

- [R2012b](#)
- [Global Optimization Toolbox](#)
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ga

Find minimum of function using genetic algorithm

Syntax

```
x = ga(fitnessfcn,nvars)
x = ga(fitnessfcn,nvars,A,b)
x = ga(fitnessfcn,nvars,A,b,Aeq,beq)
x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB)
x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB,nonlcon)
x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB,nonlcon,options)
x = ga(fitnessfcn,nvars,A,b,[],[],LB,UB,nonlcon,IntCon)
x = ga(fitnessfcn,nvars,A,b,[],[],LB,UB,nonlcon,IntCon,options)
x = ga(problem)
[x,fval] = ga(fitnessfcn,nvars,...)
[x,fval,exitflag] = ga(fitnessfcn,nvars,...)
[x,fval,exitflag,output] = ga(fitnessfcn,nvars,...)
[x,fval,exitflag,output,population] = ga(fitnessfcn,nvars,...)
[x,fval,exitflag,output,population,scores] = ga(fitnessfcn,nvars,...)
```

Description

$x = \text{ga}(\text{fitnessfcn}, \text{nvars})$ finds a local unconstrained minimum, x , to the objective function, fitnessfcn . nvars is the dimension (number of design variables) of fitnessfcn . The objective function, fitnessfcn , accepts a vector x of size 1-by- nvars , and returns a scalar evaluated at x .

$x = \text{ga}(\text{fitnessfcn}, \text{nvars}, A, b)$ finds a local minimum x to fitnessfcn , subject to the linear inequalities $A \cdot x \leq b$. fitnessfcn accepts input x and returns a scalar function value evaluated at x .

$x = \text{ga}(\text{fitnessfcn}, \text{nvars}, A, b, Aeq, beq)$ finds a local minimum x to fitnessfcn , subject to the linear equalities $Aeq \cdot x = beq$ as well as $A \cdot x \leq b$. (Set $A=[]$ and $b=[]$ if no inequalities exist.)

$x = \text{ga}(\text{fitnessfcn}, \text{nvars}, A, b, Aeq, beq, LB, UB)$ defines a set of lower and upper bounds on the design variables, x , so that a solution is found in the range $LB \leq x \leq UB$. Use empty matrices for LB and UB if no bounds exist.

$x = \text{ga}(\text{fitnessfcn}, \text{nvars}, A, b, Aeq, beq, LB, UB, \text{nonlcon})$ subjects the minimization to the constraints defined in nonlcon . The function nonlcon accepts x and returns vectors c and ceq , representing the nonlinear inequalities and equalities respectively. ga minimizes the fitnessfcn such that $c(x) \leq 0$ and $ceq(x) = 0$. (Set $LB=[]$ and $UB=[]$ if no bounds exist.)

$x = \text{ga}(\text{fitnessfcn}, \text{nvars}, A, b, Aeq, beq, LB, UB, \text{nonlcon}, \text{options})$ minimizes with the default optimization parameters replaced by values in the structure options , which can be created using the [gaoptimset](#) function.

$x = \text{ga}(\text{fitnessfcn}, \text{nvars}, A, b, [], [], LB, UB, \text{nonlcon}, \text{IntCon})$ requires that the variables listed in IntCon take integer values.

Note: When there are integer constraints, ga does not accept linear or nonlinear equality constraints, only inequality constraints.

$x = \text{ga}(\text{fitnessfcn}, \text{nvars}, A, b, [], [], LB, UB, \text{nonlcon}, \text{IntCon}, \text{options})$ minimizes with integer constraints and with the default optimization parameters replaced by values in the options structure.

$x = \text{ga}(\text{problem})$ finds the minimum for problem , where problem is a structure.

$[x, fval] = \text{ga}(\text{fitnessfcn}, \text{nvars}, \dots)$ returns $fval$, the value of the fitness function at x .

$[x, fval, \text{exitflag}] = \text{ga}(\text{fitnessfcn}, \text{nvars}, \dots)$ returns exitflag , an integer identifying the reason the algorithm terminated.

$[x, fval, \text{exitflag}, \text{output}] = \text{ga}(\text{fitnessfcn}, \text{nvars}, \dots)$ returns output , a structure that contains output from each generation and other information about the performance of the algorithm.

$[x, fval, \text{exitflag}, \text{output}, \text{population}] = \text{ga}(\text{fitnessfcn}, \text{nvars}, \dots)$ returns the matrix, population , whose rows are the final population.

