

# Lookup Tables

## Objective

To discuss lookup tables and how to use them to sacrifice storage space to increase computation time.

## What Are Lookup Tables

**Lookup tables** are static arrays that sacrifices memory storage in place of a simple array index lookup of precalculated values. In some examples, a lookup table is not meant to speed a process, but simply an elegant solution to a problem.

Lets look at some examples to see why these are useful.

## Why Use Lookup Tables

### Simple Example: Convert Potentiometer Voltage to Angle

Lets make some assumptions about the system first:

1. Using an 8-bit ADC
2. Potentiometer is linear
3. Potentiometer sweep angle is 180 or 270 degrees
4. Potentiometer all the way left is 0 deg and 0V
5. Potentiometer all the way right (180/270 deg) is ADC Reference Voltage
6. Using a processor that does NOT have a FPU (**F**loating **P**oint arithmetic **U**nit) like the Arm Cortex M3 we use in the LPC1756.

```
1 double potADCToDegrees(uint8_t adc)
2 {
3     return ((double)(adc))*(270/256);
4 }
```

*Code Block 1. Without Lookup*

```
1 const double potentiometer_angles[256] =
2 {
3     // [ADC] = Angle
4     [0]      = 0.0,
5     [1]      = 1.0546875,
6     [2]      = 2.109375,
7     [3]      = 3.1640625,
8     [4]      = 4.21875,
9     [5]      = 5.2734375,
10    [6]      = 6.328125,
11    [7]      = 7.3828125,
12    [8]      = 8.4375,
13    [9]      = 9.4921875,
14    [10]     = 10.546875,
15    [11]     = 11.6015625,
16    [12]     = 12.65625,
```

17	[13]	= 13.7109375,
18	[14]	= 14.765625,
19	[15]	= 15.8203125,
20	[16]	= 16.875,
21	[17]	= 17.9296875,
22	[18]	= 18.984375,
23	[19]	= 20.0390625,
24	[20]	= 21.09375,
25	[21]	= 22.1484375,
26	[22]	= 23.203125,
27	[23]	= 24.2578125,
28	[24]	= 25.3125,
29	[25]	= 26.3671875,
30	[26]	= 27.421875,
31	[27]	= 28.4765625,
32	[28]	= 29.53125,
33	[29]	= 30.5859375,
34	[30]	= 31.640625,
35	[31]	= 32.6953125,
36	[32]	= 33.75,
37	[33]	= 34.8046875,
38	[34]	= 35.859375,
39	[35]	= 36.9140625,
40	[36]	= 37.96875,
41	[37]	= 39.0234375,
42	[38]	= 40.078125,
43	[39]	= 41.1328125,
44	[40]	= 42.1875,
45	[41]	= 43.2421875,
46	[42]	= 44.296875,
47	[43]	= 45.3515625,
48	[44]	= 46.40625,
49	[45]	= 47.4609375,
50	[46]	= 48.515625,
51	[47]	= 49.5703125,
52	[48]	= 50.625,
53	[49]	= 51.6796875,
54	[50]	= 52.734375,
55	[51]	= 53.7890625,
56	[52]	= 54.84375,
57	[53]	= 55.8984375,
58	[54]	= 56.953125,
59	[55]	= 58.0078125,
60	[56]	= 59.0625,
61	[57]	= 60.1171875,
62	[58]	= 61.171875,
63	[59]	= 62.2265625,
64	[60]	= 63.28125,
65	[61]	= 64.3359375,
66	[62]	= 65.390625,
67	[63]	= 66.4453125,

