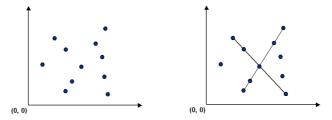
Write a program to recognize line patterns in a given set of points.

Computer vision involves analyzing patterns in visual images and reconstructing the real-world objects that produced them. The process is often broken up into two phases: feature detection and pattern recognition. Feature detection involves selecting important features of the image; pattern recognition involves discovering patterns in the features. We will investigate a particularly clean pattern recognition problem involving points and line segments. This kind of pattern recognition arises in many other applications such as statistical data analysis.

The problem. Given a set of n distinct points in the plane, find every (maximal) line segment that connects a subset of 4 or more of the points.



Point data type. Create an immutable data type Point that represents a point in the plane by implementing the following API:

```
public class Point implements Comparable<Point> {
  public Point(int x, int y)
                                                      // constructs the point (x, y)
                                                      // draws this point
  public
           void draw()
  public
            void drawTo(Point that)
                                                       // draws the line segment from this point to that point
  public String toString()
                                                       // string representation
                                                      // compare two points by y-coordinates, breaking ties by x-coordinates
  public
                        int compareTo(Point that)
                                                       // the slope between this point and that point
  public
                     double slopeTo(Point that)
  public Comparator<Point> slopeOrder()
                                                       // compare two points by slopes they make with this point
```

To get started, use the data type Point.java , which implements the constructor and the draw(), drawTo(), and toString() methods. Your job is to add the following components.

- The compareTo() method should compare points by their y-coordinates, breaking ties by their x-coordinates. Formally, the invoking point (x_0, y_0) is less than the argument point (x_1, y_1) if and only if either $y_0 < y_1$ or if $y_0 = y_1$ and $x_0 < x_1$.
- The slopeTo() method should return the slope between the invoking point (x_0, y_0) and the argument point (x_1, y_1) , which is given by the formula $(y_1 y_0) / (x_1 x_0)$. Treat the slope of a horizontal line segment as positive zero; treat the slope of a vertical line segment as positive infinity; treat the slope of a degenerate line segment (between a point and itself) as negative infinity.
- The slopeOrder() method should return a comparator that compares its two argument points by the slopes they make with the invoking point (x_0, y_0) . Formally, the point (x_1, y_1) is less than the point (x_2, y_2) if and only if the slope $(y_1 y_0) / (x_1 x_0)$ is less than the slope $(y_2 y_0) / (x_2 x_0)$. Treat horizontal, vertical, and degenerate line segments as in the slopeTo() method.
- Do not override the equals () or hashCode () methods.

Corner cases. To avoid potential complications with integer overflow or floating-point precision, you may assume that the constructor arguments x and y are each between 0 and 32.767.

Line segment data type. To represent line segments in the plane, use the data type LineSegment.java , which has the following API:

Brute force. Write a program BruteCollinearPoints.java that examines 4 points at a time and checks whether they all lie on the same line segment, returning all such line segments. To check whether the 4 points p, q, r, and s are collinear, check whether the three slopes between p and q, between p and p and p are all equal

The method segments () should include each line segment containing 4 points exactly once. If 4 points appear on a line segment in the order $p \rightarrow q \rightarrow r \rightarrow s$, then you should include either the line segment $p \rightarrow s$ or $s \rightarrow p$ (but not both) and you should not include *subsegments* such as $p \rightarrow r$ or $q \rightarrow r$. For simplicity, we will not supply any input to BruteCollinearPoints that has 5 or more collinear points.

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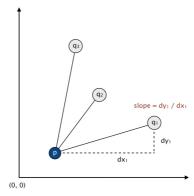
Corner cases. Throw a java.lang.IllegalArgumentException if the argument to the constructor is null, if any point in the array is null, or if the argument to the constructor contains a repeated point.

Performance requirement. The order of growth of the running time of your program should be n^4 in the worst case and it should use space proportional to n plus the number of line segments returned.

A faster, sorting-based solution. Remarkably, it is possible to solve the problem much faster than the brute-force solution described above. Given a point p, the following method determines whether p participates in a set of 4 or more collinear points.

