

$$\frac{2.267061\text{grams}}{1.39 \times 10^{24}} \approx \sqrt{\frac{k_e^2 q_e^4 T}{c G M L^2}} = \sqrt{\frac{c \hbar^2 \alpha^2 T}{G M L^2}} = M_F$$

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1 Dimensionality

Stoney-Mass $M_S = \sqrt{\frac{\hbar \alpha c}{G}}$ units are correct, but with $M_F = M_S \sqrt{\hbar \alpha}$ alone gives correct arithmetic; for all the equations below to not only work arithmetic wise, $\sqrt{\frac{T}{M^1 L^2}}$ is needed cancel any wrong units put into M_F from \hbar , M , L , and T with no subscripts are meant to mean from whichever unit system you are converting from, in this case; SI units 1kg, 1m, and 1s respectively.

$$\alpha^2 \hbar = \alpha^2 \frac{M_F L_F^2}{T_F} = \frac{G}{M_F^3 L_F^{-1} T_F^{-2}}$$

but it comes back in the solution for G . However G is wrong to begin with, because with Relativity it doesn't really exist, as it is the curvature of space time. Might help us understand α ?

$$\frac{\mu_0 c q_e^2}{2 \pi \hbar} = \frac{2 \pi 10^{-7} 299792458 (1.602176634 \times 10^{-19})^2}{6.62607015 \times 10^{-34}} = \alpha$$

$$\frac{\mu_0}{2} = \frac{\hbar \alpha}{c q_e^2}; \quad \frac{\hbar \alpha}{c q_e^2} \frac{c^2}{2\pi} = k_e; \quad \epsilon_0 = \frac{1}{\mu_0 c^2}$$

= 0.00729735257 "It has been a mystery ever since it was discovered more than fifty years ago, and all good theoretical physicists put this number up on their wall and worry about it." [Feynman, 1985, p. 129]. **Let's put it everywhere.**

$$\sqrt{\frac{T_F}{M_F L_F^2} \frac{G}{M_F^3 L_F^{-1} T_F^{-2}}} = \alpha$$

2 Speed of Sound = c_0

Given $c_0 = \sqrt{\frac{\gamma_0 N_A k_B T}{M}}$ and $39.947 \text{ g mol}^{-1}$ = molar mass of the argon gas from the experiment measuring c_0 in a purified isotope of argon gas at the Triple-Point of water = 273.16K [dePodesta et al., 2013] Where $U_F = \frac{E_F}{k_b}$, $T = \frac{\text{Kelvin}}{U_F} U_F$, and $\gamma_0 = 5/3$ for monotonic gases. Let's see how that matches up with the $c_0^2 = 94756.245 \text{ m}^2 \text{ s}^{-2}$ from the experiment in 2013.

$$c_0 = \sqrt{\frac{\frac{5}{3} 1 k_B \frac{273.16 \text{ Kelvin}}{U_F} U_F}{40.671 M_F}} = 307.701 \text{ ms}^{-1} \approx \sqrt{c_0^2}$$

$$**\text{adjusted argon gas molar mass} = 40.671 M_F = \frac{39.947}{M_F N_A}$$

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3 Time is On Our Side(& Distance)

With a Sympathetic Constant = D_C = light-second / L_F to save our wallets, watches, measuring wheels, and road signage we can still use existing definitions of distance and time.

$$\frac{1.3899982 \times 10^{24} \approx \frac{c T_{SI}}{L_F} = D_C}{1.39 \times 10^{24}} = 0.999998675$$

Perhaps one day for the sake of simplicity, Bureau international des poids et mesures might redefine the second and meter such the D_C is exactly 1.39×10^{24} rather than approx. 5 almost 6 nines.

4 Conclusion

I could go on about how some CFD software uses planck units to reduce computation by reducing the billions of multiplications of k_b ; we should care about people as much as machines and reduce the constants people have to know. Remember all wallets, watches, measuring wheels, and road signage are already calibrated to D_C and After the dust settles and all scales are calibrated to $D_C M_F$ and ammeter are calibrated to $D_C q_e$, all that will have to be remembered besides preserving dimensionality when doing calculations is the following:

$$\frac{\hbar}{c^2 M_F} = T_F \approx \frac{1 \text{ Second}}{1.39 \times 10^{24}}; \quad Q_F \approx \frac{222702.257 \text{ Coulombs}}{1.39 \times 10^{24}}$$

$$\frac{\hbar}{c M_F} = L_F \approx \frac{299792458 \text{ Meters}}{1.39 \times 10^{24}}$$

$$k_e = \alpha M_F^1 L_F^3 T_F^{-2} Q_F^{-2} \quad \hbar = 1 M_F^1 L_F^2 T_F^{-1}$$

$$\mu_0 = \alpha 4 \pi M_F^1 L_F^1 Q_F^{-2} \quad c = 1 L_F^1 T_F^{-1}$$

$$\epsilon_0 = \frac{1}{\alpha 4 \pi} M_F^{-1} L_F^{-3} T_F^2 Q_F^2 \quad N_A = 1^{**}$$

$$M_F c^2 = E_F = 1 M_F^1 L_F^2 T_F^2$$

$$R_\infty = \frac{m_e}{M_F} \frac{\alpha^2}{4 \pi} L_F^{-1} \quad \frac{2 \pi \hbar}{c q_e} = k_b = 2 \pi M_F^1 L_F^1 Q_F^{-1}$$

** only way to correct N_A being based on the Dalton = $\frac{1}{12}$ the mass of Carbon isotope C^{12} is to correct the periodic table to use the Pfund Mass = M_F like the sound-speed example.



