# Development plan for the linearization about a rotational speed set-point in OpenFAST

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#### Introduction

This document describes the implementation of an algorithm to perform linearization about a rotational set-point in *OpenFAST*. Currently, the user needs to manually adjust operating parameters until the desired rotational speed is reached, or until the transient are eliminated, before the linearization can be performed. This procedure is here automatized using a simple iterative algorithm. The method supports simulations with zero rotational speed, a fixed rotational speed (generator off), or simulations with a variable speed (generator on). In the later case, the algorithm presented adjusts one of the following operating parameter to reach the target rotational speed: the blade pitch angle, the generator torque or the neutral yaw position of the turbine. A proportional gain on the rotational speed error is used to adjust the parameters. To speed-up the convergence, the damping may be artificially increased in the iteration step. At the end of the iteration algorithm, the transient have dissipated, the rotor is at the target rotational speed and a steady or periodic operating point is reached. The linearization is then performed for one rotor revolution (if applicable) without the previously added damping. The algorithm is such that it only involves modifications of the *OpenFAST* glue-code and of ServoDyn.

# 1 OpenFAST implementation

### 1.1 Basic workflow and changes to the code

The basic workflow is listed below. More details follow in subsequent sections.

- New parameters are read from the input files (given in subsection 1.2)
- If the parameter CalcSteady is false, *OpenFAST* the linearization process will happen as before (at LinTimes)
- If CalcSteady is true, OpenFAST will iterate and update a controller parameter until the rotational speed matches the parameter RotSpeed given in ElastoDyn's input file, and then perform the linearization at this periodic operating point. A different controller variable is adjusted in the iterative step based on the value of the parameter TrimCase: the neutral yaw YawNeut, the generator torque GenTrq or the blade pitch BlPitch. The procedure follows the steps below.
- After the initialization of *ElastoDyn*, additional initialization inputs are passed to *ServoDyn* for its initialization: the glue-code inputs CalcSteady, TrimCase and TrimGain and the

reference rotational speed RotSpeedRef. These initialization inputs will be used by ServoDyn to adjust one of the controller parameter based on the current rotational speed error. If the reference rotation speed is 0 or if the generator degree of freedom is off, no controller trimming is required.

- ServoDyn is initialized. The discrete-time state CtrlOffset is added to the module to keep track of the controller parameter offset.
- The glue-code starts a special time stepping loop where a convergence criteria is checked upon after each revolution, or time step if the rotational speed is zero. The time stepping loop has the following characteristics:
  - At each time step, if the controller trimming is active, ServoDyn updates its controller offset state (CtrlOffset) based on the proportional gain TrimGain and the error in rotational speed. This offset is added to the controller commands of ServoDyn and will hence have an influence on ElastoDyn.
  - At each time step, the glue-code adds additional damping, via external forces, to the structure of the modules *ElastoDyn* and *BeamDyn*.
  - At given azimuthal positions (defined by NAzimStep), the glue-code computes the relative difference between the output vector of the current revolution and the previous revolution. If the rotational speed is zero, the difference is computed between two successive time steps and the number of azimuthal step is effectively 1.
  - When this difference is below the tolerance TrimTol for all the reference azimuthal positions, the simulation has reached a periodic steady state, which also implies that the controller offset parameter has also converged and the rotational speed of the rotor matches the requested set-point. The time-stepping is stopped
- The linearization is performed for one rotor revolution (if applicable) at steps of NAzimStep. The operating point is at the requested rotational speed and it uses the controller offset obtained by the iteration procedure above.