- Think of p as the origin.
- For each other point q, determine the slope it makes with p.
- Sort the points according to the slopes they makes with p.
- Check if any 3 (or more) adjacent points in the sorted order have equal slopes with respect to p. If so, these points, together with p, are collinear.

Applying this method for each of the *n* points in turn yields an efficient algorithm to the problem. The algorithm solves the problem because points that have equal slopes with respect to *p* are collinear, and sorting brings such points together. The algorithm is fast because the bottleneck operation is sorting.



Write a program FastCollinearPoints.java that implements this algorithm.

```
public class FastCollinearPoints {
    public FastCollinearPoints(Point[] points)
    public int numberOfSegments()
    public LineSegment[] segments()
}
// finds all line segments containing 4 or more points
// the number of line segments
// the line segments
}
```

The method segments () should include each *maximal* line segment containing 4 (or more) points exactly once. For example, if 5 points appear on a line segment in the order $p \rightarrow q \rightarrow r \rightarrow s \rightarrow t$, then do not include the subsegments $p \rightarrow s$ or $q \rightarrow t$.

Corner cases. Throw a java.lang.IllegalArgumentException if the argument to the constructor is null, if any point in the array is null, or if the argument to the constructor contains a repeated point.

Performance requirement. The order of growth of the running time of your program should be $n^2 \log n$ in the worst case and it should use space proportional to n plus the number of line segments returned. FastCollinearPoints should work properly even if the input has 5 or more collinear points.

Sample client. This client program takes the name of an input file as a command-line argument; read the input file (in the format specified below); prints to standard output the line segments that your program discovers, one per line; and draws to standard draw the line segments.

```
public static void main(String[] args) {
    // read the n points from a file
    In in = new In(args[0]);
    int n = in.readInt();
    Point[] points = new Point[n];
for (int i = 0; i < n; i++) {</pre>
        int x = in.readInt();
int y = in.readInt();
        points[i] = new Point(x, y);
    // draw the points
    StdDraw.enableDoubleBuffering();
    StdDraw.setXscale(0, 32768);
    StdDraw.setYscale(0, 32768);
    for (Point p : points) {
        p.draw();
    StdDraw.show();
    // print and draw the line segments
    FastCollinearPoints collinear = new FastCollinearPoints(points);
    for (LineSegment segment : collinear.segments()) {
        StdOut.println(segment);
         segment.draw();
    StdDraw.show();
}
```

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Input format. We supply several sample input files (suitable for use with the test client above) in the following format: An integer n, followed by n pairs of integers (x, y), each between 0 and 32,767. Below are two examples.

```
% more input6.txt
                        % more input8.txt
19000 10000
                        10000
18000
      10000
                            Ω
                                10000
32000
      10000
                          3000
                                 7000
21000 10000
                          7000
                                 3000
 1234
       5678
                         20000
                                21000
14000 10000
                         3000
                                4000
                         14000
                                15000
                          6000
                                7000
```

```
% java-algs4 BruteCollinearPoints input8.txt
(10000, 0) -> (0, 10000)
(3000, 4000) -> (20000, 21000)

% java-algs4 FastCollinearPoints input8.txt
(3000, 4000) -> (20000, 21000)
(0, 10000) -> (10000, 0)

% java-algs4 FastCollinearPoints input6.txt
(14000, 10000) -> (32000, 10000)
```

Deliverables. Submit only the files <code>BruteCollinearPoints.java</code>, <code>FastCollinearPoints.java</code>, and <code>Point.java</code>. We will supply <code>LineSegment.java</code> and <code>algs4.jar</code>. You may not call any library functions other those in <code>java.lang</code>, <code>java.util</code>, and <code>algs4.jar</code>. You may use library functions in <code>java.util</code> only if they have already been introduced in the course. For example, you may use <code>Arrays.sort()</code>, but not <code>java.util.HashSet</code>.

This assignment was developed by Bob Sedgewick and Kevin Wayne. Copyright @ 2008.

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