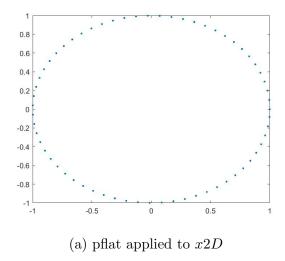
Assignment 1

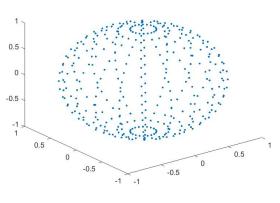
Tobias Björk

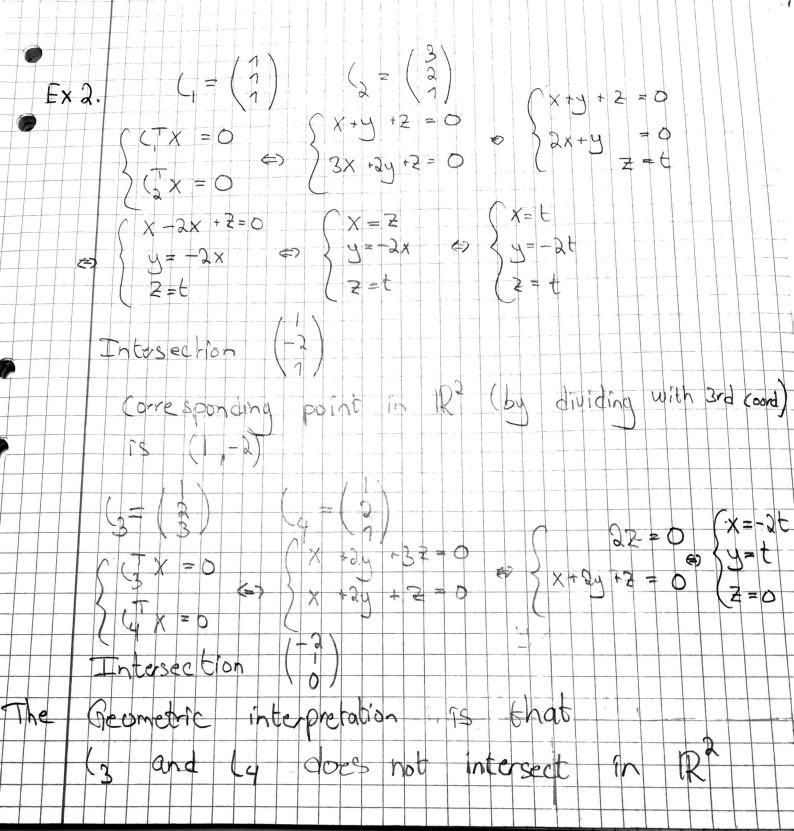
January 2022

Exercise 1

- $x_1 = (2, -1)$
- $x_2 = (-3, 2)$
- $x_3 = (2, -1)$
- The interpretation of x_4 is a vanishing point infinitely far away in the (4, -2) direction.







Seen as be can and due X and homogenous coor 1 mates duality hence DY intersection from Colleula sions: earlie

When solving for the intersection Point we look for a point that satisfies the equation of both lines. has the equation ax by + CZ =0 Cine in P2 2=0 (3 2 1) 3x + 24 + 3 the solution (x) Therfore hull space to the matrix. The intersection then in the null space Wall space : Cine of points there Is an infinitely amount of points

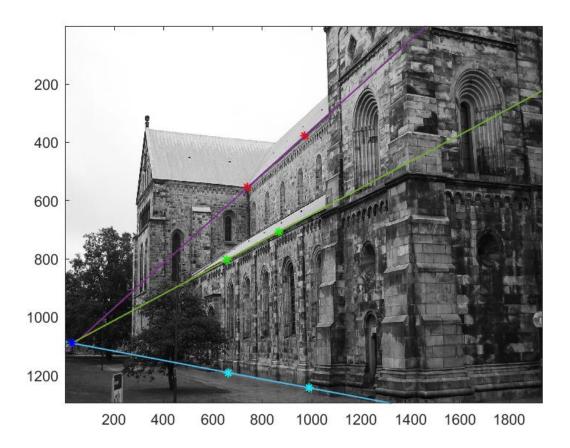


Figure 2: Plot of the points in p1 (red), p2 (green), p3 (cyan) together with the lines that goes through them. The intersect (blue) is also plotted.

- The lines look to be parallel in 3D and that's why they should intersect in the image.
- d = 8.1950 which is quite close given the scaling of the picture. All 3 lines almost intersect at the same point in this picture. This is because they are parallel in \mathbb{R}^3 . There could be some noise which explains why they all do not intersect perfectly.