The following sections describe the changes needed to the code:

- subsection 1.2: new input parameters to be added to the OpenFAST glue-code
- subsection 1.3: iterative procedure of the glue-code to ensure a periodic steady state is reached
- subsection 1.5: glue-code procedure to increase the damping and accelerate the convergence
- subsection 1.4: changes to ServoDyn to compute the controller parameter offset

#### 1.2 New glue code inputs

The following input are added to the main *OpenFAST* input file (.fst file):

- CalcSteady Calculate a steady-state periodic operating point before linearization (-) (switch)
- TrimCase Controller parameter to be trimmed {1:yaw; 2:torque; 3:pitch} [used only if CalcSteady=True]
- TrimTol Tolerance for the rotational speed convergence [>0] [used only when CalcSteady=True]

- TrimGain Proportional gain for the rotational speed error (rad/(rad/s) or Nm/(rad/s)) [>0] [used only when CalcSteady=True]
- $\bullet$  Twr\_Kdmp Damping factor for the tower (N/(m/s)) [>=0] [used only when CalcSteady=True]
- ullet Bld\_Kdmp Damping factor for the blade (N/(m/s)) [>=0] [used only when CalcSteady=True]
- NAzimStep Number of equally-spaced azimuth steps in periodic linearized model
   (-) [>=1]

Do we want to adjust more damping values? Linearization inputs are read in Fast\_Subs.f90, routine FAST\_ReadPrimaryFile about line 2273. They are returned in the structure named p or p\_FAST of type FAST\_ParameterType. The parameters above needs to be added to the FAST\_Registry.txt file as FAST\_ParameterType.

#### 1.3 Main glue-code procedure

#### Main program

- If CalcSteady is false, set Twr\_Kdmp and Bld\_Kdmp to 0 and proceed as usual
- If CalcSteady is true, follow the iterative procedure below

**Iterative procedure** The subscript p is used to refer to the *previous* time step, the subscript c is used for the *current* time step, the subscript 0 is used to refer to the target azimuthal positions. The azimuthal angle  $\psi$  at a given time step are taken from the outputs of ElastoDyn: ED%y%LSSTipPxa. The following storage variables are used by the iterative algorithm:

${f Variable}$	Dimensions	Description
$oldsymbol{\psi}_0$	$1 \times {\tt NAzimStep}$	Target azimuthal positions $\psi_0$ , indexed with the variable j
$\boldsymbol{y}_c$	$1 \times n_y$	Output vector (from all modules) at current time step
$\boldsymbol{y}_p$	$1 \times n_y$	Output vector (from all modules) at previous time step
$oldsymbol{y}_0$	$1 \times n_y$	Output vector interpolated at a target azimuthal position
$oldsymbol{Y}_0$	$n_y  imes  exttt{NAzimStep}$	Output vector at each target azimuthal positiony
$oldsymbol{\epsilon}_y$	$1 imes \mathtt{NAzimStep}$	Relative error in the output vector between two revolutions
		at the same target azimuthal position

The following steps make up the iterative procedure:



- If the generator degree of freedom is off or if the rotational speed is zero, TrimCase is set to 0 so that the trimming is cancelled. This step is done prior to the initialization of ServoDyn presented in subsection 1.4.
- If the reference rotational speed is 0, ensure that NAzimStep=1. The number of rotations is then understood as the number of time steps.
- Initialize the number of full rotor revolutions and the index of target azimuthal positions:

$$n_{\rm rot} = 0, \qquad j = 1 \tag{1}$$

• Perform time stepping until TMax (the time loop will be stopped before TMax if the convergence criteria is met). For each time step:

- Call the time step integration routine FAST\_Solution\_T. This routine applies an increased damping (based on Twr\_Kdmp and Bld\_Kdmp, see subsection 1.5) If the rotational speed is none zero and if the generator is on, ServoDyn applies an offset to the controller variables (based on  $\epsilon_{\Omega}$ , see subsection 1.4).
- Store the current azimuthal angle and output vector:  $\psi_c$  and  $\boldsymbol{y}_c$
- If t = 0 (or first time step):
  - \* Set the initial azimuthal position as  $\psi_{\text{init}} = \psi_c$  The azimuthal angle is stored as a number in the interval [0;  $2\pi$ [ ( $2\pi$  excluded), i.e.  $\psi_c = \text{mod}(\psi, 2\pi)$ , implemented as  $\psi_c = \text{Zero2TwoPi}(\psi)$ .
  - \* Set the vector of target azimuthal positions  $\psi_0$  (also in [0;  $2\pi$ ]):

