

LAB7-RMD

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Get working Directory

```
getwd()
```

```
## [1] "C:/Users/cglen/Documents/Stat Methods/Labs/LAB7"
```

Chi-Square Distribution for 1 population

```
mychisim<-function(n1=10,sigma1=3,mean1=5,iter=1000,ymax=0.1,x=20, y=0.1){  # adjust ymax to make graph look good

  y1=rnorm(n1*iter,mean=mean1,sd=sigma1)# generate iter samples of size n1

  data1.mat=matrix(y1,nrow=n1,ncol=iter,byrow=TRUE) # Each column is a sample size n1

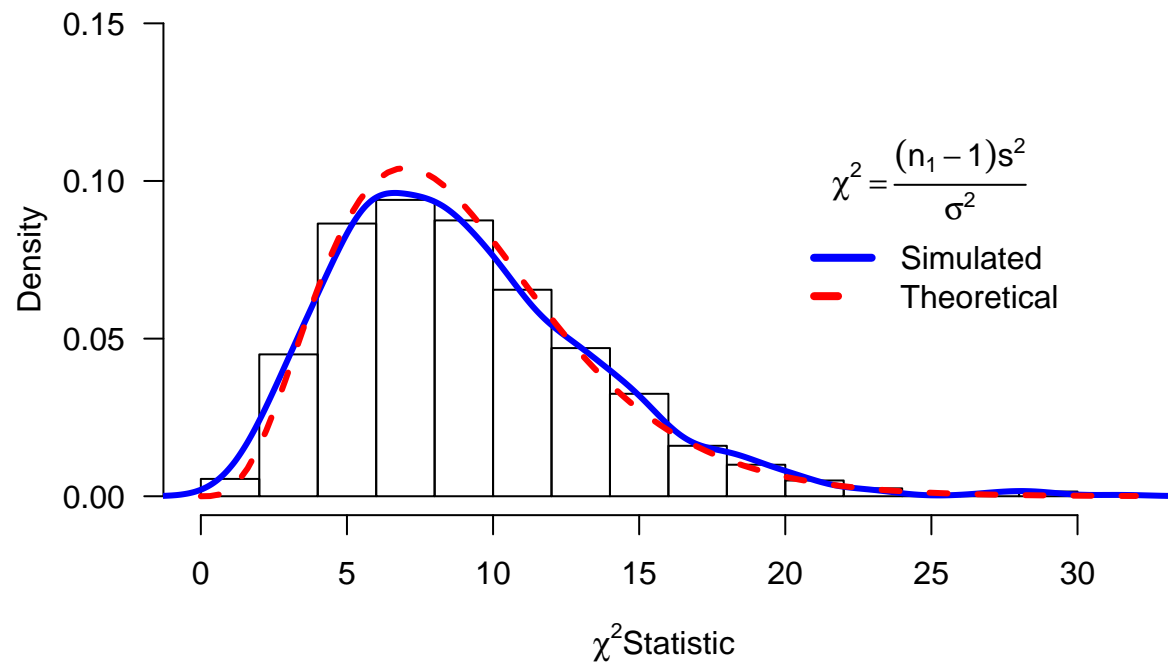
  ssq1=apply(data1.mat,2,var) # ssq1 is s squared

  w=(n1-1)*ssq1/sigma1^2      #chi-sq stat

  hist(w,freq=FALSE, ylim=c(0,ymax), # Histogram with annotation
        main=substitute(paste("Sample size = ",n[1]," = ",n1," statistic = ",chi^2)),
        xlab=expression(paste(chi^2, "Statistic",sep=" ")), las=1)
  lines(density(w),col="Blue",lwd=3) # add a density plot
  curve(dchisq(x,n1-1),add=TRUE,col="Red",lty=2,lwd=3) # add a theoretical curve
  title=expression(chi^2==frac((n[1]-1)*s^2,sigma^2)) #mathematical annotation -see ?plotmath
  legend(x,y,c("Simulated","Theoretical"),col=c("Blue","Red"),lwd=4,lty=1:2,bty="n",title=title) # Legend
  return()#list(w=w,summary=summary(w),sd=sd(w),fun="Chi-sq") # some output to use if needed
}

mychisim(n1 = 10, iter=1000,mean = 10, sigma = 4,ymax=0.15)
```