Exercise 4

•
$$y_1 = (1, 0, 0)^T$$

•
$$y_2 = (1, 1, 1)^T$$

•
$$l_1 = (-1, -1, 1)^T$$

•
$$l_2 = (0, -1, 1)^T$$

$$\bullet \ (H^{-1})^T = l_2$$

•
$$y \sim Hx$$

$$0 = l_1^T x = l_1^T H^{-1} H x = l_1^T H^{-1} y = ((H^{-1})^T l_1)^T y = l_2^T y$$

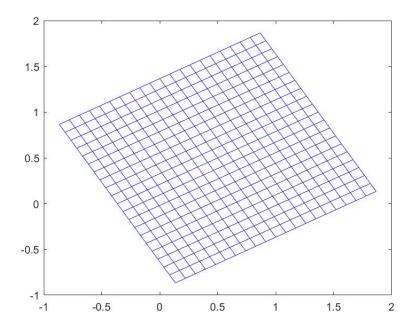


Figure 3: H_1 is an euclidean transformation since the original points have only been rotated. Both angles, parallel lines and distance between points are preserved. The digit in the right corner is not 1, but factorizing out a 2 solves the problem and shows that the matrix has the right form.

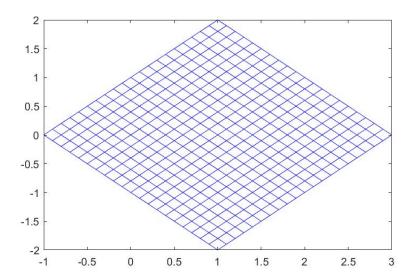


Figure 4: H_2 has both rotated and scaled the points. Angles between lines are still preserved so this is a similarity transform. Parallel lines are also preserved, but lengths are not.

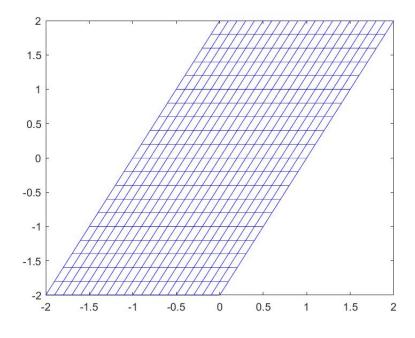


Figure 5: H_3 is an affine transform which map parallel lines to parallel lines. Angles are not preserved and lengths between points are not preserved.

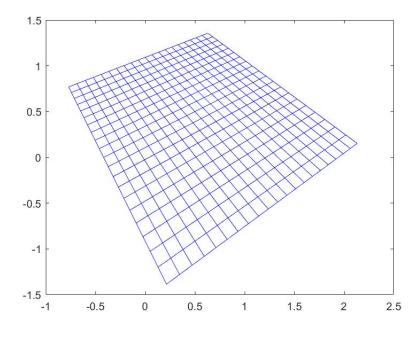


Figure 6: H_4 is a projective transformation. This can be seen upon inspecting the last row of the matrix which does not match the affine form. Parallel lines, angles and distance between points are not preserved.

Exercise 5

- Projection of $X_1 = (0.25, 0.5)$
- Projection of $X_2 = (0.5, 0.5)$
- The interpretation of the projection of X_3 is that it's a point at infinity (because it projects to (1,1,0). Direction (1,1)
- \bullet Camera center: (0,0,-1) (null space of P)
- Viewing direction: (0,0,1) (element 1-3 in the third row of P)

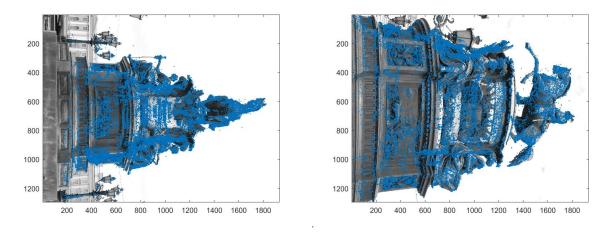


Figure 7: U projected in P1 and P2 looks very reasonable. The points seem to cover the right parts of the images.

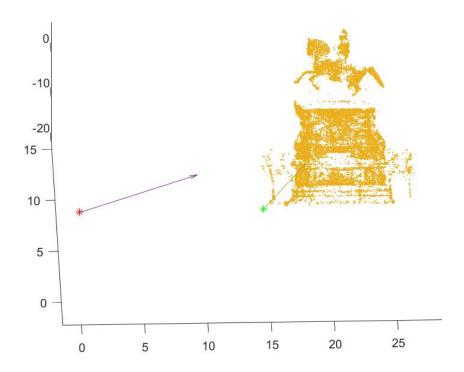


Figure 8: A plot of U, camera center of P1 (red) and camera center of P2 (green). The arrows from each center represent the viewing direction of the camera.

- Camera center for P1 = (0, 0, 0)
- Camera center for P2 = (6.64, 14.85, -15.07)
- Viewing direction of P1:(0.313, 0.946, 0.084)
- Viewing direction of P2: (0.032, 0.340, 0.940)