$[x, fval, \text{exitflag}, \text{output}, \text{population}, \text{scores}] = \text{ga}(\text{fitnessfcn}, \text{nvars}, \dots)$ returns scores the scores of the final population.

Input Arguments

fitnessfcn Handle to the fitness function. The fitness function should accept a row vector of length nvars and return a scalar value.

When the 'Vectorized' option is 'on', fitnessfcn should accept a pop-by- nvars matrix, where pop is the current population size. In this case fitnessfcn should return a vector the same length as pop containing the fitness function values. fitnessfcn should not assume any particular size for pop , since ga can pass a single member of a population even in a vectorized calculation.

nvars Positive integer representing the number of variables in the problem.

A Matrix for linear inequality constraints of the form

$$A x \leq b.$$

If the problem has m linear inequality constraints and $nvars$ variables, then

- A is a matrix of size m -by- $nvars$.
- b is a vector of length m .

Note: `ga` does not enforce linear constraints to be satisfied when the `PopulationType` option is 'bitString' or 'custom'.

b Vector for linear inequality constraints of the form

$$A x \leq b.$$

If the problem has m linear inequality constraints and $nvars$ variables, then

- A is a matrix of size m -by- $nvars$.
- b is a vector of length m .

Aeq Matrix for linear equality constraints of the form

$$Aeq x = beq.$$

If the problem has m linear equality constraints and $nvars$ variables, then

- Aeq is a matrix of size m -by- $nvars$.
- beq is a vector of length m .

Note: `ga` does not enforce linear constraints to be satisfied when the `PopulationType` option is 'bitString' or 'custom'.

beq Vector for linear equality constraints of the form

$$Aeq x = beq.$$

If the problem has m linear equality constraints and $nvars$ variables, then

- Aeq is a matrix of size m -by- $nvars$.
- beq is a vector of length m .

LB Vector of lower bounds. `ga` enforces that iterations stay above **LB**. Set $LB(i) = -\text{Inf}$ if $x(i)$ is unbounded below.

UB Vector of upper bounds. `ga` enforces that iterations stay below **UB**. Set $UB(i) = \text{Inf}$ if $x(i)$ is unbounded above.

nonlcon Function handle that returns two outputs:

$$[c, ceq] = \text{nonlcon}(x)$$

`ga` attempts to achieve $c \leq 0$ and $ceq = 0$. c and ceq are row vectors when there are multiple constraints. Set unused outputs to `[]`.

You can write `nonlcon` as a function handle to a file, such as

```
nonlcon = @constraintfile
```

where `constraintfile.m` is a file on your MATLAB path.

To learn how to use vectorized constraints, see [Vectorized Constraints](#).

Note: `ga` does not enforce nonlinear constraints to be satisfied when the `PopulationType` option is set to 'bitString' or 'custom'.
If `IntCon` is not empty, the second output of `nonlcon` (ceq) must be empty (`[]`).

options

Structure containing optimization options. Create options using [gaoptimset](#), or by exporting options from the Optimization Tool as described in [Importing and Exporting Your Work](#) in the Optimization Toolbox documentation.

IntCon

Vector of positive integers taking values from 1 to `nvars`. Each value in `IntCon` represents an `x` component that is integer-valued.

Note: When `IntCon` is nonempty, `Aeq` and `beq` must be empty (`[]`), and `nonlcon` must return empty for `ceq`. For more information on integer programming, see [Mixed Integer Optimization](#).

problem

Structure containing the following fields:

<code>fitnessfcn</code>	Fitness function
<code>nvars</code>	Number of design variables
<code>Aineq</code>	A matrix for linear inequality constraints
<code>Bineq</code>	b vector for linear inequality constraints
<code>Aeq</code>	Aeq matrix for linear equality constraints
<code>Beq</code>	beq vector for linear equality constraints
<code>lb</code>	Lower bound on <code>x</code>
<code>ub</code>	Upper bound on <code>x</code>
<code>nonlcon</code>	Nonlinear constraint function
<code>rngstate</code>	Optional field to reset the state of the random number generator
<code>intcon</code>	Index vector of integer variables
<code>solver</code>	'ga'
<code>options</code>	Options structure created using gaoptimset or the Optimization Tool

Create `problem` by exporting a problem from the Optimization Tool, as described in [Importing and Exporting Your Work](#) in the Optimization Toolbox documentation.