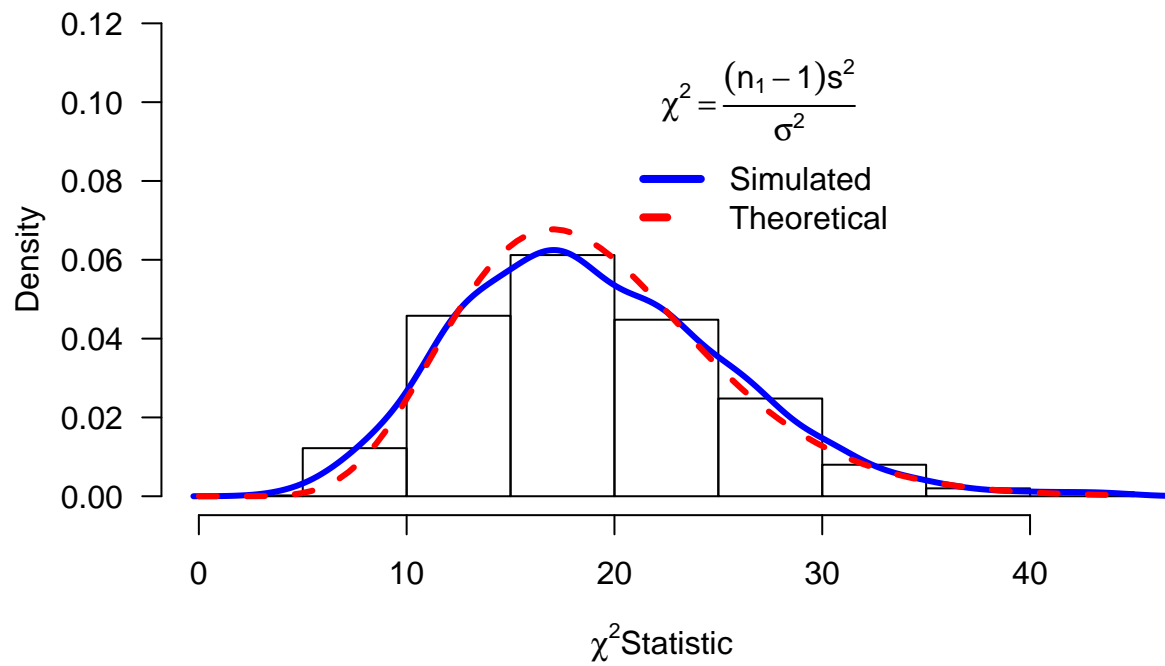
Sample size = $n_1 = 10$ statistic = χ^2



```
## NULL
```

```
mychisim(n1 = 20, iter=1000, mean = 10, sigma = 4, ymax=0.12)
```

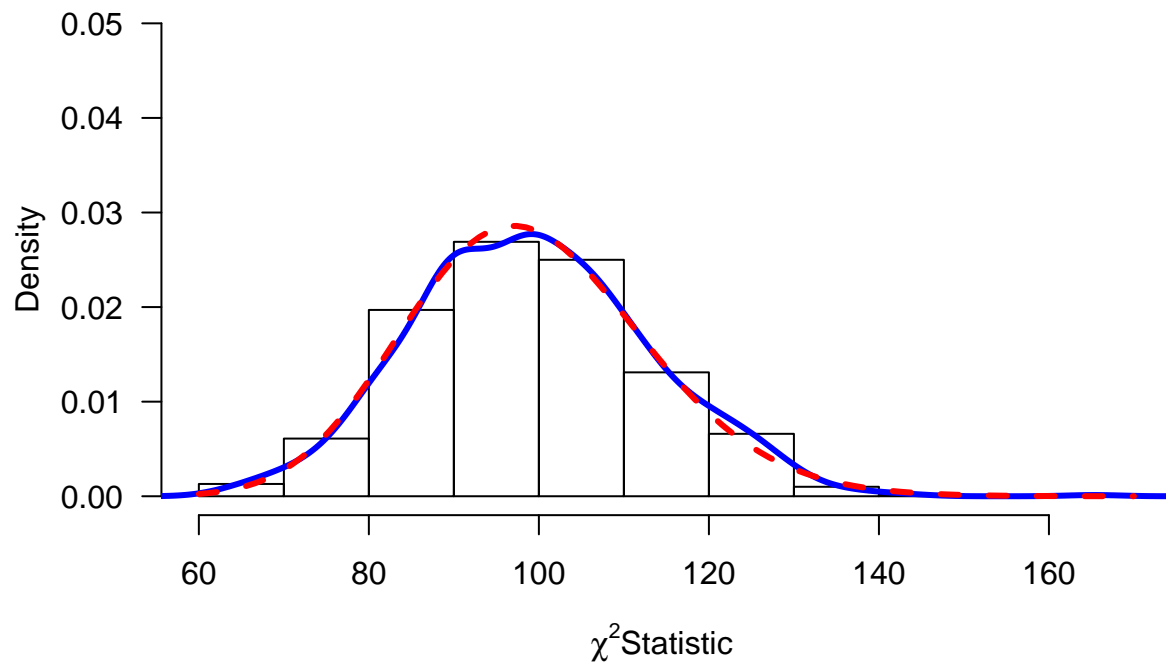
Sample size = $n_1 = 20$ statistic = χ^2



```
## NULL
```

```
mychisim(n1 = 100, iter=1000, mean = 10, sigma = 4, ymax=0.05)
```