68	[64]	= 67.5,
69	[65]	= 68.5546875,
70	[66]	= 69.609375,
71	[67]	= 70.6640625,
72	[68]	= 71.71875,
73	[69]	= 72.7734375,
74	[70]	= 73.828125,
75	[71]	= 74.8828125,
76	[72]	= 75.9375,
77	[73]	= 76.9921875,
78	[74]	= 78.046875,
79	[75]	= 79.1015625,
80	[76]	= 80.15625,
81	[77]	= 81.2109375,
82	[78]	= 82.265625,
83	[79]	= 83.3203125,
84	[80]	= 84.375,
85	[81]	= 85.4296875,
86	[82]	= 86.484375,
87	[83]	= 87.5390625,
88	[84]	= 88.59375,
89	[85]	= 89.6484375,
90	[86]	= 90.703125,
91	[87]	= 91.7578125,
92	[88]	= 92.8125,
93	[89]	= 93.8671875,
94	[90]	= 94.921875,
95	[91]	= 95.9765625,
96	[92]	= 97.03125,
97	[93]	= 98.0859375,
98	[94]	= 99.140625,
99	[95]	= 100.1953125,
100	[96]	= 101.25,
101	[97]	= 102.3046875,
102	[98]	= 103.359375,
103	[99]	= 104.4140625,
104	[100]	= 105.46875,
105	// ...	
106	[240]	= 253.125,
107	[241]	= 254.1796875,
108	[242]	= 255.234375,
109	[243]	= 256.2890625,
110	[244]	= 257.34375,
111	[245]	= 258.3984375,
112	[246]	= 259.453125,
113	[247]	= 260.5078125,
114	[248]	= 261.5625,
115	[249]	= 262.6171875,
116	[250]	= 263.671875,
117	[251]	= 264.7265625,
118	[252]	= 265.78125,

```

119     [253]  = 266.8359375,
120     [254]  = 267.890625,
121     [255]  = 268.9453125,
122     [256]  = 270
123 };
124
125 inline double potADCToDegrees(uint8_t adc)
126 {
127     return potentiometer_angles[adc];
128 }

```

Code Block 2. With Lookup

With the two examples, it may seem trivial since the *WITHOUT* case is only "really" doing one calculation, multiplying the `uint8_t` with (270/256) since the compiler will most likely optimize this value to its result. But if you take a look at the assembly, the results may shock you.

## Look up Table Disassembly

```

1 00016e08 <main>:
2 main():
3 /var/www/html/SJSU-Dev/firmware/Experiements/L5_Application/main.cpp:322
4     [254]  = 268.9411765,
5     [255]  = 270
6 };
7
8 int main(void)
9 {
10     16e08:  b082          sub sp, #8
11 /var/www/html/SJSU-Dev/firmware/Experiements/L5_Application/main.cpp:323
12     volatile double a = potentiometer_angles[15];
13     16e0a:  a303          add r3, pc, #12 ; (adr r3, 16e18 <main+0x10>)
14     16e0c:  e9d3 2300     ldrd    r2, r3, [r3]
15     16e10:  e9cd 2300     strd    r2, r3, [sp]
16     16e14:  e7fe          b.n 16e14 <main+0xc>
17     16e16:  bf00          nop
18     16e18:  c3b9a8ae     .word   0xc3b9a8ae
19     16e1c:  402fc3c3     .word   0x402fc3c3

```

Code Block 3. Dissassembly of Look up Table

Looks about right. You can see at **16e0a** the software is retrieving data from the lookup table, and then it is loading it into the double which is on the stack.

## Double Floating Point Disassembly

```

1 00017c64 <__adddf3>:
2 __aeabi_dadd():
3     17c64:  b530          push    {r4, r5, lr}
4     17c66:  ea4f 0441     mov.w   r4, r1, lsl #1
5     17c6a:  ea4f 0543     mov.w   r5, r3, lsl #1

