

26/01/2016

1)  $f(x) = \frac{4}{x^2+2} - \frac{2}{x^2+1}$

$$= \frac{4}{\frac{x^2+2}{x}} - \frac{2}{\frac{x^2+1}{x}} = 4 \cdot \frac{x}{x^2+2} - 2 \cdot \frac{x}{x^2+1} = \frac{4x}{x^2+2} - \frac{2x}{x^2+1} = \frac{4x(x^2+1) - 2x(x^2+2)}{(x^2+2)(x^2+1)} =$$

$$= \frac{(4x^3+4x) - (2x^3+4x)}{x^4+x^2+2x^2+2} = \frac{2x^3}{x^4+3x^2+2}$$

$c = \frac{x \cdot f'(x)}{f(x)}$

derivata =  $\left(\frac{f}{g}\right)' = \frac{f' \cdot g - f \cdot g'}{g^2} =$

$$= \frac{2(3x^2) \cdot x^4+3x^2+2 - 2x^3 \cdot 4x^3+3 \cdot (2x)+0}{(x^4+3x^2+2)^2} = \frac{6x^2(x^4+3x^2+2) - 2x^3(4x^3+6x)}{(x^4+3x^2+2)^2} =$$

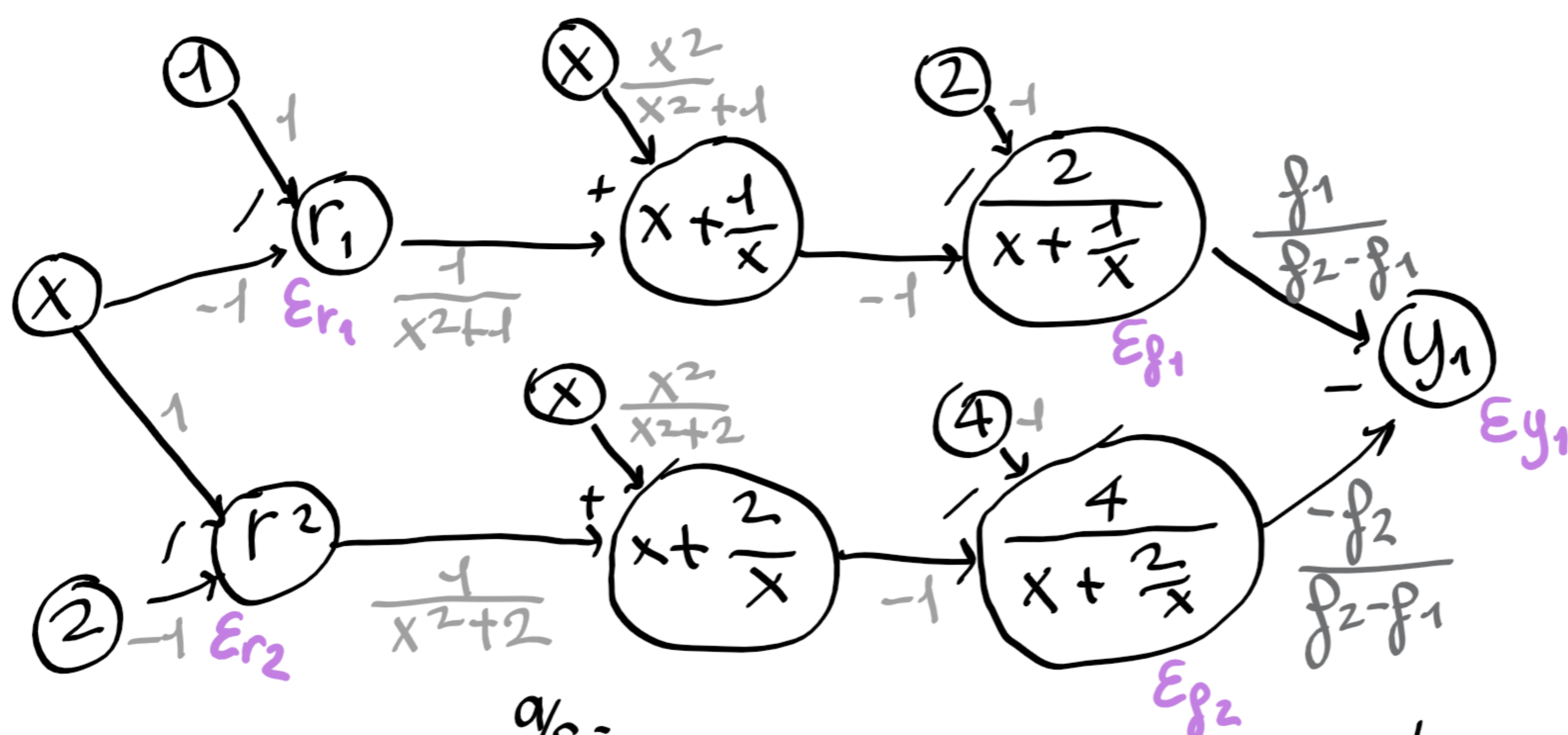
$$= \frac{(6x^6+18x^4+12x^2) - (8x^6+12x^4)}{(x^4+3x^2+2)^2} = \frac{-2x^6+6x^4+12x^2}{(x^4+3x^2+2)^2}$$