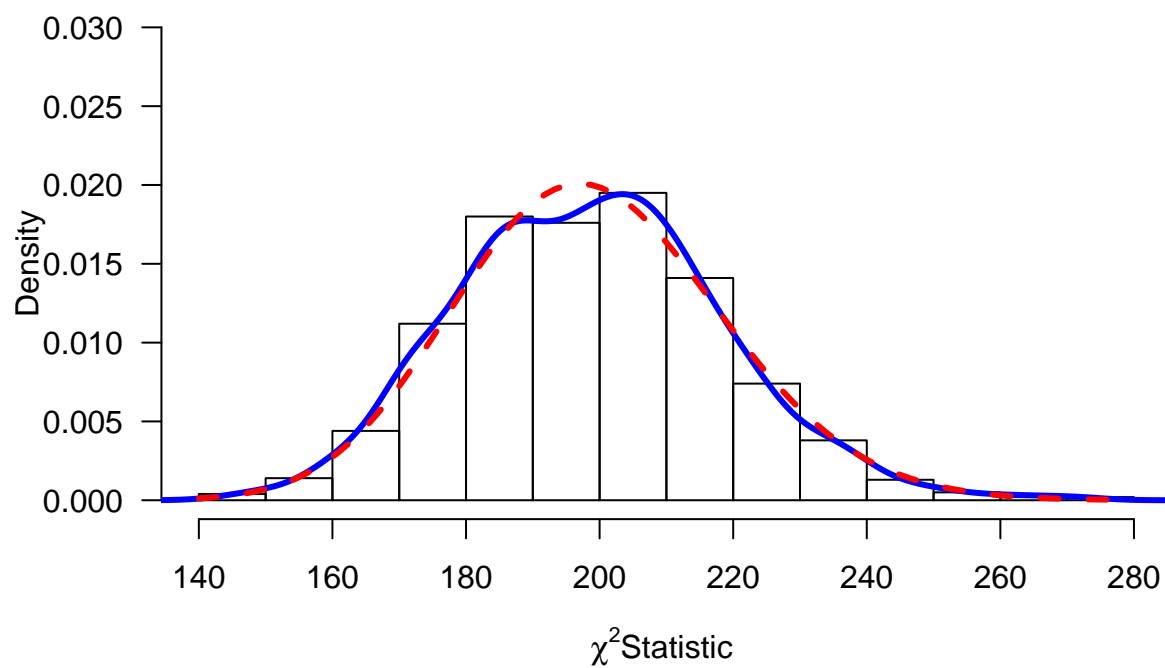
Sample size = $n_1 = 100$ statistic = χ^2



```
## NULL
```

```
mychisim(n1 = 200, iter=1000, mean = 10, sigma = 4, ymax=0.03)
```

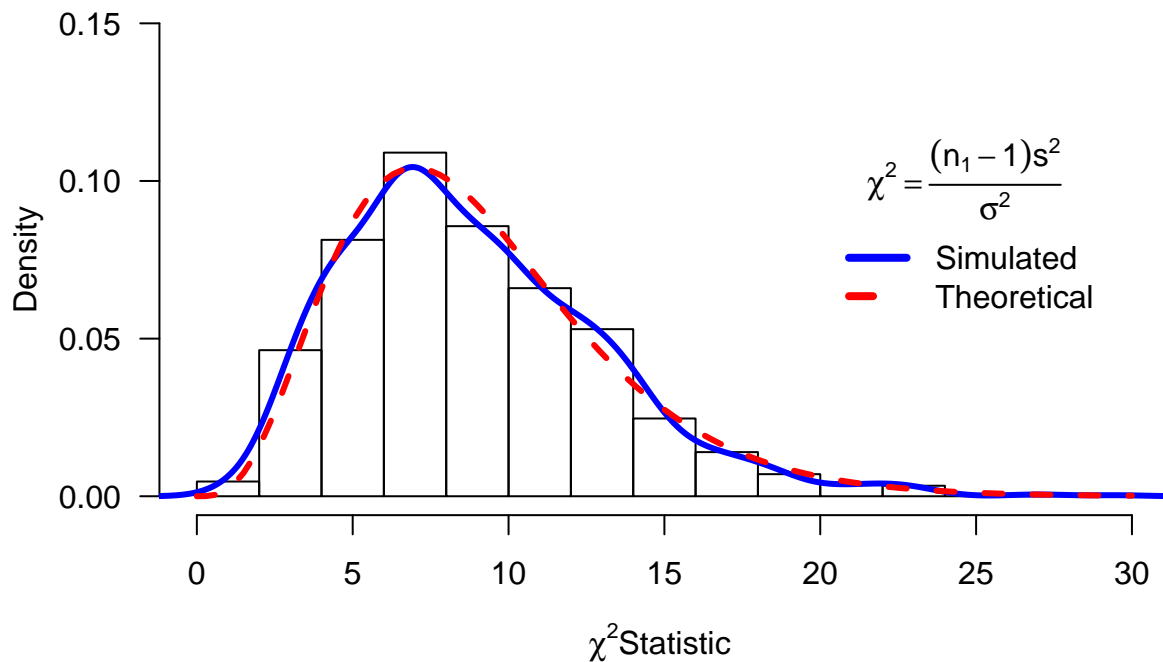
Sample size = $n_1 = 200$ statistic = χ^2



```
## NULL
```

```
chisq=mychisim(n1 = 10, iter=1500,mean = 20, sigma = 10,ymax=0.15)
```