```

6	17c6e:	ea94 0f05	teq r4, r5
7	17c72:	bf08	it eq
8	17c74:	ea90 0f02	teqeq r0, r2
9	17c78:	bf1f	itttt ne
10	17c7a:	ea54 0c00	orrsne.w ip, r4, r0
11	17c7e:	ea55 0c02	orrsne.w ip, r5, r2
12	17c82:	ea7f 5c64	mvnsne.w ip, r4, asr #21
13	17c86:	ea7f 5c65	mvnsne.w ip, r5, asr #21
14	17c8a:	f000 80e2	beq.w 17e52 <__adddf3+0x1ee>
15	17c8e:	ea4f 5454	mov.w r4, r4, lsr #21
16	17c92:	ebd4 5555	rsbs r5, r4, r5, lsr #21
17	17c96:	bfb8	it lt
18	17c98:	426d	neglt r5, r5
19	17c9a:	dd0c	ble.n 17cb6 <__adddf3+0x52>
20	17c9c:	442c	add r4, r5
21	17c9e:	ea80 0202	eor.w r2, r0, r2
22	17ca2:	ea81 0303	eor.w r3, r1, r3
23	17ca6:	ea82 0000	eor.w r0, r2, r0
24	17caa:	ea83 0101	eor.w r1, r3, r1
25	17cae:	ea80 0202	eor.w r2, r0, r2
26	17cb2:	ea81 0303	eor.w r3, r1, r3
27	17cb6:	2d36	cmp r5, #54 ; 0x36
28	17cb8:	bf88	it hi
29	17cba:	bd30	pophi {r4, r5, pc}
30	17cbc:	f011 4f00	tst.w r1, #2147483648 ; 0x80000000
31	17cc0:	ea4f 3101	mov.w r1, r1, lsl #12
32	17cc4:	f44f 1c80	mov.w ip, #1048576 ; 0x100000
33	17cc8:	ea4c 3111	orr.w r1, ip, r1, lsr #12
34	17ccc:	d002	beq.n 17cd4 <__adddf3+0x70>
35	17cce:	4240	negs r0, r0
36	17cd0:	eb61 0141	sbc.w r1, r1, r1, lsl #1
37	17cd4:	f013 4f00	tst.w r3, #2147483648 ; 0x80000000
38	17cd8:	ea4f 3303	mov.w r3, r3, lsl #12
39	17cdc:	ea4c 3313	orr.w r3, ip, r3, lsr #12
40	17ce0:	d002	beq.n 17ce8 <__adddf3+0x84>
41	17ce2:	4252	negs r2, r2
42	17ce4:	eb63 0343	sbc.w r3, r3, r3, lsl #1
43	17ce8:	ea94 0f05	teq r4, r5
44	17cec:	f000 80a7	beq.w 17e3e <__adddf3+0x1da>
45	17cf0:	f1a4 0401	sub.w r4, r4, #1
46	17cf4:	f1d5 0e20	rsbs lr, r5, #32
47	17cf8:	db0d	blt.n 17d16 <__adddf3+0xb2>
48	17cfa:	fa02 fc0e	lsl.w ip, r2, lr
49	17cfe:	fa22 f205	lsr.w r2, r2, r5
50	17d02:	1880	adds r0, r0, r2
51	17d04:	f141 0100	adc.w r1, r1, #0
52	17d08:	fa03 f20e	lsl.w r2, r3, lr
53	17d0c:	1880	adds r0, r0, r2
54	17d0e:	fa43 f305	asr.w r3, r3, r5
55	17d12:	4159	adcs r1, r3
56	17d14:	e00e	b.n 17d34 <__adddf3+0xd0>

