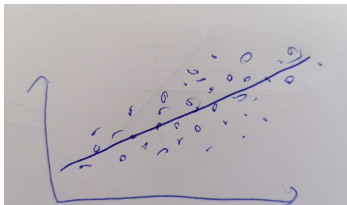


Introduction to Machine Learning

Introduction: Learners



Learning goals

- Understand the components of a learner
- Know the formalization of supervised learning
- Be able to apply the concept of a learner to a supervised learning task

COMPONENTS OF A LEARNER

Summarizing what we have seen before, nearly all supervised learning algorithms can be described in terms of three components:

Learning = Hypothesis Space + Risk + Optimization

- **Hypothesis Space:** Defines (and restricts!) what kind of model f can be learned from the data.
- **Risk:** Quantifies how well a specific model performs on a given data set. This defines how to compare observed values to predictions and allows us to rank candidate models in order to choose the best one.
- **Optimization:** Defines how to search for the best model in the **hypothesis space**, typically guided by the metric used for the **risk**.

SUPERVISED LEARNING, FORMALIZED

A **learner** (or **inducer**) \mathcal{I} is a *program* or *algorithm* which

- receives a **training set** $\mathcal{D} \in \mathcal{X} \times \mathcal{Y}$, and,
- for a given **hypothesis class** \mathcal{H} of **models** $f : \mathcal{X} \rightarrow \mathbb{R}^g$,
- based on a **risk** function $\mathcal{R}_{\text{emp}}(f)$ that quantifies the performance of $f \in \mathcal{H}$ on \mathcal{D} ,
- uses an **optimization** procedure to find

$$\hat{f} = \arg \min_{f \in \mathcal{H}} \mathcal{R}_{\text{emp}}(f).$$

As before, we can also adapt this concept to finding $\hat{\theta}$ for parametric models.

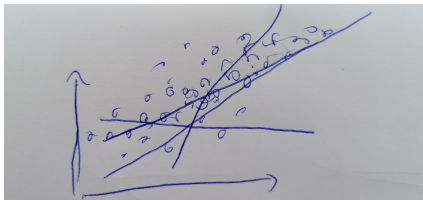
(This does not cover all special cases, but it's a useful framework for most supervised ML problems.)

EXAMPLE OF A LEARNER

Let us consider a linear regression task with a single feature and a single target variable.

- The **hypothesis space** in univariate linear regression is the set of all linear functions, with $\theta = (\theta_0, \theta)$:

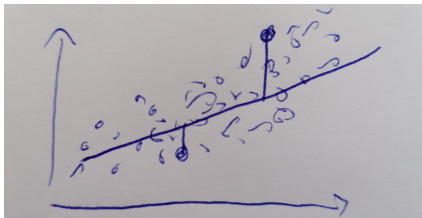
$$\mathcal{H} = \{f(\mathbf{x}) = \theta_0 + \theta \mathbf{x} : \theta_0, \theta \in \mathbb{R}\}$$



EXAMPLE OF A LEARNER

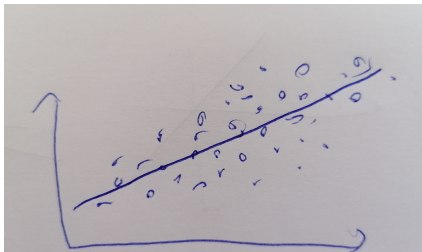
- We might use the mean squared error as loss function to our **risk**, punishing larger distances between observations and regression line more severely:

$$\mathcal{R}_{\text{emp}}(\theta) = \frac{1}{n} \sum_{i=1}^n (y^{(i)} - \theta_0 - \theta \mathbf{x}^{(i)})^2$$



EXAMPLE OF A LEARNER

- **Optimization** will usually mean deriving the ordinary-least-squares (OLS) estimator $\hat{\theta}$ analytically. We might, however, also use gradient descent or some other optimization procedure.



VARIETY OF LEARNING COMPONENTS

Hypothesis Space : {
Step functions
Linear functions
Sets of rules
Neural networks
Voronoi tessellations
...

Risk : {
Mean squared error
Misclassification rate
Negative log-likelihood
Information gain
...

Optimization : {
Analytical solution
Gradient descent
Combinatorial optimization
Genetic algorithms
...

LEARNING AS EMPIRICAL RISK MINIMIZATION

- By decomposing learners into these building blocks,
 - we have a framework to understand how they work,
 - we can more easily evaluate in which settings they may be more or less suitable, and
 - we can tailor learners to specific problems by clever choice of each of the three components.
- There will, for instance, be optimization procedures that work well for a certain combination of hypothesis space and risk function but perform poorly on others.
- In fact, it is a commonly acknowledged problem that no universally best learner exists.