$$k = 1..\mathtt{NAzimStep}, \quad \pmb{\psi}_0[k] = \mathrm{mod}(\psi_{\mathrm{init}} + (k-1)\Delta\psi, 2\pi), \quad \Delta\psi \stackrel{\triangle}{=} \frac{2\pi}{\mathtt{NAzimStep}} \quad (2)$$

- \* Set  $\boldsymbol{y}_p = \boldsymbol{y}_c$  ans  $\psi_p = \psi_c$
- If  $(\psi_c \psi_p) \ge \Delta \psi$ , return an error: the rotor is spinning too fast, the time step or NazimStep are too large
- If  $\psi_c \geq \psi_0[j]$ 
  - \* Interpolate the output vector to the target azimuthal position  $\psi_0[j]$  using the current output values  $\boldsymbol{y}_c$  and the previous ones  $\boldsymbol{y}_p$ :

if 
$$t = 0$$
 or  $\Omega_{\text{ref}} = 0$ ,  $\boldsymbol{y}_0 = \boldsymbol{y}_p$ , else  $\boldsymbol{y}_0 = \boldsymbol{y}_p + (\boldsymbol{y}_c - \boldsymbol{y}_p) \frac{\psi_0[j] - \psi_p}{\psi_c - \psi_p}$  (3)

Note: outputs that are 3D rotations should be transformed to logarithmic maps. Note: special care is needed if angles are close to 0 or  $2\pi$ , in which case they should be taken between  $-\pi$  and  $\pi$ .

\* If  $n_{\text{rot}} > 0$ , compute the mean squared relative error of the output vector at the azimuthal position  $\psi_0[j]$  between the current revolution and the previous one:

$$\epsilon_y^2[j] = \frac{1}{n_y} \sum_i \left( \frac{y_0[i] - Y_0[i, j]}{y_{\text{ref}}[i]} \right)^2$$
 (4)

The reference value  $y_{\text{ref}}$  is defined in Equation 7.

Note: if the variable  $y_0[i]$  is in radian or degree, the difference of the variable should be taken between  $-\pi$  and  $\pi$ , implemented using MPi2Pi.

\* Store the interpolated value

$$\boldsymbol{Y}_0[:,j] = \boldsymbol{y}_0 \tag{5}$$

- \* Increment j
- Set the current values as previous values for the next time step

$$\psi_p \leftarrow \psi_c, \qquad \boldsymbol{y}_p \leftarrow \boldsymbol{y}_c$$
 (6)

- If j > NAzimStep:

- \* Increment  $n_{\rm rot}$
- \* Check convergence over all azimuthal positions:  $\epsilon_u^2[k] < \texttt{TrimTol}$  for all k
- \* If converged, exit the time loop
- \* Otherwise, compute a reference value for each of the index of the output vector, based on the maximum and minimum values taken over one rotor revolution.

$$y_{\text{ref}}[i] = \max(Y_0[:,i]) - \min(Y_0[:,i])$$
 if  $y_{\text{ref}}[i] > 10^{-6}$ , else  $y_{\text{ref}}[i] = 1$  (7)

Set j = 1 and continue the time stepping.

• If the time loop run up to TMax, return an error, otherwise perform the linearization step below

#### Linearization

- The values Twr\_Kdmp and Bld\_Kdmp are set to 0
- The standard linearization procedure takes place

## 1.4 Changes in ServoDyn

In the updated implementation, ServoDyn has the possibility to modify some of its outputs based on offset that is updated internally as a discrete state.

