

**Project 1(a):**

For the model used in introductory physics courses, a projectile thrown vertically at some initial velocity  $v_i$  has position  $y(t) = y_i + v_i t - \frac{1}{2}gt^2$ , where  $g = 9.8 \text{ m/s}^2$ . Write a Python program that creates two lists, one containing time data (50 data points over 5 seconds) and the other containing the corresponding vertical position data for this projectile. The program should ask the user for the initial height  $y_i$  and initial velocity  $v_i$ , and should print a nicely-formatted table of the list values after it has calculated them.

**Project 1(b):**

Write a Python Program to plot  $y(t)$  from  $t=0$  until the ball hits the ground.

## Project 2:

In nuclear physics, the semi-empirical mass formula is a formula for calculating the approximate nuclear binding energy  $B$  of an atomic nucleus with atomic number  $Z$  and mass number  $A$ :

$$B = a_1 A - a_2 A^{2/3} - a_3 \frac{Z^2}{A^{1/3}} - a_4 \frac{(A - 2Z)^2}{A} + \frac{a_5}{A^{1/2}},$$

where, in units of millions of electron volts, the constants are  $a_1 = 15.67$ ,  $a_2 = 17.23$ ,  $a_3 = 0.75$ ,  $a_4 = 93.2$ , and

$$a_5 = \begin{cases} 0 & \text{if } A \text{ is odd,} \\ 12.0 & \text{if } A \text{ and } Z \text{ are both even,} \\ -12.0 & \text{if } A \text{ is even and } Z \text{ is odd.} \end{cases}$$

- Write a program that takes as its input the values of  $A$  and  $Z$ , and prints out the binding energy for the corresponding atom. Use your program to find the binding energy of an atom with  $A = 58$  and  $Z = 28$ . (Hint: The correct answer is around 490 MeV.)
- Modify your program to print out not the total binding energy  $B$ , but the binding energy per nucleon, which is  $B/A$ .
- Now modify your program so that it takes as input just a single value of the atomic number  $Z$  and then goes through all values of  $A$  from  $A = Z$  to  $A = 3Z$ , to find the one that has the largest binding energy per nucleon. This is the most stable nucleus with the given atomic number. Have your program print out the value of  $A$  for this most stable nucleus and the value of the binding energy per nucleon.
- Modify your program again so that, instead of taking  $Z$  as input, it runs through all values of  $Z$  from 1 to 100 and prints out the most stable value of  $A$  for each one. At what value of  $Z$  does the maximum binding energy per nucleon occur? (The true answer, in real life, is  $Z = 28$ , which is nickel. You should find that the semi-empirical mass formula gets the answer roughly right, but not exactly.)

### Project 3:

A mass  $m$  is suspended from a spring of spring constant  $k$ . The mass is displaced from equilibrium by an initial distance  $y_o$ , then released. Write a Python program to plot  $y(t)$  for some reasonable set of parameters.

For the previous problem, plot a *phase-space* plot. The horizontal axis should be position, and the vertical axis velocity.

Repeat the previous two problems, but add damping to the spring-mass system. In other words, the equation of motion for the system is

$$\ddot{y} = -\frac{k}{m}y - \beta\dot{y} .$$

Assume that  $\beta < 2\sqrt{k/m}$ .