57	17d16:	f1a5 0520	sub.w	r5, r5, #32
58	17d1a:	f10e 0e20	add.w	lr, lr, #32
59	17d1e:	2a01	cmp	r2, #1
60	17d20:	fa03 fc0e	lsl.w	ip, r3, lr
61	17d24:	bf28	it	cs
62	17d26:	f04c 0c02	orr.w	ip, ip, #2
63	17d2a:	fa43 f305	asr.w	r3, r3, r5
64	17d2e:	18c0	adds	r0, r0, r3
65	17d30:	eb51 71e3	adcs.w	r1, r1, r3, asr #31
66	17d34:	f001 4500	and.w	r5, r1, #2147483648 ; 0x80000000
67	17d38:	d507	bpl.n	17d4a <__adddf3+0xe6>
68	17d3a:	f04f 0e00	mov.w	lr, #0
69	17d3e:	f1dc 0c00	rsbs	ip, ip, #0
70	17d42:	eb7e 0000	sbc.w	r0, lr, r0
71	17d46:	eb6e 0101	sbc.w	r1, lr, r1
72	17d4a:	f5b1 1f80	cmp.w	r1, #1048576 ; 0x100000
73	17d4e:	d31b	bcc.n	17d88 <__adddf3+0x124>
74	17d50:	f5b1 1f00	cmp.w	r1, #2097152 ; 0x200000
75	17d54:	d30c	bcc.n	17d70 <__adddf3+0x10c>
76	17d56:	0849	lsrs	r1, r1, #1
77	17d58:	ea5f 0030	movs.w	r0, r0, rrx
78	17d5c:	ea4f 0c3c	mov.w	ip, ip, rrx
79	17d60:	f104 0401	add.w	r4, r4, #1
80	17d64:	ea4f 5244	mov.w	r2, r4, lsl #21
81	17d68:	f512 0f80	cmn.w	r2, #4194304 ; 0x400000
82	17d6c:	f080 809a	bcs.w	17ea4 <__adddf3+0x240>
83	17d70:	f1bc 4f00	cmp.w	ip, #2147483648 ; 0x80000000
84	17d74:	bf08	it	eq
85	17d76:	ea5f 0c50	movseq.w	ip, r0, lsr #1
86	17d7a:	f150 0000	adcs.w	r0, r0, #0
87	17d7e:	eb41 5104	adc.w	r1, r1, r4, lsl #20
88	17d82:	ea41 0105	orr.w	r1, r1, r5
89	17d86:	bd30	pop	{r4, r5, pc}
90	17d88:	ea5f 0c4c	movs.w	ip, ip, lsl #1
91	17d8c:	4140	adcs	r0, r0
92	17d8e:	eb41 0101	adc.w	r1, r1, r1
93	17d92:	f411 1f80	tst.w	r1, #1048576 ; 0x100000
94	17d96:	f1a4 0401	sub.w	r4, r4, #1
95	17d9a:	d1e9	bne.n	17d70 <__adddf3+0x10c>
96	17d9c:	f091 0f00	teq	r1, #0
97	17da0:	bf04	itt	eq
98	17da2:	4601	moveq	r1, r0
99	17da4:	2000	moveq	r0, #0
100	17da6:	fab1 f381	clz	r3, r1
101	17daa:	bf08	it	eq
102	17dac:	3320	addeq	r3, #32
103	17dae:	f1a3 030b	sub.w	r3, r3, #11
104	17db2:	f1b3 0220	subs.w	r2, r3, #32
105	17db6:	da0c	bge.n	17dd2 <__adddf3+0x16e>
106	17db8:	320c	adds	r2, #12
107	17dba:	dd08	ble.n	17dce <__adddf3+0x16a>

