

# Computer Vision 2

## Assignment 2



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

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Group 8  
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### Problem 1 Graphical models (20 Points)

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#### 1. 1 Point

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Two main ingredients the set of random variables describing the entities involved the problem, and the second ingredient is the set of conditional probabilities, that tell us the relation between a certain variable and another variable or variables from the set.

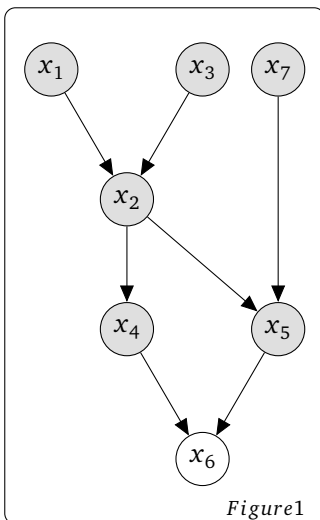
#### 2. 1 Point

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As we know that directed graphs are versatile, but not always appropriate. So they are not always be convenient to provide conditional distributions, and some of certain conditional independence structures that a directed graph can not represent. So for example Loopy graph, it is not possible to express the same conditional independence statements using the a directed graph model.

#### 3. 2 Points

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The Markov Blanket of variable  $x_2$  is formed from the variables that are filled with gray color.

#### 4. 2 Points

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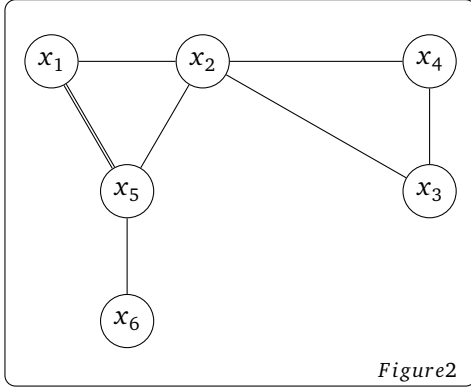
The factorization of the directed graphical model is as follows

$$p(x_1, x_2, x_4, x_5, x_6, x_7, x_8, x_9, x_{10}, x_{11}, x_{12}, x_{13}, x_{14}, x_{15}) = p(x_1)p(x_2)p(x_3)p(x_6)p(x_7)p(x_4|x_1, x_2)p(x_5|x_2, x_3)p(x_{10}|x_7)p(x_{11}|x_{10})p(x_8|x_4, x_5)p(x_9|x_3, x_5, x_6)p(x_{14}|x_{11})p(x_{12}|x_8, x_9)p(x_{13}|x_9)p(x_{15}|x_{12})$$

The factorization of the undirected graphical model is as follows

$$p(x_1, x_2, x_4, x_5, x_6, x_7, x_8, x_9, x_{10}, x_{11}, x_{12}, x_{13}, x_{14}, x_{15}) = \frac{1}{Z} \phi_0(x_3)\phi_1(x_1, x_4)\phi_2(x_2, x_4, x_5, x_8)\phi_3(x_7, x_{10})\phi_4(x_7, x_{11})\phi_5(x_{11}, x_{14})\phi_6(x_5, x_9)\phi_7(x_8, x_{12})\phi_8(x_9, x_{12}, x_{13}, x_{15})\phi_9(x_6, x_9)$$

