

 $\label{eq:Figure 1: interconnect} \ \ \text{Figure 1: interconnect} \ \ - \ \ \text{Resistive electro-thermal interconnect element}.$

Author: Kai Li

Description:

This element implements an interconnect line as an electro-thermal resistor. effects.

Form: interconnectrt: $\langle instance name \rangle n_1 n_2 n_3 n_4 \langle parameter list \rangle$

instance name is the model name,

 n_1, n_2, n_3 and n_4 are the element terminals,

 n_1 and n_2 are element electrical terminals,

 n_3 and n_4 are element thermal terminals,

 n_2 is the element local reference node,

 n_4 is the element thermal reference node.

Parameters:

Parameter	Type	Default value	Required?
l: Length of interconnect line (m)	DOUBLE	n/a	yes
w: Width of interconnect line (m)	DOUBLE	$1 \mu m$	no
tm: Thickness of interconnect line (m)	DOUBLE	$0.3~\mu m$	no
rho: Resistivity of metal $(\Omega - m)$	DOUBLE	n/a	no
metal: Metal (Silver, Copper, Gold, Aluminum)	STRING	copper	no
t: System temperature $({}^{0}C)$	DOUBLE	20	no
tnom: Initial system temperature $({}^{0}C)$	DOUBLE	20	no
tc: Temperature coefficient $(1/{}^{0}C)$	DOUBLE	0	no
pdr: Thermal element flag	BOOLEAN	false	no

Example:

interconnectrt: irt1 2 0 3 "tref" 1 = 20u metal = "copper"

Details:

The resistive thermal interconnect is modeled as resistive only, the metal line is made by a kind of metal,

which includes silver, copper, gold, and aluminum that are predefined in the model.

This is an electro-thermal element is modeled differently depending on the setting of the Parameter pdr.

pdr = false/true.

When pdr is false (the default) the interconnect line is calculated as a resistor by giving length and resistivity or metal selection.

When pdr is true, the interconnect line is modeled as electro-thermal resistor by giving length, resistivity or metal selection, and system temperature. Resistance calculation is based on the electrical parameters and system temperature. The power dissipation and heat flux are modeled with thermal terminals.

Resistance of the interconnect line:

$$R = \frac{\rho \cdot l}{A}$$

Electro-thermal resistance of the interconnect with temperature coefficient:

$$R = \frac{\rho \cdot l}{A} \cdot [1 + \beta \cdot (t - t_0)]$$

interconnectrt: irt1 2 0 3 "tref" l = 20u metal = "copper"

Here terminals '0' and 'tref' are the local reference terminals of the element. Terminal '0' is the global ground. Terminal 'tref' is a thermal local reference terminal of the element. An example netlist is:

```
.ref "tref"
.ref 0

vsource 1 0 vac = 1 f = 5GHz
res:r1 1 2 r=50
interconnectrt:irt1 2 0 1000 "tref" l = 1m metal = "copper" pdr=1
```

References:

- 1. Houssam S.Kanj. fREEDA element ResistorT, "elements \r ResistorT".
- 2. Tony Mulder, Travis Lentz. fREEDA element CmosInvT, "elements\c\CmosInvT"