108	17dbc:	f102 0c14	add.w	ip, r2, #20	
109	17dc0:	f1c2 020c	rsb	r2, r2, #12	
110	17dc4:	fa01 f00c	lsl.w	r0, r1, ip	
111	17dc8:	fa21 f102	lsr.w	r1, r1, r2	
112	17dcc:	e00c	b.n	17de8 <__adddf3+0x184>	
113	17dce:	f102 0214	add.w	r2, r2, #20	
114	17dd2:	bfd8	it	le	
115	17dd4:	f1c2 0c20	rsble	ip, r2, #32	
116	17dd8:	fa01 f102	lsl.w	r1, r1, r2	
117	17ddc:	fa20 fc0c	lsr.w	ip, r0, ip	
118	17de0:	bfdc	itt	le	
119	17de2:	ea41 010c	orr.le.w	r1, r1, ip	
120	17de6:	4090	lsl.le	r0, r2	
121	17de8:	1ae4	subs	r4, r4, r3	
122	17dea:	bfa2	ittt	ge	
123	17dec:	eb01 5104	addge.w	r1, r1, r4, lsl #20	
124	17df0:	4329	orrge	r1, r5	
125	17df2:	bd30	popge	{r4, r5, pc}	
126	17df4:	ea6f 0404	mvn.w	r4, r4	
127	17df8:	3c1f	subs	r4, #31	
128	17dfa:	da1c	bge.n	17e36 <__adddf3+0x1d2>	
129	17dfc:	340c	adds	r4, #12	
130	17dfe:	dc0e	bgt.n	17e1e <__adddf3+0x1ba>	
131	17e00:	f104 0414	add.w	r4, r4, #20	
132	17e04:	f1c4 0220	rsb	r2, r4, #32	
133	17e08:	fa20 f004	lsr.w	r0, r0, r4	
134	17e0c:	fa01 f302	lsl.w	r3, r1, r2	
135	17e10:	ea40 0003	orr.w	r0, r0, r3	
136	17e14:	fa21 f304	lsr.w	r3, r1, r4	
137	17e18:	ea45 0103	orr.w	r1, r5, r3	
138	17e1c:	bd30	pop	{r4, r5, pc}	
139	17e1e:	f1c4 040c	rsb	r4, r4, #12	
140	17e22:	f1c4 0220	rsb	r2, r4, #32	
141	17e26:	fa20 f002	lsr.w	r0, r0, r2	
142	17e2a:	fa01 f304	lsl.w	r3, r1, r4	
143	17e2e:	ea40 0003	orr.w	r0, r0, r3	
144	17e32:	4629	mov	r1, r5	
145	17e34:	bd30	pop	{r4, r5, pc}	
146	17e36:	fa21 f004	lsr.w	r0, r1, r4	
147	17e3a:	4629	mov	r1, r5	
148	17e3c:	bd30	pop	{r4, r5, pc}	
149	17e3e:	f094 0f00	teq	r4, #0	
150	17e42:	f483 1380	eor.w	r3, r3, #1048576 ; 0x100000	
151	17e46:	bf06	itte	eq	
152	17e48:	f481 1180	eoreq.w	r1, r1, #1048576 ; 0x100000	
153	17e4c:	3401	addeq	r4, #1	
154	17e4e:	3d01	subne	r5, #1	
155	17e50:	e74e	b.n	17cf0 <__adddf3+0x8c>	
156	17e52:	ea7f 5c64	mvns.w	ip, r4, asr #21	
157	17e56:	bf18	it	ne	
158	17e58:	ea7f 5c65	mvnsne.w	ip, r5, asr #21	

```

159 17e5c: d029      beq.n  17eb2 <__addddf3+0x24e>
160 17e5e: ea94 0f05    teq r4, r5
161 17e62: bf08        it  eq
162 17e64: ea90 0f02    teqeq  r0, r2
163 17e68: d005      beq.n  17e76 <__addddf3+0x212>
164 17e6a: ea54 0c00    orrs.w  ip, r4, r0
165 17e6e: bf04        itt eq
166 17e70: 4619      moveq  r1, r3
167 17e72: 4610      moveq  r0, r2
168 17e74: bd30      pop {r4, r5, pc}
169 17e76: ea91 0f03    teq r1, r3
170 17e7a: bf1e      ittt   ne
171 17e7c: 2100      movne  r1, #0
172 17e7e: 2000      movne  r0, #0
173 17e80: bd30      popne  {r4, r5, pc}
174 17e82: ea5f 5c54    movs.w  ip, r4, lsr #21
175 17e86: d105      bne.n  17e94 <__addddf3+0x230>
176 17e88: 0040      lsls   r0, r0, #1
177 17e8a: 4149      adcs   r1, r1
178 17e8c: bf28      it  cs
179 17e8e: f041 4100    orrcs.w r1, r1, #2147483648 ; 0x80000000
180 17e92: bd30      pop {r4, r5, pc}
181 17e94: f514 0480    adds.w  r4, r4, #4194304   ; 0x400000
182 17e98: bf3c      itt  cc
183 17e9a: f501 1180    addcc.w r1, r1, #1048576   ; 0x100000
184 17e9e: bd30      popcc  {r4, r5, pc}
185 17ea0: f001 4500    and.w  r5, r1, #2147483648 ; 0x80000000
186 17ea4: f045 41fe    orr.w  r1, r5, #2130706432 ; 0x7f000000
187 17ea8: f441 0170    orr.w  r1, r1, #15728640   ; 0xf00000
188 17eac: f04f 0000    mov.w  r0, #0
189 17eb0: bd30      pop {r4, r5, pc}
190 17eb2: ea7f 5c64    mvns.w  ip, r4, asr #21
191 17eb6: bf1a      itte   ne
192 17eb8: 4619      movne  r1, r3
193 17eba: 4610      movne  r0, r2
194 17ebc: ea7f 5c65    mvnseq.w ip, r5, asr #21
195 17ec0: bf1c      itt  ne
196 17ec2: 460b      movne  r3, r1
197 17ec4: 4602      movne  r2, r0
198 17ec6: ea50 3401    orrs.w  r4, r0, r1, lsl #12
199 17eca: bf06      itte   eq
200 17ecc: ea52 3503    orrseq.w r5, r2, r3, lsl #12
201 17ed0: ea91 0f03    teqeq  r1, r3
202 17ed4: f441 2100    orrne.w r1, r1, #524288 ; 0x80000
203 17ed8: bd30      pop {r4, r5, pc}
204 17eda: bf00      nop

