

$$1.39e+24 \text{ and The Pfund Mass} = \sqrt{\frac{10^{-14} q_e^4 c^3}{G}} = M_F$$

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Using $\frac{q_e}{\text{coulomb}} \frac{\text{kg} \cdot \text{m}^2}{\text{s}^2} = eV = 1.602176634 \times 10^{-19} J$ = the ElectronVolt; units of Mass = $\frac{eV}{c^2}$, Length = $\frac{\hbar c}{eV}$, or Time = $\frac{\hbar}{eV}$ can be constructed. Maybe we can do better:

$$\begin{aligned} \frac{\hbar}{c M_F} &= L_F = \frac{\hbar c}{E_F}; & \frac{\hbar}{c^2 M_F} &= T_F = \frac{\hbar}{E_F}; & q_e &= Q_F \\ k_e &= \alpha M_F^1 L_F^3 T_F^{-2} Q_F^{-2} & \hbar &= 1 M_F^1 L_F^2 T_F^{-1} \\ \mu_0 &= \alpha 4 \pi M_F^1 L_F^1 Q_F^{-2} & c &= 1 L_F^1 T_F^{-1} \\ \epsilon_0 &= \frac{1}{\alpha 4 \pi} M_F^{-1} L_F^{-3} T_F^2 Q_F^2 & N_A &= 1^{**} \\ R_\infty &= \frac{m_e}{M_F} \frac{\alpha^2}{4 \pi} L_F^{-1} & M_F c^2 &= E_F = 1 M_F^1 L_F^2 T_F^2 \\ & & \frac{2 \pi \hbar}{c q_e} &= k_b = 2 \pi M_F^1 L_F^1 Q_F^{-1} \end{aligned}$$

** only way to correct N_A being based on the Dalton = $\frac{1}{12}$ the mass of Carbon isotope C^{12} is to correct the periodic table to use the Pfund Mass = M_F like the example to the right.

1 Dimensionality

Stoney-Mass $M_S = \sqrt{\frac{\hbar \alpha c}{G}}$ dimensions are correct but $M_F = M_S \sqrt{\hbar \alpha}$ it does mess up the dimensions, but the numbers make all the equations above work, need to do some math and maybe some powers of α & other constants can get rid of the $1 M^{1/2} L^1 T^{-1/2}$.

$$\hbar \alpha^2 = \frac{10^{-14} Q_F^4}{M_F T_F} = \frac{G}{M_F^3 L_F^{-1} T_F^{-2} Q_F^0}$$

Only unit with wrong dimensionality is G , but the arithmetic is correct; for correct dimensionality M_F needs to be multiplied times $\sqrt{\frac{T}{M L^2}}$ (this also goes the reciprocal of L_F and T_F). Does gravity exist, or is it just the curvature of space time?

$$2 \pi 10^{-7} = \frac{\mu_0 Q^2}{2 M L} = \frac{Q^2}{M L} \frac{\hbar \alpha}{c q_e^2}; \quad k_e = \frac{\hbar \alpha c^2}{c q_e^2 2 \pi}; \quad \epsilon_0 = \frac{1}{\mu_0 c^2}$$

$$\frac{\mu_0 c q_e^2}{2 2 \pi \hbar} = \frac{2 \pi 10^{-7} 299792458 (1.602176634 \times 10^{-19})^2}{6.62607015 \times 10^{-34}} = \alpha$$

= 0.00729735257 - "It has been a mystery ever since it was discovered more than fifty years ago, and all good theoretical physicists put this number up on their wall and worry about it." [Feynman, 1985, p. 129].

$$k_e = 10^{-7} c^2 \frac{T^2}{L^2} \frac{M}{T^2} \frac{L^3}{Q^2}$$

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2 Speed of Sound = c_0

Given $c_0 = \sqrt{\frac{\gamma_0 N_A k_B T}{M}}$ and $39.947 g \text{ mol}^{-1}$ = molar mass of the argon gas from the experiment measuring c_0 in a purified isotope of argon gas at the Triple-Point of water = 273.16K [dePodesta et al., 2013] Where $U_F = \frac{E_F}{k_b}$, $T = \frac{\text{Kelvin}}{U_F} U_F$, and $\gamma_0 = 5/3$ for monotonic gases. Let's see how that matches up with the $c_0^2 = 94756.245 m^2 s^{-2}$ from the experiment in 2013.

$$c_0 = \sqrt{\frac{\frac{5}{3} 1 k_B \frac{273.16 \text{ Kelvin}}{U_F} U_F}{40.671 M_F}} = 307.701 m s^{-1} \approx \sqrt{c_0^2}$$

$$**\text{adjusted argon gas molar mass} = 40.671 M_F = \frac{39.947}{M_F N_A}$$

3 Time is On Our Side(& Distance)

With a Sympathetic Constant = D_C = light-second / L_F to save our wallets, watches, measuring wheels, and road signage we can still use existing definitions of distance and time.

$$\frac{1.3899982e + 24 \approx \frac{c T_{SI}}{L_F} = D_C}{1.39e + 24} = 0.999998675$$

Perhaps one day for the sake of simplicity, Bureau international des poids et mesures might redefine the second and meter such the D_C is exactly $1.39e+24$ rather than approx. 5 almost 6 nines.