Example of Transient Analysis (.TRAN2) Fixed times steps, time-stepping nonlinear analysis. netlist file: interconnectrt.net:

```
*** Transient InterconnectRT test

*** Transient Analysis
.tran2 tstop=4e-6 tstep=10e-9 out_steps=5
.options InitTmp=300
.ref "tref"
```

```
.ref 0
*** Sources
vpulse: Vp 1 0 v1=1 v2=5 per=2e-6 pw=1e-6 tr=0.05e-6 tf=0.05e-6
*** Network
resistor:rs 1 2 r=2k
interconnectrt:irt1 2 0 1000 "tref" l=1e-3 metal="copper" pdr=1
*interconnectrt:irt1 2 0 1000 "tref" l=1e-3 rho=1.83e-8 tc=0.004041 pdr=1
*** Thermal network
resistor:rt1 1000 1001 r=6e3
vsource:vt1 1001 "tref" vdc=InitTmp
capacitor:ct1 1000 1001 c=1e-12
*** Transient Output
.options gnuplot
*.out plot term 2 vt in "trans_input.out"
.out plot term 2 vt element "interconnectrt:irt1" 0 it div in "trans_res.out"
*.out plot element "interconnectrt:irt1" 0 it in "trans_current.out"
.out plot element "interconnectrt:irt1" 1 ut in "trans_temp.out"
.end
The output log file is
****** fREEDA 1.3 running on Thu Apr 17 22:25:28 2008 ********
** Environment variables: **
FREEDA_HOME = /Users/Jerry/freeda
FREEDA_LIBRARY = /Users/Jerry/freeda/library
FREEDA_PROJECTS = /Users/Jerry/freeda/projects
FREEDA_PATH = /Users/Jerry/freeda/freeda
FREEDA_BIN = /Users/Jerry/freeda/freeda/bin
FREEDA_SIMULATOR = /Users/Jerry/freeda/freeda/simulator
FREEDA_ELEMENTS = /Users/Jerry/freeda/freeda/simulator/elements
FREEDA_DOCUMENTATION = /tmp
FREEDA_WEB_DOCUMENTATION = http://www.freeda.org/doc
FREEDA_BROWSER = firefox
*** Transient InterconnectRT test
*** Transient InterconnectRT test
*** Transient Analysis
.tran2 tstop=4e-6 tstep=10e-9 out_steps=5
.options inittmp=300
.ref "tref"
.ref 0
```

```
*** Sources
vpulse:vp 1 0 v1=1 v2=5 per=2e-6 pw=1e-6 tr=0.05e-6 tf=0.05e-6
*** Network
resistor:rs 1 2 r=2k
interconnectrt:irt1 2 0 1000 "tref" l=1e-3 metal="copper" pdr=1
*interconnectrt:irt1 2 0 1000 "tref" l=1e-3 rho=1.83e-8 tc=0.004041 pdr=1
*** Thermal network
resistor:rt1 1000 1001 r=6e3
vsource:vt1 1001 "tref" vdc=inittmp
capacitor:ct1 1000 1001 c=1e-12
*** Transient Output
.options gnuplot
*.out plot term 2 vt in "trans_input.out"
.out plot term 2 vt element "interconnectrt:irt1" 0 it div in "trans_res.out"
*.out plot element "interconnectrt:irt1" 0 it in "trans_current.out"
.out plot element "interconnectrt:irt1" 1 ut in "trans_temp.out"
  *** Starting analysis ...
                  ------
  Matrix size = 6
  Matrix nnz = 12
  equed = 1.42812e-306
  recip_pivot_growth = 1
  1 / Condition number = 0.297426
  info = 0
  ferr = 2.85551e-307
  berr = 1
  No of nonzeros in factor L = 12
  No of nonzeros in factor U = 12
  No of nonzeros in L+U = 18
  L\U MB 0.000 total MB needed 0.001 expansions 0
  Using line search method.
  Nonlinear analysis tolerance (ftol) = 6.12865e-06
  Maximum number of nonlinear iterations per time-point (maxit) = 250
  Using Lee and Lee's quasi-Newton updates.
  --- Starting transient simulation ...
  Number of nonlinear state variables: 2
  | Step | Time (s) | Residual | Recent Max | Max |
_____
       0 | 0.000000e+00 | 3.303597e-06 | 3.303597e-06 | 3.303597e-06 |
       5 | 5.000000e-08 | 3.170376e-06 | 3.204794e-06 | 3.303597e-06 |
       10 | 1.000000e-07 | 2.053913e-15 | 2.358213e-07 | 3.303597e-06 |
```