5. 1 Point



6. 2 Points

$x_1$	$x_2$	$x_3$	$x_4$	$p(x_1, x_2, x_3, x_4)$	$\frac{1}{Z}p(x_1, x_2, x_3, x_4)$
0	0	0	0	$1*1*1*1=1$	0.1077
0	0	0	1	$1*1*0.1*0.1=0.01$	0.001077
0	0	1	0	$1*0.1*0.1*1=0.01$	0.001077
0	0	1	1	$1*0.1*2*0.1=0.02$	0.002155
0	1	0	0	$0.1*0.1*1*1=0.01$	0.001077
0	1	0	1	$0.1*0.1*0.1*0.1=0.0001$	0.00001077
0	1	1	0	$0.1*2*0.1*1=0.02$	0.002155
0	1	1	1	$0.1*2*2*0.1=0.04$	0.00431
1	0	0	0	$0.1*1*1*0.1=0.01$	0.001077
1	0	0	1	$0.1*1*0.1*2=0.02$	0.002155
1	0	1	0	$0.1*0.1*0.1*0.1=0.0001$	0.00001077
1	0	1	1	$0.1*0.1*2*2=0.04$	0.00431
1	1	0	0	$2*0.1*1+0.1=0.02$	0.002155
1	1	0	1	$2*0.1*0.1*2=0.04$	0.00431
1	1	1	0	$2*2*0.1*0.1=0.04$	0.00431
1	1	1	1	$2*2*2*2=8$	0.86206

We have computed Z as the sum of all the probabilities above, and after the calculation we found  $Z=9.28$ .

7. 2 Points

Based on those four records

a	b	c	$p(a,b,c)$
0	1	0	0.048
1	0	0	0.192
0	1	1	0.216
1	0	1	0.064

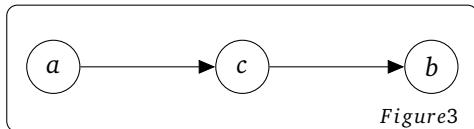
The first and second row c remain the same but a and b change and with them the distribution too, the same happens in the third and fourth row. So we can conclude that those variable a and b are marginally dependent, when  $b=1$  and  $a=0$  then the distribution is 0.048 but in the other hand, when  $b=0$  and  $a=1$  then the distribution is 0.192, so this means knowing event b does help in value of event a and vice versa.

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8. 3 Points

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Based on the given distributions  $p(a)$   $p(b|c)$   $p(c|a)$  we can draw the directed graph as follows :



And from the figure above we can write:

$$p(a, b, c) = p(a)p(a|c)p(b|a, c) = p(a)p(a|c)p(b|c)$$

As we know from directed graph, because 'c' tell us about 'a', we can take away 'a' from  $p(b|a, c)$ , and therefore we get the desired probability.

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9. 2 Points

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Markov blanket of variables in undirected graph:

$$x_1 -> x_2, x_3$$

$$x_2 -> x_1, x_4$$

$$x_3 -> x_1, x_4$$

$$x_4 -> x_2, x_3$$

Markov blanket of variables in directed graph:

$$x_1 -> x_2, x_3$$

$$x_2 -> x_1, x_3, x_4$$

$$x_3 -> x_1, x_2, x_4$$

$$x_4 -> x_2, x_3$$

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10. 4 Points

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Based also in the previous question about for Markov blanket for each of the variables, we can conclude that in the figure 2, undirected graph, the first one that says  $x_1$  is independent of  $x_4$  and that  $x_2$  and  $x_3$  are the Markov blanket of  $x_1$ , is completely true based also in the definition that, a node is conditionally independent of all other nodes given its Markov blanket. The second one that says  $x_2$  is independent of  $x_3$ , because the  $x_3$  is not in the Markov blanket of  $x_2$ , and from definition a node is conditionally independent of all other nodes given its Markov blanket, and that  $x_1$  and  $x_4$  are the Markov blanket of  $x_2$ , because they are direct node of  $x_2$ . And for the directed Graph, first one that says  $x_1$  independent of  $x_4$ , exactly as the definition from above, and that  $x_2$  and  $x_3$  are the Markov blanket of  $x_1$ , because  $x_1$  has 2 children and no other parents and also those children have just one parent and its  $x_1$ . The second one

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Problem 2 Markov random fields with Student-t potentials (10 Points)

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Tasks 1-4 within code

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5. 3 Points

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Problem 3 Stereo with gradient-based optimization (17 Points)

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Everything else is in code.

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6. 4 Points

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Problem 4 Stereo with a generalized robust function (10 Points)

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Everything else is in code.

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5. ? Point/s

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6. ? Point/s

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