Sample size = $n_1 = 10$ statistic = χ^2



T Distribution for 1 population

```
myTsim<-function(n1=10,sigma1=3,mean1=5,iter=1000,ymax=0.1,x=2,y=0.3,...){  # adjust ymax to make gray
  y1=rnorm(n1*iter,mean=mean1,sd=sigma1)# generate iter samples of size n1

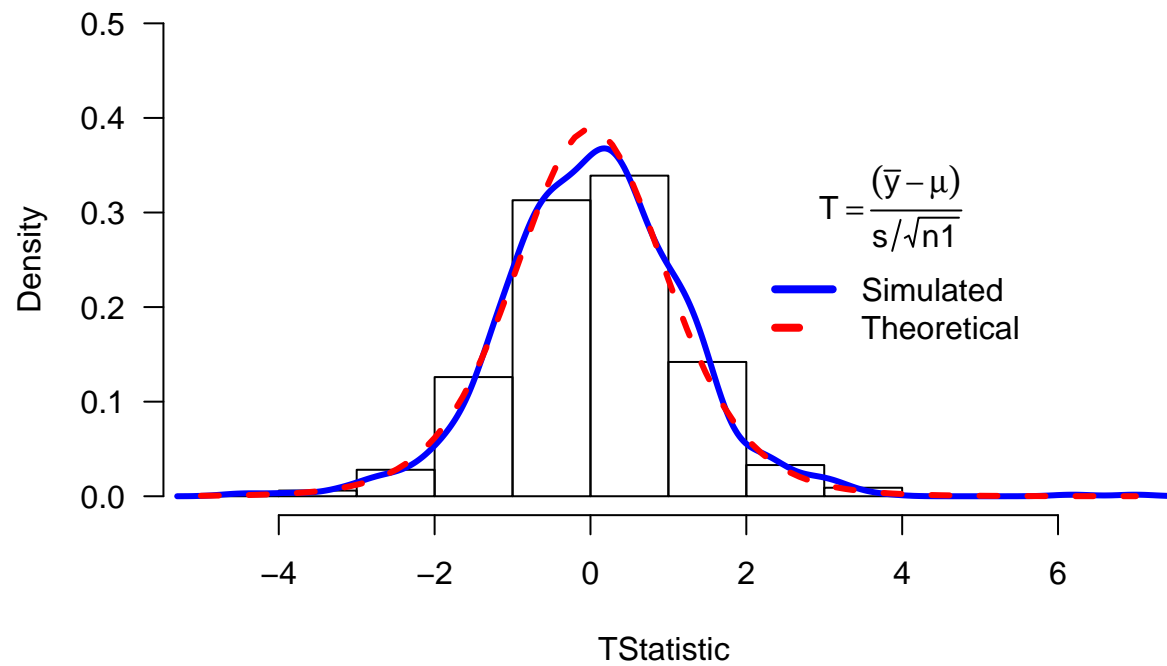
  data1.mat=matrix(y1,nrow=n1,ncol=iter,byrow=TRUE) # Each column is a sample size n1

  sd1=apply(data1.mat,2,sd) # sd
  ybar=apply(data1.mat,2,mean) # mean

  w=(ybar-mean1)/(sd1/sqrt(n1)) #T stat

  hist(w,freq=FALSE, ylim=c(0,ymax), # Histogram with annotation
        main=substitute(paste("Sample size = ",n[1]," = ",n1," statistic = ",T," iterations= ",iter)),
        xlab=expression(paste(T, "Statistic",sep=" ")), las=1)
  lines(density(w),col="Blue",lwd=3) # add a density plot
  curve(dt(x,n1-1),add=TRUE,col="Red",lty=2,lwd=3) # add a theoretical curve
  title=expression(T==frac((bar(y)-mu),s/sqrt(n1))) #mathematical annotation -see ?plotmath
  legend(x,y,c("Simulated","Theoretical"),col=c("Blue","Red"),lwd=4,lty=1:2,bty="n",title=title) # Legend
  return(list(w=w,summary=summary(w),sd=sd(w),fun="T")) # some output to use if needed
}
myTsim(n1 = 10, iter=1000,mean = 10, sigma = 4,ymax=0.5)
```