15 | 1.500000e-07 | 1.871533e-06 | 2.138801e-06 *| 3.303597e-06 |

```
20 | 2.000000e-07 | 1.871421e-06 | 1.871423e-06 *| 3.303597e-06 |
25 | 2.500000e-07 | 1.871421e-06 | 1.871421e-06 * | 3.303597e-06 |
 30 | 3.000000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 35 | 3.500000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 40 | 4.000000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 45 | 4.500000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 50 | 5.000000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 55 | 5.500000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 60 | 6.000000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 65 | 6.500000e-07 | 1.871421e-06 | 1.871421e-06 * | 3.303597e-06
 70 | 7.000000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 75 | 7.500000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 80 | 8.000000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
 85 | 8.500000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
90 | 9.000000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
95 | 9.500000e-07 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
100 | 1.000000e-06 | 1.871421e-06 | 1.871421e-06 *| 3.303597e-06
105 | 1.050000e-06 | 1.871421e-06 | 1.871421e-06 * 3.303597e-06
110 | 1.100000e-06 | 3.202763e-06 | 3.219358e-06 | 3.303597e-06
115 | 1.150000e-06 | 5.551115e-17 | 5.007632e-09 | 3.303597e-06 |
120 | 1.200000e-06 | 4.924549e-07 | 5.627811e-07 *| 3.303597e-06
125 | 1.250000e-06 | 4.924256e-07 | 4.924261e-07 *| 3.303597e-06
130 | 1.300000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
135 | 1.350000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
140 | 1.400000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
145 | 1.450000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
150 | 1.500000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
155 | 1.550000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
160 | 1.600000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
165 | 1.650000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
170 | 1.700000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
175 | 1.750000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
180 | 1.800000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
185 | 1.850000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
190 | 1.900000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
195 | 1.950000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
200 | 2.000000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06
205 | 2.050000e-06 | 3.170377e-06 | 3.204658e-06 | 3.303597e-06
210 | 2.100000e-06 | 1.665335e-16 | 2.358209e-07 | 3.303597e-06
215 | 2.150000e-06 | 1.871531e-06 | 2.138800e-06 *| 3.303597e-06
220 | 2.200000e-06 | 1.871420e-06 | 1.871422e-06 *| 3.303597e-06
225 | 2.250000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06
230 | 2.300000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06
235 | 2.350000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06
240 | 2.400000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06
245 | 2.450000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06
250 | 2.500000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06
255 | 2.550000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06
260 | 2.600000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06
265 | 2.650000e-06 | 1.871420e-06 | 1.871420e-06 * | 3.303597e-06 |
270 | 2.700000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06 |
```

```
275 | 2.750000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06 |
    280 | 2.800000e-06 | 1.871420e-06 | 1.871420e-06 * | 3.303597e-06 |
    285 | 2.850000e-06 | 1.871420e-06 | 1.871420e-06 * | 3.303597e-06 |
    290 | 2.900000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06 |
    295 | 2.950000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06 |
    300 | 3.000000e-06 | 1.871420e-06 | 1.871420e-06 *| 3.303597e-06 |
    305 | 3.050000e-06 | 1.871420e-06 | 1.871420e-06 * | 3.303597e-06 |
    310 | 3.100000e-06 | 3.202763e-06 | 3.219358e-06 | 3.303597e-06 |
    315 | 3.150000e-06 | 5.684368e-14 | 5.007632e-09 | 3.303597e-06 |
    320 | 3.200000e-06 | 4.924549e-07 | 5.627812e-07 *| 3.303597e-06 |
    325 | 3.250000e-06 | 4.924256e-07 | 4.924262e-07 *| 3.303597e-06 |
    330 | 3.300000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    335 | 3.350000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    340 | 3.400000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    345 | 3.450000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    350 | 3.500000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    355 | 3.550000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    360 | 3.600000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    365 | 3.650000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    370 | 3.700000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    375 | 3.750000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    380 | 3.800000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    385 | 3.850000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    390 | 3.900000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    395 | 3.950000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
    400 | 4.000000e-06 | 4.924256e-07 | 4.924256e-07 *| 3.303597e-06 |
--- Maximum Residual: 3.3036e-06
```

Plotting output file: trans_res.out.
Plotting output file: trans_temp.out.

****** fREEDA 1.3 stopping on Thu Apr 17 22:25:28 2008 ********

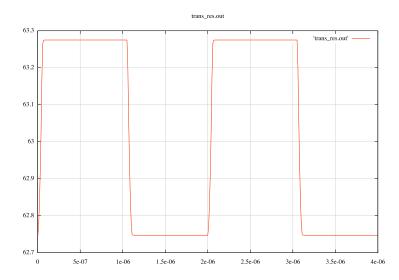


Figure 2: Transient Analysis - Resistance variation of thermal interconnect

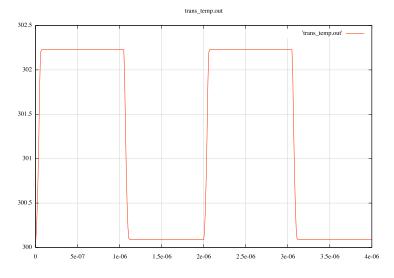


Figure 3: Transient Analysis - Temperature variation of interconnect line

Version:

2008.04.21 (2008 April 21)

Credits:

Name Affiliation Date Links

Kai Li NC State University April 2008 \blacksquare NC STATE UNIVERSITY

kli@ieee.org www.ncsu.edu