

Formulae

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1 movement

Given a velocity v and a position vector s

We currently $s_{n+1} = s_n + v * t$

We want to use a solver for the DE $v = \frac{\partial s}{\partial t}$

2 acceleration

We currently use $v_{n+1} = v_n + a * t$

We want to use a solver for the DE $v = \frac{\partial^2 s}{\partial t^2}$

3 force

$$a = \frac{F}{m}$$

4 collisions

collision on a plane with normalized normal n_u

decompose v into vector u orthogonal to the plane and w parallel to the plane

$$u = v * n_u * n_u$$

$$w = v - u$$

compute the outgoing velocity v' , considering the coefficient of restitution c_r

and the coefficient of friction c_f

$$v' = w * c_f - u * c_r$$

computing the force F_c needed to transform v into v'

$$F_c = m * \frac{\partial v}{\partial t} = m * \frac{dv'}{dt} - v \frac{\partial}{\partial t}$$

5 normal force

Computing the normal force F_n , being the projection of F_g onto the normalized normal vector n_u of the plane supporting an object

$$F_n = F_g * n_u * n_u$$