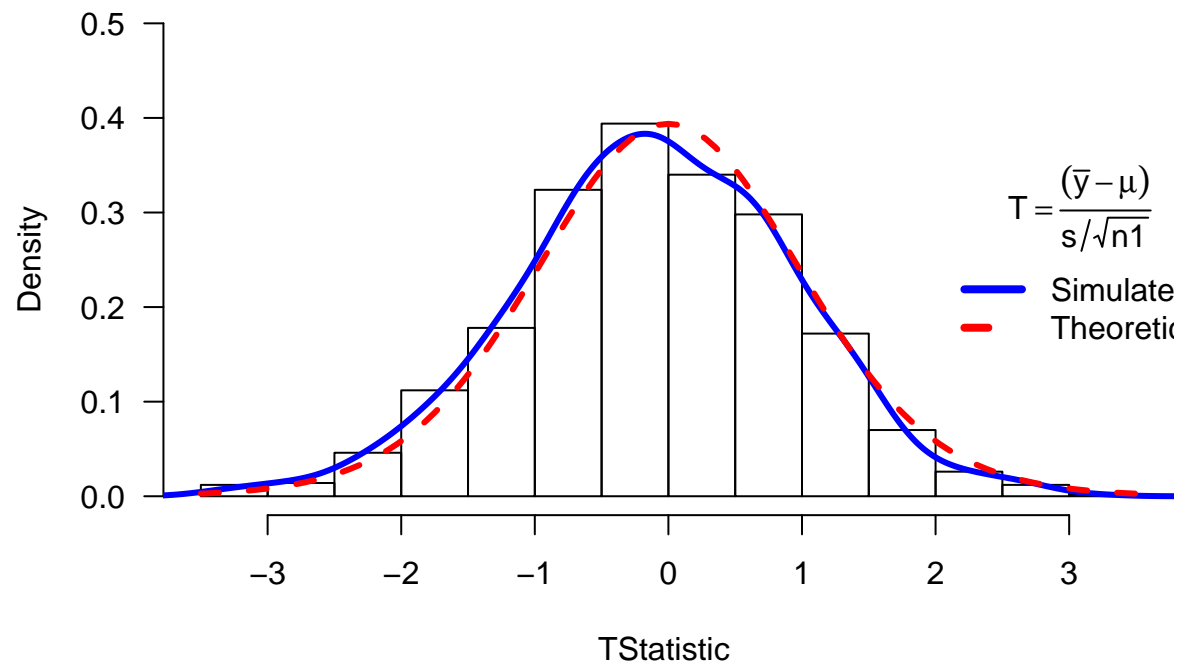
Sample size = $n_1 = 10$ statistic = T iterations= 1000



```
## NULL
```

```
myTsim(n1 = 20, iter=1000,mean = 10, sigma = 4,ymax=0.5)
```

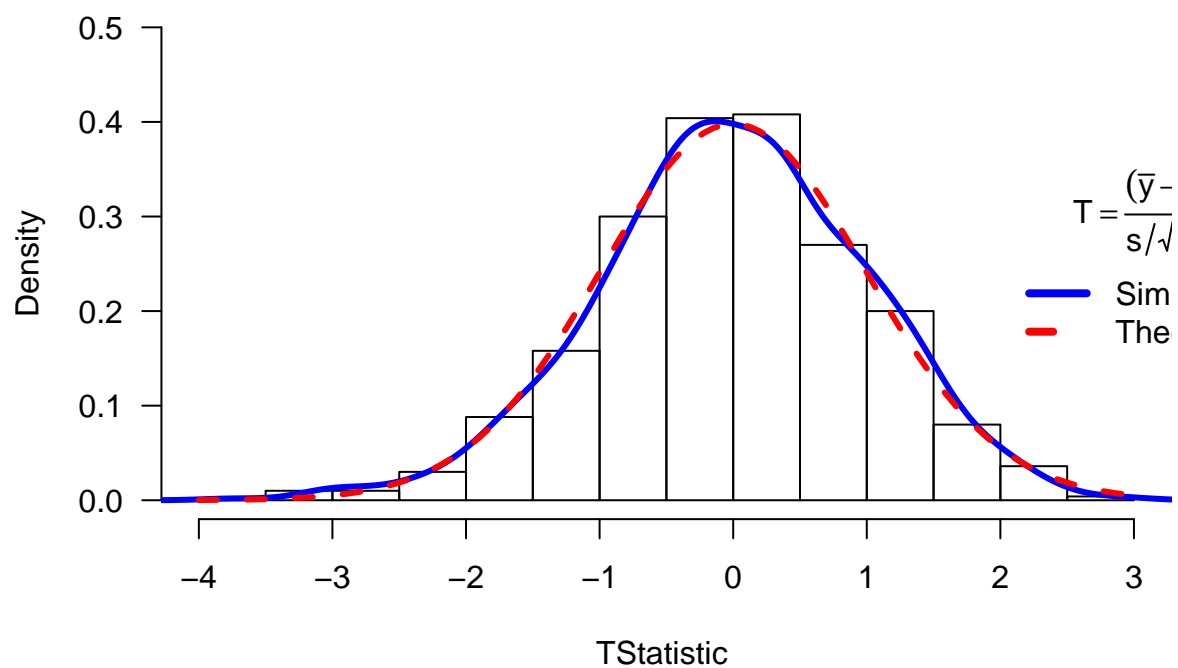
Sample size = $n_1 = 20$ statistic = T iterations= 1000



```
## NULL
```

```
myTsim(n1 = 100, iter=1000,mean = 10, sigma = 4,ymax=0.5)
```

