

Lab Report 6

Submitted by: Submitted to:

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1.2.1 Part A

Find the Jaccard similarity of each of the above documents to all other documents.

Answer:

The Jaccard similarity is defined as,

$$JS(A,B) = \frac{A \cap B}{A \cup B}$$

Where, A and B are two documents, $A \cap B$ denote the total number of unique words on both of them and $A \cup B$ denotes the number of common words both the documents have.

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PART A: Find the Jaccard similarity of each of the above documents to all other documents.
For Document 1 and 2:
Intersection: {'am', 'sam', 'i'}
Union: { 'am', 'i', 'sam' }
Jaccard similarity: 1.0
For Document 1 and 3:
Intersection: {'i'}
Union: {'eggs', 'not', 'and', 'ham', 'do', 'sam', 'i', 'am', 'green', 'like'}
Jaccard similarity: 0.1
For Document 1 and 4:
Intersection: {'am', 'sam', 'i'}
Union: {'not', 'do', 'sam', 'i', 'them', 'am', 'like'}
Jaccard similarity: 0.42857142857142855
For Document 2 and 3:
Intersection: {'i'}
Union: {'eggs', 'not', 'and', 'ham', 'do', 'sam', 'i', 'am', 'green', 'like'}
Jaccard similarity: 0.1
For Document 2 and 4:
Intersection: {'am', 'sam', 'i'}
Union: {'not', 'do', 'sam', 'i', 'them', 'am', 'like'}
Jaccard similarity: 0.42857142857142855
For Document 3 and 4:
Intersection: {'not', 'do', 'like', 'i'}
Union: {'not', 'and', 'ham', 'green', 'do', 'sam', 'i', 'them', 'am', 'eggs', 'like'}
Jaccard similarity: 0.36363636363636363
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1.2.2 Part B

Calculate the Cosine similarity of the above documents.

Answer:

Cosine similarity is calculated as,

$$\operatorname{CosSim}(\boldsymbol{d}_{j}, \boldsymbol{q}) = \frac{\vec{\boldsymbol{d}}_{j} \cdot \vec{\boldsymbol{q}}}{\left| \vec{\boldsymbol{d}}_{j} \right| \cdot \left| \vec{\boldsymbol{q}} \right|} = \frac{\sum_{i=1}^{t} (w_{ij} \cdot w_{iq})}{\sqrt{\sum_{i=1}^{t} w_{ij}^{2} \cdot \sum_{i=1}^{t} w_{iq}^{2}}}$$

Where $\overrightarrow{d_j}$ is a document vector which is calculated by the weights of all the words in both the documents with respect to document j. It is computed as

$$w_{ij} = tf_{ij} idf_i = tf_{ij} \log_2 (N/df_i)$$

where,

$$tf_{ij} = f_{ij} / max_i \{f_{ij}\}$$

 f_{ij} is the frequency of ith word in jth document.

 df_i = document frequency of term i

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For Document 1 and 2
Cosine Similarity: 1.0

For Document 1 and 3
Cosine Similarity: 0.0

For Document 1 and 4
Cosine Similarity: 0.21658124988136848

For Document 2 and 3
Cosine Similarity: 0.0

For Document 2 and 4
Cosine Similarity: 0.21658124988136848

For Document 3 and 4
Cosine Similarity: 0.25395862933166535

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