Output Arguments

x

Best point that `ga` located during its iterations.

fval

Fitness function evaluated at `x`.

exitflag

Integer giving the reason `ga` stopped iterating:

Exit Flag	Meaning
1	<p>Without nonlinear constraints — Average cumulative change in value of the fitness function over <code>StallGenLimit</code> generations is less than <code>TolFun</code>, and the constraint violation is less than <code>TolCon</code>.</p> <p>With nonlinear constraints — Magnitude of the complementarity measure (see Definitions) is less than <code>sqrt(TolCon)</code>, the subproblem is solved using a tolerance less than <code>TolFun</code>, and the constraint violation is less than <code>TolCon</code>.</p>
2	Fitness limit reached and the constraint violation is less than <code>TolCon</code> .
3	Value of the fitness function did not change in <code>StallGenLimit</code> generations and the constraint violation is less than <code>TolCon</code> .
4	Magnitude of step smaller than machine precision and the constraint violation is less than <code>TolCon</code> .
5	Minimum fitness limit <code>FitnessLimit</code> reached and the constraint violation is less than <code>TolCon</code> .
0	Maximum number of generations <code>Generations</code> exceeded.
-1	Optimization terminated by the output or plot function.
-2	No feasible point found.
-4	Stall time limit <code>StallTimeLimit</code> exceeded.
-5	Time limit <code>TimeLimit</code> exceeded.

When there are integer constraints, `ga` uses the penalty fitness value instead of the fitness value for stopping criteria.

output

Structure containing output from each generation and other information about algorithm performance. The output structure contains the following fields:

- `problemtype` — String describing the type of problem, one of:
 - `'unconstrained'`
 - `'boundconstraints'`
 - `'linearconstraints'`
 - `'nonlinearconstr'`
 - `'integerconstraints'`
- `rngstate` — State of the MATLAB random number generator, just before the algorithm started. You can use the values in `rngstate` to reproduce the output of `ga`. See [Reproducing Your Results](#).
- `generations` — Number of generations computed.
- `funccount` — Number of evaluations of the fitness function.
- `message` — Reason the algorithm terminated.
- `maxconstraint` — Maximum constraint violation, if any.

population

Matrix whose rows contain the members of the final population.

scores

Column vector of the fitness values (scores for `integerconstraints` problems) of the final population.

Examples

Given the following inequality constraints and lower bounds

$$\begin{bmatrix} 1 & 1 \\ -1 & 2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \leq \begin{bmatrix} 2 \\ 2 \\ 3 \end{bmatrix},$$

$$x_1 \geq 0, \quad x_2 \geq 0,$$

use this code to find the minimum of the `lincontest6` function, which is provided in your software:

```
A = [1 1; -1 2; 2 1];
b = [2; 2; 3];
lb = zeros(2,1);
[x,fval,exitflag] = ga(@lincontest6,...
    2,A,b,[],[],lb)
```

Optimization terminated: average change in the fitness value less than options.TolFun.

```
x =
    0.6700    1.3310
```

```
fval =
   -8.2218
```

```
exitflag =
     1
```

Optimize a function where some variables must be integers:

```
fun = @(x) (x(1) - 0.2)^2 + ...
    (x(2) - 1.7)^2 + (x(3) - 5.1)^2;
x = ga(fun,3,[],[],[],[],[],[],[], ...
    [2 3]) % variables 2 and 3 are integers
```

Optimization terminated: average change in the penalty fitness value less than options.TolFun and constraint violation is less than options.TolCon.

```
x =
    0.2000    2.0000    5.0000
```

Alternatives

For problems without integer constraints, consider using [patternsearch](#) instead of `ga`.

More About

[expand all](#)

Complementarity Measure

In the nonlinear constraint solver, the complementarity measure is the norm of the vector whose elements are $c_i \lambda_i$, where c_i is the nonlinear inequality constraint violation, and λ_i is the corresponding Lagrange multiplier.

Tips

- To write a function with additional parameters to the independent variables that can be called by `ga`, see [Passing Extra Parameters](#) in the Optimization Toolbox documentation.
- For problems that use the population type `double` vector (the default), `ga` does not accept functions whose inputs are of type `complex`. To solve problems involving complex data, write your functions so that they accept real vectors, by separating the real and imaginary parts.

Algorithms

For a description of the genetic algorithm, see [How the Genetic Algorithm Works](#).

For a description of the mixed integer programming algorithm, see [Integer ga Algorithm](#).

For a description of the nonlinear constraint algorithm, see [Nonlinear Constraint Solver Algorithm](#).

- [Genetic Algorithm](#)
- [Getting Started with Global Optimization Toolbox](#)
- [Optimization Problem Setup](#)

See Also

[gamultiobj](#) | [gaoptimset](#) | [patternsearch](#)

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