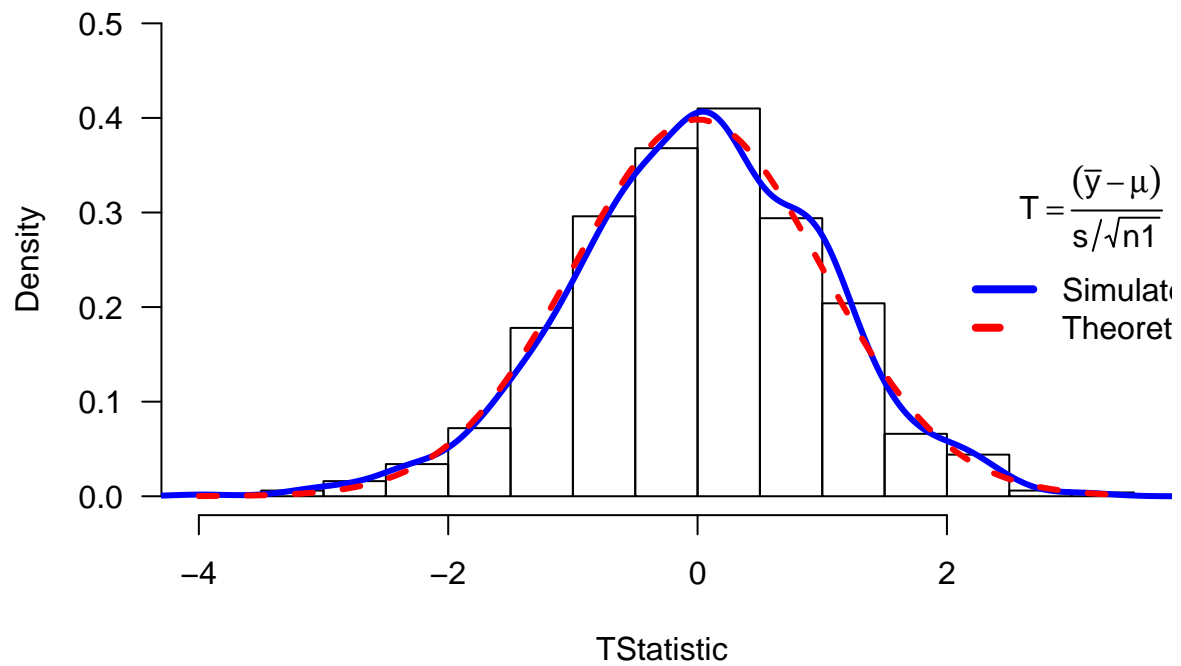

Sample size = $n_1 = 100$ statistic = T iterations= 1000



```
## NULL
```

```
myTsim(n1 = 200, iter=1000, mean = 10, sigma = 4, ymax=0.5)
```

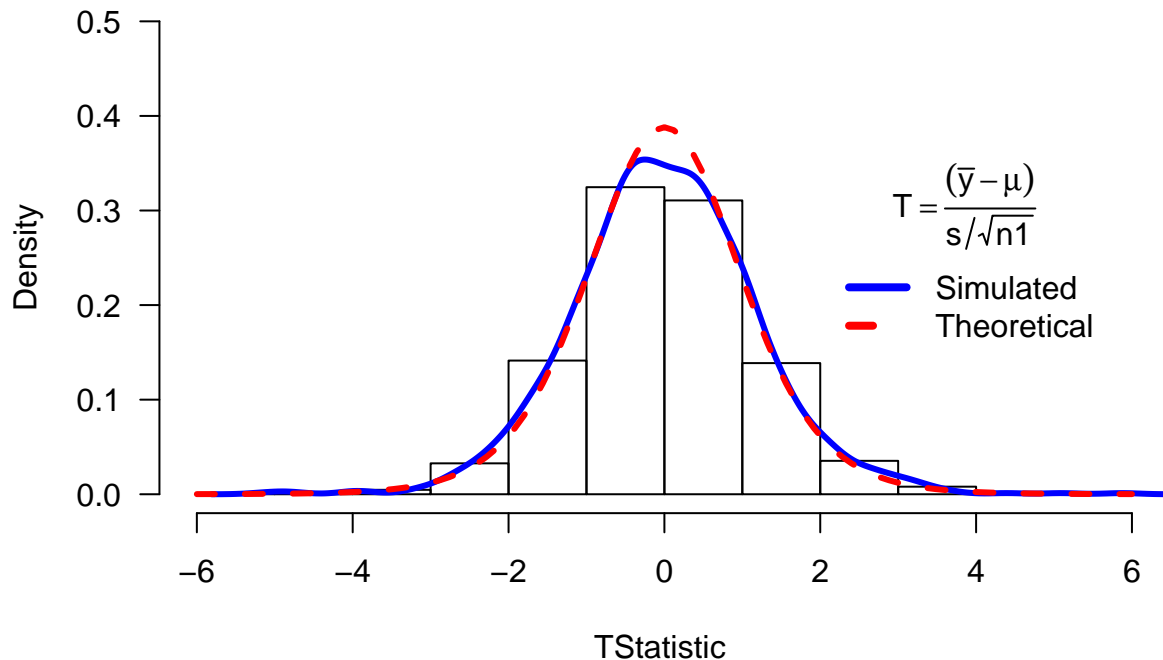
Sample size = $n_1 = 200$ statistic = T iterations= 1000



```
## NULL
```

```
T<-myTsim(n1 = 10, iter=1500,mean = 20, sigma = 10,ymax=0.50)
```

