

# Numeroes complejos

$$\bar{z} = a + j b$$

$$|\bar{z}| = |z|$$

## Polar

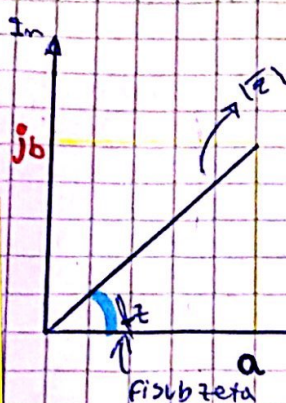
$$|\bar{z}| = \sqrt{(z_x)^2 + (z_y)^2}$$

$$\alpha z = \arctan\left(\frac{z_y}{z_x}\right)$$

## binomica

$$z_x = |\bar{z}| \cos(\alpha z)$$

$$z_y = |\bar{z}| \sin(\alpha z)$$



SOLCARTOA

## Formula de Euler

$$e^{jx} = \cos(x) + j \sin(x)$$

$$e^{-jx} = \cos(x) - j \sin(x)$$

$$\frac{e^{jx} + e^{-jx}}{2} = \cos(x)$$

$$\frac{e^{jx} - e^{-jx}}{2j} = \sin(x)$$

$$\cos \alpha z = \frac{z_x}{|\bar{z}|}$$

$$\sin \alpha z = \frac{z_y}{|\bar{z}|}$$

## Resolvemos

### 1) Pasar a polar

$$\begin{aligned} \bar{a} &= 1 + j1 & \sqrt{2} & e^{j45^\circ} \\ \bar{b} &= 10 + j0 & 10 & e^{j0^\circ} \\ \bar{c} &= 0 + j10 & 10 & e^{j90^\circ} \\ \bar{d} &= -20 - j10 & 22,36 & e^{j206,56^\circ} \\ \bar{e} &= -3 + j4 & 5 & e^{j126,87^\circ} \\ \bar{f} &= 3 - j6 & 6,71 & e^{j-63,43^\circ} \end{aligned}$$

$$\begin{aligned} |\bar{a}| &= \sqrt{1^2 + 1^2} & \alpha \bar{a} &= \tan^{-1}\left(\frac{1}{1}\right) \\ |\bar{a}| &= \sqrt{2} & \alpha \bar{a} &= 45^\circ \end{aligned}$$

$$\begin{aligned} |\bar{b}| &= \sqrt{10^2 + 0^2} & \alpha \bar{b} &= \tan^{-1}\left(\frac{0}{10}\right) \\ |\bar{b}| &= \sqrt{100} & \alpha \bar{b} &= 0 \\ |\bar{b}| &= 10 \end{aligned}$$

$$\begin{aligned} |\bar{c}| &= \sqrt{0^2 + 10^2} & \alpha \bar{c} &= \tan^{-1}\left(\frac{10}{0}\right) \\ |\bar{c}| &= 10 & \alpha \bar{c} &= 90^\circ \end{aligned}$$

$$\begin{aligned} |\bar{d}| &= \sqrt{(-20)^2 + (-10)^2} & \alpha \bar{d} &= \tan^{-1}\left(\frac{-10}{-20}\right) \\ |\bar{d}| &= 22,36 & \alpha \bar{d} &= 206,56^\circ \end{aligned}$$

$$\begin{aligned} |\bar{e}| &= \sqrt{(-3)^2 + 4^2} & \alpha \bar{e} &= \tan^{-1}\left(\frac{4}{-3}\right) \\ |\bar{e}| &= 5 & \alpha \bar{e} &= 126,87^\circ \end{aligned}$$

### 2) Pasar a binomica

$$\begin{aligned} \bar{a} &= 3e^{j20^\circ} & 2,18 & + j1,026 \\ \bar{b} &= 5e^{j0^\circ} & 0 & + j0 \\ \bar{c} &= 2e^{j90^\circ} & -2 & + j0 \\ \bar{d} &= 6e^{j206,56^\circ} & 0 & - j6 \\ \bar{e} &= 8e^{j126,87^\circ} & 8 & + j5 \\ \bar{f} &= 4e^{j-63,43^\circ} & 1,41 & + j1,41 \\ \bar{g} &= 2e^{j0^\circ} & 2 & + j0 \end{aligned}$$