5 Constants

Avogadro constant $N_A = 6.02214076 \times 10^{26} \frac{\text{atoms per kg}}{\text{molar mass}}$

Planck constant $h = 6.62607015 \times 10^{-34} \text{kg m}^2 \text{s}^{-1}$

lightspeed constant $c = 299792458 \text{m s}^{-1}$

electron charge $q_e = 1.602176634 \times 10^{-19} \text{Coulombs}$

gravity constant $G = 6.67430 \times 10^{-11} \text{kg}^{-1} \text{m}^3 \text{s}^{-2}$

On May 20, 2019 the values of N_A , $\hbar = \frac{h}{2\pi}$, and h , were fixed to the Dalton = $\frac{1}{12}$ the mass of Carbon isotope C^{12} [Bettin]. s = “duration of 9192631770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the cesium 133 atom”[SI, 1968] to finish the definition of c , An international agreement in Paris on Oct. 20 1983 defines the meter as $\frac{1}{299792458}$ the distance light travels in a vacuum in 1 second[Times, 1983],

[Tiesinga et al., 2021] gives us q_e , and G . Just don’t forget Milikan’s Oil Drop or the Cavendish Mitchell Device.

5.1 How the Avogadro constant was measured for the last time

N_A and h were measured using a incredibly round & pure ball of Si^{28} and a Kibble balance and the equations basically verbatim from [Bettin] Where $\alpha^2 m_e c / 2 h = R_\infty$ is the Rydberg constant, $\sum_{i=28}^{30} x_i A_r(i Si) = A_r(Si)$ average molar mass of a silicon atom in the crystal is calculated using the proportions x_i of the various isotopes $i Si$, V is Volume of Silicon Sphere, a Lattice parameter of the silicon crystal, 8 is the number of atoms in an elementary cell of the lattice(cube with edge length a). M Molar mass of silicon contained in sphere. m mass of sphere.

$$N = \frac{8 V}{a^3} = \text{Number of atoms in silicon sphere}$$

$$N_A = \frac{M 8 V}{m a^3} = \text{Avogadro constant}$$

$$m(Si) = \frac{m}{N} = \frac{m a^3}{8 V} = m(e) \frac{A_r(Si)}{A_r(e)}$$

$$m(e) = \frac{2 h R_\infty}{c \alpha^2} = \frac{2 (2\pi \hbar) R_\infty}{c \alpha^2}$$

$$h = \frac{c \alpha^2 m a^3}{2 R_\infty 8 V} \frac{A_r(e)}{\sum_{i=28}^{30} x_i A_r(i Si)}$$

References

Horst Bettin. How the avogadro constant was measured for the last time. URL <https://q-more.chemeurope.com/q-more-articles/287/how-the-avogadro-constant-was-measured-for-the-last-time.html>.

Michael dePodesta, Robin Underwood, Gavin Sutton, Paul Morantz, Peter Harris, Darren F Mark, Finlay M Stuart, Gergely Vargha, and Graham Machin. A low-uncertainty measurement of the boltzmann constant. *Metrologia*, 50(4): 354–376, jul 2013. doi: 10.1088/0026-1394/50/4/354. URL <https://doi.org/10.1088/0026-1394/50/4/354>.

Richard Feynman. *QED : the strange theory of light and matter*. Princeton University Press, Princeton, N.J, 1985. ISBN 978-0-691-08388-9.

SI. *CGPM13 CGPM : Comptes rendus de la 13e reunion (1968)*. Bureau international des poids et mesures, F-92312 Sèvres Cedex, France, 1968. URL <https://www.bipm.org/documents/20126/17314988/CGPM13.pdf/ff522dd4-7c97-9b8d-127b-4fe77f3fe2bc?version=1.2&t=1587104721230&download=true#page=103>.

George Johnstone Stoney. On the physical units of nature. *The Scientific Proceedings of the Royal Dublin Society*, 3:51–60, 1883. URL <https://books.google.com/books?id=R79WAAAAIAAJ&pg=PA51>.

Eite Tiesinga, Peter J. Mohr, David B. Newell, and Barry N. Taylor. Codata recommended values of the fundamental physical constants: 2018. *Rev. Mod. Phys.*, 93:025010, Jun 2021. doi: 10.1103/RevModPhys.93.025010. URL <https://link.aps.org/doi/10.1103/RevModPhys.93.025010>.

NY Times. Science watch. *NY Time*, page 6, Nov 1983. URL <https://www.nytimes.com/1983/11/01/science/science-watch-011004.html>.

Supplementary Materials

Only reason I found this was for some reason or another I had just looked at $\sqrt{\hbar \alpha}$, and I had Avogadro constant for Stoney-Mass $M_S = \sqrt{\frac{\hbar \alpha c}{G}}$ mass popping up in a script I had running with some notes to see how the Planck-Units, and the Stoney-Units[Stoney, 1883], baked out the need for certain constants. But when I had left the speed of sound calc to see how the planck units canceled out the Boltzman constant, and the Avogadro constant for M_S also popped up, not exact match but so close I had to do more tests.