to the surface)? Scientists have defined an abstract process known as percolation to model such situations.

The model. We model a percolation system using an n-by-n grid of sites. Each site is either open or blocked. A full site is an open site that can be connected to an open site in the top row via a chain of neighboring (left, right, up, down) open sites. We say the system percolates if there is a full site in the bottom row. In other words, a system percolates fir we fill all open sites connected to the top row and that process fills some open site on the bottom row. (For the insulating metallic materials example, the open sites correspond to metallic materials, so that a system that percolates has a metallic path from top to bottom, with full sites conducting. For the porous substance example, the open sites correspond to empty space through which water might flow, so that a system that percolates lets water fill open sites, flowing from top to bottom.)





The problem. In a famous scientific problem, researchers are interested in the following question: if sites are independently set to be open with probability p (and therefore blocked with probability 1-p), what is the probability that the system percolates? When p equals 0, the system does not percolate; when p equals 1, the system percolates. The plots below show the site vacancy probability p versus the percolation probability for 20-by-20 random grid (left) and 100-by-100 random grid (right).





When n is sufficiently large, there is a threshold value p^* such that when $p \le p^*$ a random n-by-n grid almost never percolates, and when $p \ge p^*$, a random n-by-n grid almost always percolates. No mathematical solution for determining the percolation threshold p^* has yet been derived. Your task is to write a computer program to estimate p^* .

Percolation data type. To model a percolation system, create a data type Percolation with the following API:

```
public class Percolation {
    // creates n-by-n grid, with all sites initially blocked
    public Percolation(int n)
    // opens the site (row, col) if it is not open already
    public wid open(int row, int col)
    // is the site (row, col) open?
    public boolean isopen(int row, int col)
    // is the site (row, col) open?
    public boolean isopen(int row, int col)
    // returns the number of open sites
    public int numberOfOpenSites()
    // does the system percolate?
    public boolean percolates()
    // test client (optional)
    public static void main(String[] args)
}
```

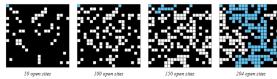
Corner cases. By convention, the row and column indices are integers between 1 and n, where (1,1) is the upper-left site: Throw an IllegalArgumentException if any argument to open(), isOpen(), or isFull() is outside its prescribed range. Throw an IllegalArgumentException in the constructor if $n \le 0$.

Performance requirements. The constructor should take time proportional to n²; all methods should take constant time plus a constant number of calls to the union-find methods union(), find(), connected(), and count().

Monte Carlo simulation. To estimate the percolation threshold, consider the following computational experiment

- Initialize all sites to be blocked.
- Repeat the following until the system percolates
 - Choose a site uniformly at random among all blocked sites.
 - o Open the site.
- The fraction of sites that are opened when the system percolates provides an estimate of the percolation threshold.

For example, if sites are opened in a 20-by-20 lattice according to the snapshots below, then our estimate of the percolation threshold is 204/400 = 0.51 because the system percolates when the 204th site is opened.



By repeating this computation experiment T times and averaging the results, we obtain a more accurate estimate of the percolation threshold. Let x_t be the fraction of open sites in computational experiment t. The sample mean \overline{x} provides an estimate of the percolation threshold; the sample standard deviation s_t measures the sharpness of the threshold.

$$\overline{x} = \frac{x_1 + x_2 + \dots + x_T}{T}, \quad s^2 = \frac{(x_1 - \overline{x})^2 + (x_2 - \overline{x})^2 + \dots + (x_T - \overline{x})^2}{T - 1}$$

Assuming T is sufficiently large (say, at least 30), the following provides a 95% confidence interval for the percolation threshold:

$$\left[\ \overline{x} - rac{1.96s}{\sqrt{T}}, \ \ \overline{x} + rac{1.96s}{\sqrt{T}} \
ight]$$

To perform a series of computational experiments, create a data type PercolationStats with the following API.

```
public class PercolationStats {

// perform independent trials on an n-by-n grid
public PercolationStats(int n, int trials)

// sample mean of percolation threshold
public double mean()

// sample standard deviation of percolation threshold
public double stddev()

// law admalated new confidence interval
```

```
public double confidenceto()

// high endpoint of 95% confidence interval
public double confidenceHi()

// test client (see below)
public static void main(String[] args)
}
```

Throw an IllegalArgumentException in the constructor if either $n \le 0$ or $trials \le 0$.

Also, include a main() method that takes two command-line arguments n and T, performs T independent computational experiments (discussed above) on an n-by-n grid, and prints the sample mean, sample standard deviation, and the 95% confidence interval for the percolation threshold. Use https://discussed.above) on an n-by-n grid, and prints the sample mean, sample standard deviation, and the 95% confidence interval for the percolation threshold. Use https://discussed.above) on an n-by-n grid, and prints the sample mean, sample standard deviation, and the 95% confidence interval for the percolation threshold. Use https://discussed.above) on an n-by-n grid, and prints the sample mean, sample standard deviation, and the 95% confidence interval for the percolation threshold. Use https://discussed.above) on an n-by-n grid, and prints the sample mean, sample standard deviation.



Analysis of running time and memory usage (optional and not graded). Implement the Percolation data type using the quick find algorithm in quickFindUF 🐇

- Use \$\frac{1}{2}\$ to measure the total running time of PercolationStats for various values of n and T. How does doubling n affect the total running time? How does doubling T affect the total running time? Give a formula (using tilde notation) of the total running time on your computer (in seconds) as a single function of both n and T.
- Using the 64-bit memory-cost model from lecture, give the total memory usage in bytes (using tilde notation) that a Percolation object uses to model an n-by-n percolation system. Count all memory that is used, including memory for the union-find data structure.

Now, implement the Percolation data type using the weighted quick witon algorithm in <a href="https://linearchy.org/linearchy.or

Web submission. Submit a zip file containing only Submit only Percolation. java (using the weighted quick-union algorithm from HeightedQuickUnionUF 4) and PercolationStats. java. We will supply algs4. jar. Your submission may not call library functions except those in Stdin 4, Stdout 5, Stdout 5

For fun. Create your own percolation input file and share it in the discussion forums. For some inspiration, do an image search for "nonogram puzzles solved."

This assignment was developed by Bob Sedgewick and Kevin Wayne. Copyright @ 2008.