4 Conclusion

Remember all wallets, watches, measuring wheels, and road signage are already calibrated to D_C and After the dust settles and all scales and ammeter are calibrated, all that will have to be remembered besides preserving dimensionality when doing calculations is the following:

$$\begin{aligned} 222702.257 \text{Coulombs} &= D_C Q_F \\ \frac{\hbar}{c^2 M_F} D_C &= 1 \text{Second} = T_F D_C \\ \frac{\hbar}{c M_F} \frac{D_C}{299792458} &= 1 \text{Meter} = L_F \frac{D_C}{299792458} \\ 2.267061 \text{grams} \approx 1 \text{Pfund} \frac{c T_{SI}}{L_F} &= M_F D_C \end{aligned}$$



5 Constants

Avogadro constant $N_A = 6.02214076 \times 10^{26} \frac{\text{atoms per kg}}{\text{molar mass}}$

Planck constant $h = 6.62607015 \times 10^{-34} \text{ kg m}^2 \text{ s}^{-1}$

lightspeed constant $c = 299792458 \text{ m s}^{-1}$

electron charge $q_e = 1.602176634 \times 10^{-19} \text{ Coulombs}$

gravity constant $G = 6.67430 \times 10^{-11} \text{ kg}^{-1} \text{ m}^3 \text{ s}^{-2}$

On May 20, 2019 the values of N_A , $\hbar = \frac{h}{2\pi}$, and h , were fixed to the Dalton = $\frac{1}{12}$ the mass of Carbon isotope C^{12} [Bettin]. s = “duration of 9192631770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the cesium 133 atom” [SI, 1968] to finish the definition of c , An international agreement in Paris on Oct. 20 1983 defines the meter as $\frac{1}{299792458}$ the distance light travels in a vacuum in 1 second [Times, 1983],

[Tiesinga et al., 2021] gives us q_e , and G . Just don’t forget Milikan’s Oil Drop or the Cavendish Mitchell Device.

5.1 How the Avogadro constant was measured for the last time

N_A and h were measured using a incredibly round & pure ball of Si^{28} and a Kibble balance and the equations basically verbatim from [Bettin] and [Wood and Bettin, 2019] Where $\alpha^2 m_e c / 2 h = R_\infty$ is the Rydberg constant, $\sum_{i=28}^{30} x_i A_r(iSi) = A_r(Si)$ average molar mass of a silicon atom in the crystal is calculated using the proportions x_i of the various isotopes iSi , V is Volume of Silicon Sphere, a Lattice parameter of the silicon crystal, 8 is the number of atoms in an elementary cell of the lattice (cube with edge length a). M Molar mass of silicon contained in sphere. m mass of sphere.

$$N = \frac{8V}{a^3} = \text{Number of atoms in silicon sphere}$$

$$N_A = \frac{M 8V}{m a^3} = \text{Avogadro constant}$$

$$m(Si) = \frac{m}{N} = \frac{m a^3}{8V} = m(e) \frac{A_r(Si)}{A_r(e)}$$

$$m(e) = \frac{2 h R_\infty}{c \alpha^2} = \frac{2 (2\pi \hbar) R_\infty}{c \alpha^2}$$

$$h = \frac{c \alpha^2 m a^3}{2 R_\infty 8V} \frac{A_r(e)}{\sum_{i=28}^{30} x_i A_r(iSi)}$$

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Supplementary Materials

This was originally some notes on how the Planck-Units, and the Stoney-Units [Stoney, 1883], baked out the need for certain constants. Stoney-Mass $M_S = \sqrt{\frac{\hbar \alpha c}{G}}$ dimensions are correct but $M_F = M_S \sqrt{\hbar \alpha}$ it does mess up the dimensions, but the numbers cancel like a million things out. Only reason I knew about it was I had avogadro constant for Stoney-Mass mass popping up to do the speed of sound calc to see how the planck units canceled out the Boltzman constant, and I saw the Avogadro constant for M_S and for some reason or another I had just looked at $\sqrt{\hbar \alpha}$. Hopefully this unit system will bring α in front of more eyes.