Sample size = $n_1 = 10$ statistic = T iterations= 1500



Chi-Squared Distribution with 2 populations

```
mychisim2<-function(n1=10,n2=14,sigma1=3,sigma2=3,mean1=5,mean2=10,iter=1000,ymax=0.07,x=40,y=0.04,...){
  y1=rnorm(n1*iter,mean=mean1,sd=sigma1)# generate iter samples of size n1
  y2=rnorm(n2*iter,mean=mean2,sd=sigma2)

  data1.mat=matrix(y1,nrow=n1,ncol=iter,byrow=TRUE) # Each column is a sample size n1
  data2.mat=matrix(y2,nrow=n2,ncol=iter,byrow=TRUE)

  ssq1=apply(data1.mat,2,var) # ssq1 is s squared
  ssq2=apply(data2.mat,2,var)

  spsq=((n1-1)*ssq1 + (n2-1)*ssq2)/(n1+n2-2) # pooled s squared

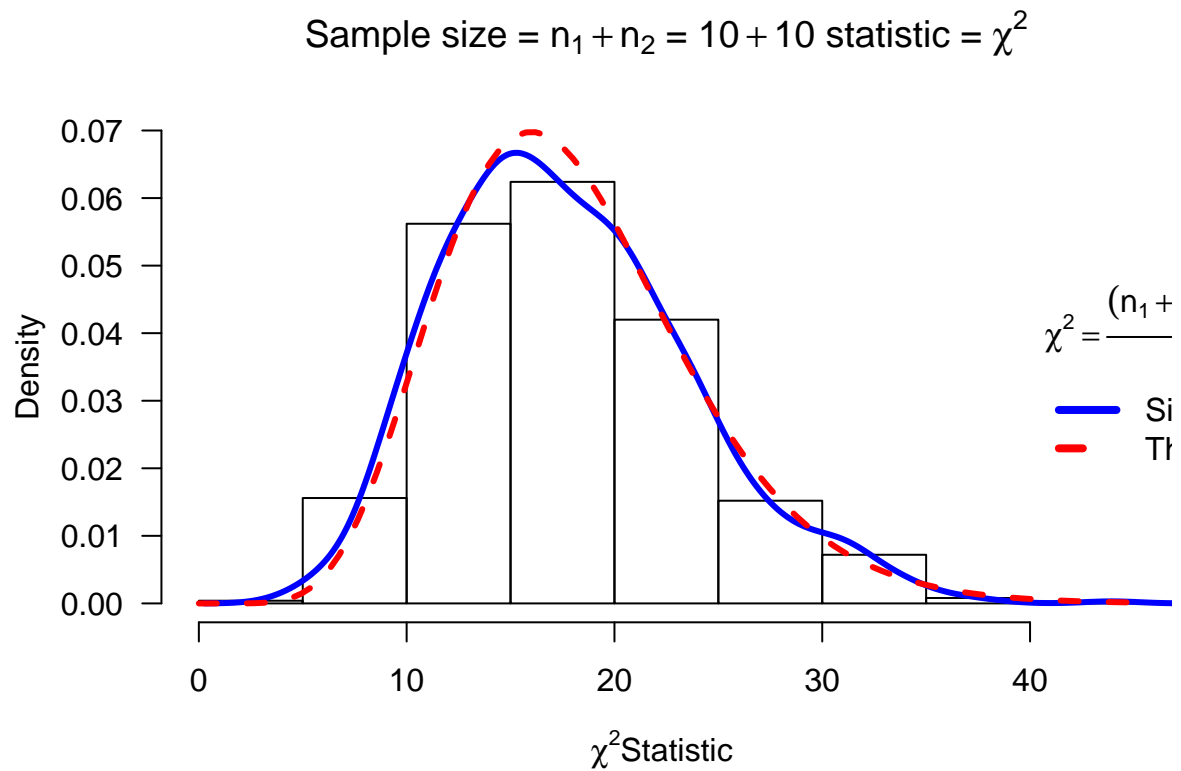
  w=(n1+n2-2)*spsq/(sigma1^2)#sigma1=sigma2, Chi square stat

  hist(w,freq=FALSE, ylim=c(0,ymax), # Histogram with annotation
       main=substitute(paste("Sample size = ",n[1]+n[2]," = ",n1+n2," statistic = ",chi^2)),
       xlab=expression(paste(chi^2, "Statistic",sep=" ")), las=1)
  lines(density(w),col="Blue",lwd=3) # add a density plot
  curve(dchisq(x,n1+n2-2),add=TRUE,col="Red",lty=2,lwd=3) # add a theoretical curve
  title=expression(chi^2==frac((n[1]+n[2]-2)*S[p]^2,sigma^2)) #mathematical annotation -see ?plotmath
}
```

```

legend(x,y,c("Simulated","Theoretical"),col=c("Blue","Red"),lwd=4,lty=1:2,bty="n",title=title) # Legend
return() # list(w=w,summary=summary(w),sd=sd(w),fun="Chi-sq") # some output to use if needed
}
mychisim2(n1=10,n2=10,mean1=5,mean2=10,sigma1=4,sigma2=4,iter=1000)

