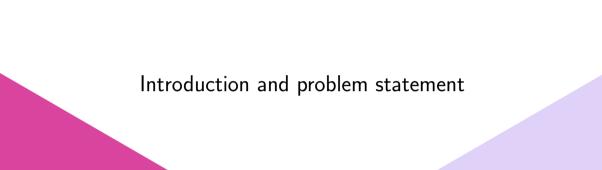


Overview



- 1. Introduction and problem statement
- 2. TD-methods with discretization
- 3. SARSA with function approximation
- 4. DQN
- 5. Final results
- 6. Conclusions





Problem statement

The project tackles the problem of the "LunarLander-v2", an environment of OpenAl gym (https://www.gymlibrary.ml/environments/box2d/lunar_lander/) [3].

The **goal** is to land a shuttle on the moon.

Start

► The lander starts at the top center of the viewport with a random initial force applied to its center of mass.

Termination:

- 1. The lander's body gets in contact with the moon;
- 2. The lander gets outside of the viewport.

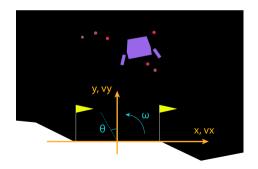


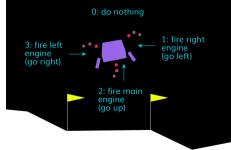
States - continuous

▶ 8 variables: 6 continuous $(x, y, v_x, v_y, \theta, \omega)$ and 2 booleans.

Actions - discrete

▶ 4 actions: do nothing, fire right (go left), fire main, fire left (go right).







Reward structure

Positive reward when:

- Moving towards the landing pad;
- ightharpoonup Coming to rest (+100 points);
- ▶ Leg on the ground (+10 points. each)

Negative reward when:

- Moving away from the landing pad;
- ▶ Lander crashes (-100 points);
- Fire main engine (-0.3 points), fire left/right engine (-0.03 points).

The game is considered solved with 200 points.



Model-free problem, with continuous states.

To solve the problem different approaches can be used. In the project the following algorithms were implemented:

- 1. TD-methods with discretization
- 2. SARSA with non-linear function approximation
- 3. DQN

TD-methods with discretization

TD-methods with discretization



Discretization

Set $I=[var_{min},var_{max}]$ for each variable var - the interval is divided in n bins; in additions, two bins collect all the observations that fall outside the minimum/maximum of I, respectively.

Discretization: equally sized bins with with reasonable choice of minimum/maximum values.

Complexity: Huge state space

$$\begin{split} O(x\times y\times v_x\times v_y\times \theta\times \omega\times \mathsf{bool}_1\times \mathsf{bool}_2) &= \\ &= O(6\times 4\times 4\times 4\times 4\times 4\times 2\times 2) = \\ &= 24576 \end{split}$$

TD-methods with discretization



SARSA (on-policy TD control)

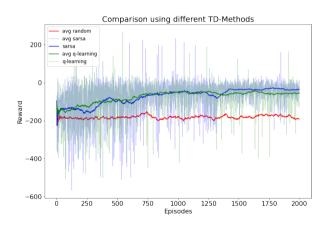
```
Inputs: step size \alpha \in (0,1], small \varepsilon > 0;
Initialize Q(s, a), for all s \in \mathcal{S}, a \in \mathcal{A}(s).
 arbitrarily except that Q(\text{terminal}, \cdot) = 0:
foreach episode do
     Initialize S:
     Choose A from S using policy derived
       from Q (e.g., \varepsilon-greedy);
     foreach step of episode do
           Take action A, observe R, S':
           Choose A' from S' using policy
             derived from Q (e.g., \varepsilon-greedy):
           Q(S, A) \leftarrow Q(S, A) + \alpha[R + \gamma]
            Q(S',A') - Q(S,A);
           S, A \leftarrow S', A':
     end foreach
     until S is terminal
end foreach
```

Q-learning (off-policy TD control)

```
Inputs: step size \alpha \in (0, 1], small \varepsilon > 0:
Initialize Q(s, a), for all s \in \mathcal{S}, a \in \mathcal{A}(s),
  arbitrarily except that Q(\text{terminal}, \cdot) = 0;
foreach episode do
      Initialize S.
     foreach step of episode do
           Choose A from S using policy
             derived from Q (e.g., \varepsilon-greedy);
           Take action A, observe R, S':
           Q(S, A) \leftarrow Q(S, A) + \alpha [R + \gamma]
             \max_a Q(S', a) - Q(S, A)];
           S \leftarrow S':
     end foreach
end foreach
```

TD-methods with discretization Results





- Both SARSA and Q-learning perform poorly, as expected
- Discretization is not rich enough to describe the continuous states
- Insufficient exploration

SARSA with function approximation

SARSA with function approximation



The general idea is to:

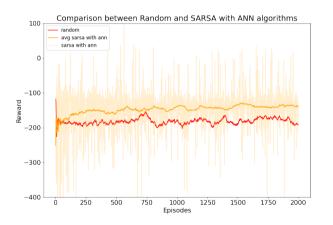
- 1. Compute the Q-values with function approximation instead of using the Q-table
- 2. Update approximation given the past experience

In this project, a semi-gradient SARSA with non-linear function approximation through ANN was implemented.

$$Q(S, a) \approx ANN, \quad a \in A$$

SARSA with function approximation Results





- Poor performance, worse than expected
- Possible explanation: update of all weights of an action network combined with highly correlated observations
- Possible solution: use batches of observations, not feasible for standard on-policy





Deep reinforcement learning method proposed by DeepMind [4].

It is a Q-learning algorithm that uses ANN to approximate the state-action value function.

Some techniques are used to improve and stabilize the learning:

- 1. ε-greedy policy
- 2. Experience replay
- 3. Target network

Experience replay



Problem: sequence of experience tuples (s, a, r, s') derived from the interaction of the agent with the environment is auto-correlated.

Solution: the idea is to store a history of experience tuples in a memory. This allows to:

use mini-batches of experiences drawn at random from the stored samples, instead of using a single experience tuple. This should lead to more stable training and better convergence.



Target network

Problem: target values change continuously as the parameters of the network change with each iteration. This can make the learning unstable.

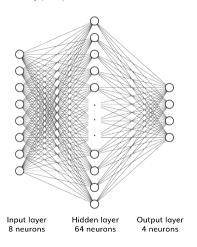
Solution: use an additional target network.

- ▶ the **main network** is only used for calculating the Q-values for selecting the next action and is trained every update_every step;
- ▶ the target network is used for computing the target Q-values to update the main model. This network is updated every update_every step. soft update:

$$w'_{\texttt{target}} = (1 - \tau) \cdot w_{\texttt{target}} + \tau \cdot w_{\texttt{main}}$$

Networks and hyperparameters

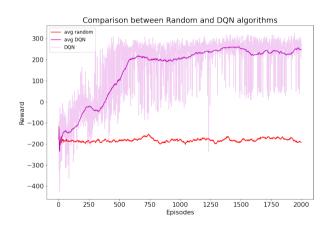




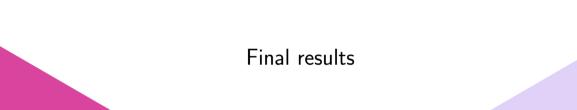
- $r = 5e^{-4}$
- $\gamma = 0.99$
- ightharpoonup ε decays over episodes
- ightharpoonup update_every = 4
- ightharpoonup buffer_size = 1e5
- ▶ batch_size = 64
- au = 1e 3

DQN Results





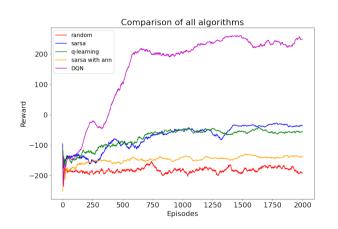
- Good performance as expected;
- The winning condition is reached;
- ▶ To reach the winning condition only \sim 600 episodes are needed.



Final results

Comparison





| | Max Avg Reward |
|------------|----------------|
| SARSA | -26.62 |
| Q-learning | -39.73 |
| ANN SARSA | -128.54 |
| DQN | 261.36 |

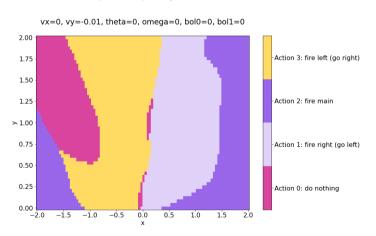
 DQN largely outperforms the other methods, as expected

Final results

DQN policy visualization

, ...

Can we interpret the learned optimal policy?



Final results

DQN: watch the lunar lander successfully landing on the moon!







Conclusions



To sum up:

Different model-free critic-only methods have been implemented and compared:

- ▶ **SARSA** and **Q-learning** need discretization to be applied. Performance is low as expected, discretization is neither rich enough to describe the continuous states, nor feasible for a good exploration;
- ▶ SARSA with ANN function approximation works directly on continuous states. Performance is even worse, a guess is that the weights update with highly correlated observations and without batches negatively affects the learning;
- ▶ **DQN** works directly on continuous states. Very good performance, it solved the environment in a small number of epochs.

Conclusions



What else we could have done, which was outside the scope of the project:

- Experiment with richer discretization;
- Perform a more in-depth parameters tuning, in all algorithms but especially in the ones based on ANN;
- Use some stochastic policy methods, which are a common alternative in the case of continuous states.



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