```

Code Block 4. Arm Software Floating Point Addition Implementation

This isn't even the full code. This is a function that our calculation function has to run each time it wants to add two doubles together. Also, note that it is not just a straight shot of 202 instructions, because you can see that there are loops in the code



where ever you see an instruction's mnemonic that starts with the letter **b** (stands for branch).

## Other Use Cases

- Correlate degrees to radians (assuming degrees are whole numbers)
- Table of cosine or sine given radians or degrees
  - In the radians case, you will need to create your own trivial hashing function to convert radians to an index
- Finding a number of bits SET in a 32-bit number
  - Without a lookup table time complexity is  $O(n)$  where ( $n = 32$ ), the number of bits you want to look through
  - With a lookup table, the time complexity is  $O(1)$ , constant time, and only needs the followin operations
    - 3 bitwise left shifts operations
    - 4 bitwise ANDS operations
    - 4 load from memory addresses
    - 4 binary ADD operations
    - Total of 15 operations total

```

1  /* Found this on wikipedia! */
2
3  /* Pseudocode of the lookup table 'uint32_t bits_set[256]' */
4  /*
5     0b00, 0b01, 0b10, 0b11, 0b100, 0b101, ... */
6  int bits_set[256] = {    0,    1,    1,    2,    1,    2, // 200+ more entries
7
8  /* (this code assumes that 'int' is an unsigned 32-bits wide integer) */
9  int count_ones(unsigned int x) {
10     return bits_set[ x      & 255] + bits_set[(x >> 8) & 255]
11     + bits_set[(x >> 16) & 255] + bits_set[(x >> 24) & 255];
12 }

```

*Code Block 5. Bits set in a 32-bit number (Found this on wikipedia (look up tables))*

**i** There are far more use cases then this, but these are a few.

## Lookup Table Decision Tree

Lookup tables can be used as elegant ways to structure information. In this case, they may not provide a speed up but they will associate indexes with something greater, making your code more readable and easier to maintain. In this example, we will be looking at a matrix of function pointers.

### Example: Replace Decision Tree

See the function below:

```

1 void makeADecisionRobot(bool power_system_nominal, bool no_obstacles_ahead)
2 {
3     if(power_system_nominal && no_obstacles_ahead) {
4         moveForward();
5     }
6     else if(power_system_nominal && !no_obstacles_ahead) {

```

```
7     moveOutOfTheWay();
8 }
9 else if(!power_system_nominal && no_obstacles_ahead) {
10     slowDown();
11 }
12 else {
13     emergencyStop();
14 }
15 }
```

Code Block 6. Typical Decision Tree

```
1 void (* decision_matrix[2][2])(void) =
2 {
3     [1][1] = moveForward,
4     [1][0] = moveOutOfTheWay,
5     [0][1] = slowDown,
6     [0][0] = emergencyStop,
7 };
8
9 void makeADecisionRobot(bool power_system_nominal, bool no_obstacles_ahead)
10 {
11     decision_matrix[power_system_nominal][no_obstacles_ahead]();
12 }
```

Code Block 7. Lookup Table Decision Tree

The interesting thing about the decision tree is that it is also more optimal in that, it takes a few instructions to do the look up from memory, then the address of the procedure [function] is looked up and executed, where the former required multiple read instructions and comparison instructions.

- ✔ This pattern of lookup table will be most useful to us for the interrupts lab assignment.