New registry types The inputs RotSpeedRef, TrimCase, TrimGain are added:

```
InitInputType IntKi TrimCase - - - "Controller parameter to be trimmed" - InitInputType ReKi TrimGain - - - "Proportional gain on rotational speed error" - InitInputType ReKi RotSpeedRef - - - "Reference rotational speed" rad/s??
```

These inputs should also be added as ParameterType in the registry file. The discrete state CtrlOffset (also noted  $x_{\text{off}}$ ) is added:

```
DiscreteStateType ReKi CtrlOffset - - - "Controller offset parameter" -
```

Glue-code transfer before the init routine The controller trimming option of ServoDyn requires additional parameters from the glue-code and ElastoDyn. These parameters need to be transferred via the SrvD\_InitInputType structure. Currently, these transfer occur in the routine FAST\_InitializeAll of FAST\_Subs.f90. The following transfer is added:

```
InitInData_SrvD%TrimCase = p_FAST%TrimCase
InitInData_SrvD%TrimGain = p_FAST%TrimGain
InitInData_SrvD%RotSpeedRef = ED%Outpu () )%RotSpeed
```

If the generator degree of freedom is off or if the rotational speed is zero, TrimCase is set to 0 so that the trimming is cancelled.

Initialization routine Srvd\_Init The added variables from InitInputType are copied to the ParameterType variables. The state variable CtrlOffset is initialized to 0. If the parameter TrimGain is not strictly positive, an error is thrown.

Update state routine Srvd\_UpdateDiscState A simple proportional gain on the rotational speed error is used to correct the control parameters. The error in rotor speed  $\epsilon_{\Omega}$  is the difference between the target speed and the current rotor speed:

$$\epsilon_{\Omega} = \Omega_c - \Omega_{\text{ref}} \tag{8}$$

The current rotor speed is  $\Omega_c = u \text{RotSpeed}$ . The offset on the controller variable is computed using the speed error and a proportional gain  $k_p > 0$ . The offset is computed as:

$$x_{\text{off}} = x_{\text{off}} + s \, k_p \, \epsilon_{\Omega} \tag{9}$$

The variable s above accounts for possible sign adjustments. The offset is such that it will converge to a constant value as  $\epsilon_{\Omega}$  tends to 0. When TrimCase=1,  $x_{\rm off}$  is the yaw angle offset (in rad). When TrimCase=2,  $x_{\rm off}$  is the generator torque offset (in N). When TrimCase=3,  $x_{\rm off}$  is the pitch angle offset (in rad). For the pitch and generator torque, s=1. Indeed, when the rotational speed is faster than  $\Omega_{\rm ref}$  ( $\epsilon_{\Omega}>0$ ), the pitch or generator torque needs to be increased to lower the rotational speed. The opposite holds when the rotor spins slower than  $\Omega_{\rm ref}$ . On the other hand, when  $\epsilon_{\Omega}>0$ , the yaw angle needs to be increased if the yaw angle is positive, or decreased if this angle is negative, in order to decrease the rotational speed. For this case,  $s={\rm sign}(\theta_{\rm yaw,0}+x_{\rm off})$ , where  $\theta_{\rm yaw,0}$  is the neutral yaw angle defined by p%YawNeut. Another subtlety arises for the yaw case, since the main variable of ServoDyn is actually the yaw moment. Yet, it is more convenient to manipulate an offset on the yaw angle since the offset sign depends on the yaw angle. This issue will be addressed in the next paragraph. The update of the discrete state is implemented as follows:

Output routine SrvD\_CalcOutput The output variables of ServoDyn are directly modified using the offset CtrlOffset. As mentioned in the previous paragraph, in the yaw case, the main variable outputted by ServoDyn is the yaw moment and not the yaw angle. The part of the yaw moment that depends on the yaw angle is computed as:

$$Q_{\text{vaw}} = -k_{\text{vaw}}(\theta_{\text{vaw,ED}} - \theta_{\text{vaw,0}}) \tag{10}$$