$$x \cdot \frac{(-2x^6+6x^4+12x^2)}{(x^4+3x^2+2)^2} \cdot \frac{x^4+3x^2+2}{2x^3} = \frac{-2x^7+6x^5+12x^3}{2x^3(x^4+3x^2+2)} = \frac{-2x^3(x^4-3x^2-6)}{2x^3(x^4+3x^2+2)} =$$

$$= \frac{-(x^4-3x^2-6)}{x^4+3x^2+2} = \frac{-x^4+3x^2+6}{x^4+3x^2+2}$$

$\lim_{x \rightarrow 0} (c) = \lim_{x \rightarrow 0} \frac{-x^4+3x^2+6}{x^4+3x^2+2} = \frac{6}{2} = 3$

$a_1 = r_1 = 1/x; r_2 = 2/x; f_1 = \frac{2}{x+r_1}; f_2 = \frac{4}{x+r_2}; y = f_2 - f_1$



$a/c = \frac{x}{x^2+1} \rightarrow \frac{x}{\frac{x^2+1}{x}} = x \cdot \frac{x}{x^2+1} = \frac{x^2}{x^2+1} \rightarrow b/c = \frac{1}{\frac{x^2+1}{x}} = \frac{1}{x} \cdot \frac{x}{x^2+1} = \frac{1}{x^2+1}$

$\epsilon_{a_1} = \epsilon_{r_1} \left\{ \frac{1}{x^2+1} \cdot (-1) \cdot \epsilon_{f_1} \right\} + \epsilon_{r_2} \left\{ \frac{1}{x^2+2} \cdot (-1) \cdot \epsilon_{f_2} \right\} + \epsilon_{f_1} \left\{ \frac{f_1}{f_2-f_1} \right\} + \epsilon_{f_2} \left\{ \frac{-f_2}{f_2-f_1} \right\} + \epsilon_{y_1}$



$$f(x) = \frac{3x-2}{3x+2} - \frac{x-3}{x+3}$$

$$= \frac{(3x-2)(x+3) - (x-3)(3x+2)}{(3x+2)(x+3)} = \frac{(3x^2 + 9x - 2x - 6) - (3x^2 + 2x - 9x - 6)}{3x^2 + 11x + 6} =$$

$$= \frac{3x^2 + 9x - 2x - 6 - 3x^2 - 2x + 9x + 6}{3x^2 + 11x + 6} = \frac{18x - 4x}{3x^2 + 11x + 6} = \frac{14x}{3x^2 + 11x + 6}$$

$$\text{der} \left( \frac{f}{g} \right)' = \frac{f'g - f \cdot g'}{g^2} = \frac{14 \cdot (3x^2 + 11x + 6) - (14x) \cdot (6x + 11 + 0)}{(3x^2 + 11x + 6)^2} =$$

$$\frac{(42x^2 + 154x + 84) - (84x^2 + 154x)}{(3x^2 + 11x + 6)^2} = \frac{42x^2 + 154x + 84 - 84x^2 - 154x}{(3x^2 + 11x + 6)^2} =$$

$$= \frac{-42x^2 + 84}{(3x^2 + 11x + 6)^2}$$

$$C = \frac{x \cdot f'(x)}{f(x)} = x \cdot \frac{-42x^2 + 84}{(3x^2 + 11x + 6)^2} \cdot \frac{3x^2 + 11x + 6}{14x} = \frac{14(-3x^2 + 6)}{3x^2 + 11x + 6} \cdot \frac{1}{14} = \frac{-3x^2 + 6}{3x^2 + 11x + 6}$$

$$\lim_{x \rightarrow -\infty} = \frac{-\infty}{\infty} = -1$$

alg<sub>1</sub> :  $f_1 = \frac{3x-2}{3x+2}$      $f_2 = \frac{x-3}{x+3}$      $y_1 = f_1 - f_2$

