

AI Lab - Lesson 4

Markov Decision Process

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Start Your Working Environment

Start the previously installed (lesson 1) conda environment *ai-lab*

Listing 1: Update Environment

```
cd AI-Lab  
git stash (NB: remember to backup the previous lessons before this step!)  
git pull  
git stash pop  
conda activate ai-lab  
jupyter notebook
```

Listing 2: Open Lesson

To open the tutorial navigate with your browser to:
`lesson_4/lesson_4_problem.ipynb`

NumPy

What is it

NumPy is the fundamental package for scientific computing with Python. It contains among other things:

- *a powerful N-dimensional array object*
- *sophisticated (broadcasting) functions*
- *tools for integrating C/C++ and Fortran code*
- *useful linear algebra, Fourier transform, and random number capabilities*

What is it for

Fast array manipulation and mathematical operations. Think of it as a MATLAB like environment for Python: try to speed up the computations writing code in a vectorial fashion.

Where to find it

<http://www.numpy.org>

- Your assignments for this lesson are at:
lesson_4/lesson_4_problem.ipynb. You will be required to implement value iteration and policy iteration algorithms
- In the following you can find pseudocodes for such algorithms

Value Iteration

```
function VALUE-ITERATION(mdp,  $\epsilon$ ) returns a utility function
  inputs: mdp, an MDP with states  $S$ , actions  $A(s)$ , transition model  $P(s' | s, a)$ ,
           rewards  $R(s)$ , discount  $\gamma$ 
            $\epsilon$ , the maximum error allowed in the utility of any state
  local variables:  $U$ ,  $U'$ , vectors of utilities for states in  $S$ , initially zero
                      $\delta$ , the maximum change in the utility of any state in an iteration

  repeat
     $U \leftarrow U'$ ;  $\delta \leftarrow 0$ 
    for each state  $s$  in  $S$  do
       $U'[s] \leftarrow R(s) + \gamma \max_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s']$ 
      if  $|U'[s] - U[s]| > \delta$  then  $\delta \leftarrow |U'[s] - U[s]|$ 
  until  $\delta < \epsilon(1 - \gamma)/\gamma$ 
  return  $U$ 
```

Policy Iteration

```
function POLICY-ITERATION(mdp) returns a policy
inputs: mdp, an MDP with states  $S$ , actions  $A(s)$ , transition model  $P(s' | s, a)$ 
local variables:  $U$ , a vector of utilities for states in  $S$ , initially zero
                   $\pi$ , a policy vector indexed by state, initially random

repeat
     $U \leftarrow \text{POLICY-EVALUATION}(\pi, U, \text{mdp})$ 
    unchanged?  $\leftarrow$  true
    for each state  $s$  in  $S$  do
        if  $\max_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s'] > \sum_{s'} P(s' | s, \pi[s]) U[s']$  then do
             $\pi[s] \leftarrow \operatorname{argmax}_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s']$ 
            unchanged?  $\leftarrow$  false
until unchanged?
return  $\pi$ 
```

To implement the *Policy-Evaluation* step, use the following formula:

$$U_i(s) = R(s) + \gamma \sum_{s'} P(s' | s, \pi_i(s)) U_i(s').$$