Hence, if  $\theta_{\text{yaw},0}$  is replaced by  $\theta_{\text{yaw},0} + x_{\text{off}}$ , it is seen that the yaw moment is given the offset  $k_{\text{yaw}}x_{\text{off}}$ . For the implementation, the control outputs are trimmed just after their computation within the SrvD\_CalcOutput routine, that is after calling Pitch\_CalcOutput, Torque\_CalcOutput and Yaw\_CalcOutput, as follows:

```
if (TrimCase == 1) then
    y%YawMom = y%YawMom + xd%CtrlOffset * p%YawSpr
else if (TrimCase == 2)
```

```
y%GenTrq = y%GenTrq + xd%CtrlOffset
else if (TrimCase==3)
    y%BlPitchCom = y%BlPitchCom + xd%CtrlOffset
else
   ! do nothing
endif
```

By doing the update in Svrd\_CalcOutput, it is ensured that the operating point will be about the proper conditions. Indeed, in Svrd\_GetOP, the operating point variables are set from the outputs directly:

```
y_op(Indx_Y_BlPitchCom) = y%BlPitchCom
y_op(Indx_Y_YawMom) = y%YawMom
y_op(Indx_Y_GenTrq) = y%GenTrq
```

It is important to note that the routines CalculateStandardYaw and CalcuateTorque returns values without offset. These routines are for instance called by Yaw\_UpdateStates and Torque\_UpdateStates.

**Linearization routine** SrvD\_JacobianPInput This routine uses a generator torque which does not have an offset. It may require the following modification:

```
if (TrimCase == 2)
    GenTrq = GenTrq + xd%CtrlOffset
endif
```

#### 1.5 Additional glue-code procedure to increase the damping

Artificial damping forces are added to the external forces applied on the structure. For now, the extra damping is only applied to ElastoDyn and BeamDyn. The extra damping force is set to be proportional to the velocity of each node of the structure. The proportionality constants Twr\_Kdmp and Bld\_Kdmp are used respectively for nodes on the tower or the blade. In general, the force F on a given node of velocity v is updated as follows:

$$F \leftarrow F - k_{\rm dmp} \ v$$
 (11)

To avoid damping the rotation of the blade, the following is applied for nodes along the blade:

$$F \leftarrow F - k_{\rm dmp} \ (\boldsymbol{v} - \boldsymbol{\Omega}_c \times \boldsymbol{r})$$
 (12)

where r is the instantaneous position vector of a blade node. The forces are usually found as inputs of a module while the kinematics are found in the outputs. The additional damping forces can be implemented in the procedure ED\_InputSolve of the glue-code. For ElastoDyn, the update of the forces

where K is the blade number and J is the node index (along the tower or blade, looping til NNodes), u and y are the module input and outputs, and  $Vrot = \Omega_c \times r$  is the velocity due to the rotation of the blade node, computed using Equation 13. For BeamDyn, the additional damping is added as follows:

The variable extstyle extstyle

$$m{\Omega}_c = \Omega_c \cdot ext{y%HubPtMotion%Orientation(1,:,1)} \ m{r} = m{r}_{ ext{node}} - m{r}_{ ext{hub}}$$

 $r_{
m hub} = exttt{y\%HubPtMotion\%Position(1:3,1)} + exttt{y\%HubPtMotion\%TranslationDisp(1:3,1)}$ 

 $r_{
m node} = y\% {
m BladeLn2Mesh(K)\%Position(1:3,J)} + y\% {
m BladeLn2Mesh(K)\%TranslationDisp(1:3,J)}$ 

where  $r_{\text{node}}$  is defined for ElastoDyn above. It is defined in BeamDyn as:

 $r_{
m node} = exttt{y(k)\%BladeMotion\%Position(1:3,J)} + exttt{y(k)\%BladeMotion(K)\%TranslationDisp(1:3,J)}$