

# Pathological Tasks

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## Sommario

### 1 Introduction

The problems discussed below were first proposed by Hochreiter and Schmidhuber [1] as examples of difficult problems because they require learning long term correlations and have been commonly used as benchmark tasks since.

### 2 Temporal order problem

### 3 Addition problem

The problem consists in performing an addition between two real numbers  $x_i$  and  $x_j$  in  $[-1.1]$  belonging to a sequence of randomly generated numbers. The difficulty in this problem is that such numbers can be arbitrarily distant in the input sequence, so the learning net must exhibit a long term memory. More specifically the input is a sequence of pairs; each pair is composed of a real number and a marker which can be in  $\{1, 0\}$ . The marker is used to select the two numbers in the sequence to add. The prediction is the last value in the output sequence, the target is  $\frac{x_i+x_j}{2}$ . The prediction  $y$  is considered correct if  $|y - \frac{x_i+x_j}{2}| < 0.04$ .

Sequences have random length, say  $L$ , between the minimal sequence length  $T$  and  $T + \frac{T}{10}$ , the position of the first marker is sampled in first  $\frac{L}{10}$  positions, the last marker is instead sampled in  $[\frac{4L}{10}, \frac{5L}{10}]$

### 4 Multiplication problem

The problem is very similar to the addition problem, here we select two numbers in the input sequences of real numbers in  $[0, 1]$  and we need to predict the product.

## 5 Random permutation problem

## **Riferimenti bibliografici**

- [1] Sepp Hochreiter and Jürgen Schmidhuber. Long short-term memory, 1995.