## Theory of Computation, Fall 2021 Assignment 6 Solutions

## **Exercises**

- Q1. (a) True. Every Turing machine semidecides exactly one language, which is L(M).
  - (b) False. If a Turing machines does not always halt, then it does not decides any language.
  - (c) False.
- Q2. Since M decides some language, it halts on every input. Therefore, L(M) is the set of all strings over the input alphabet.
- Q3. This problem is equivalent to the language L(G), and the following Turing machine M decides this language where  $M_{C1}$  is the Turing machine we used to decide  $A_{CFG}$  in class.

```
M= on input w:

1. run M_{C1} on "G""w".

2. accept if M_{C1} accept, and reject otherwise.
```

We can conclude that every context-free language is recursive.

Q4. The problem can be expressed as

```
A = \{\text{``M"``R"}: M \text{ is a DFA and } R \text{ is a regular expression such that } L(M) = L(R)\}
```

We construct a Turing machine  $M^*$  to decide A as follows.

```
M^* =  on input "M""R":

1. convert R to an equivalent NFA, and then convert the NFA to an equivalent DFA D.

2. run M_{R5} on "M""D" (to see whether M and D are equivalent)

3. If M_{R5} accepts,

4. accept

5. else

5. reject
```

Recall that  $M_{R5}$  is the Turing machine we used in class to decide whether two DFAs are equivalent.