```

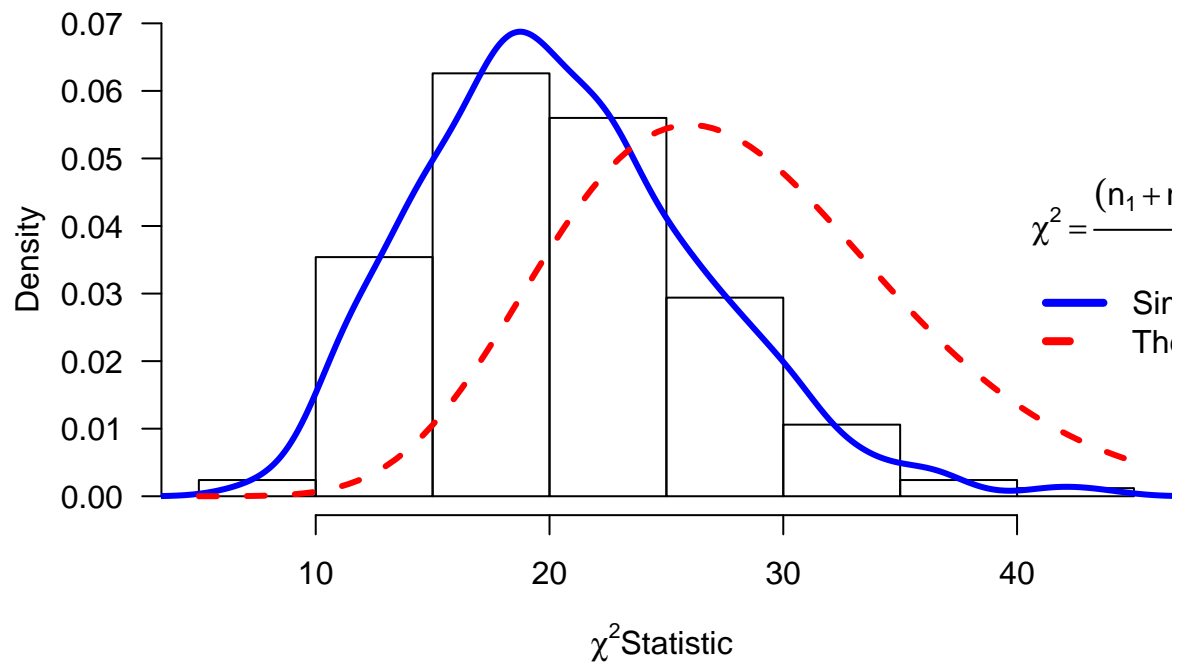


```

## NULL
mychisim2(n1=20,n2=10,mean1=3,mean2=5,sigma1=10,sigma2=4,iter=1000)

```

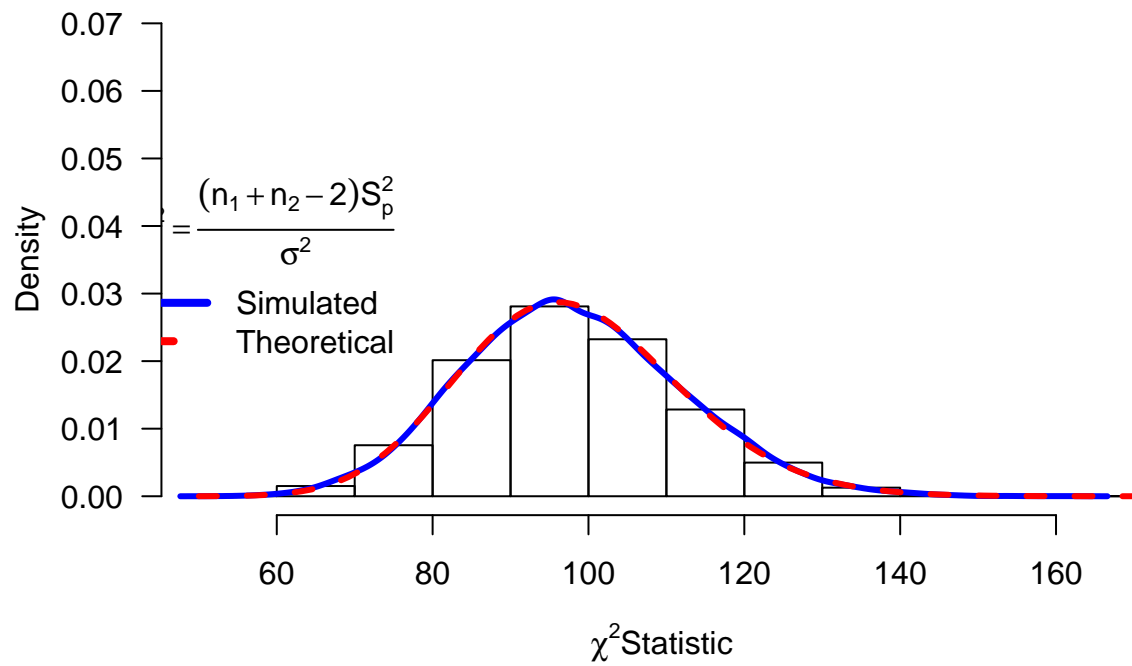
Sample size = $n_1 + n_2 = 20 + 10$ statistic = χ^2



```
## NULL
```

```
mychisim2(n1=50,n2=50,mean1=5,mean2=10,sigma1=4,sigma2=4,iter=10000)
```

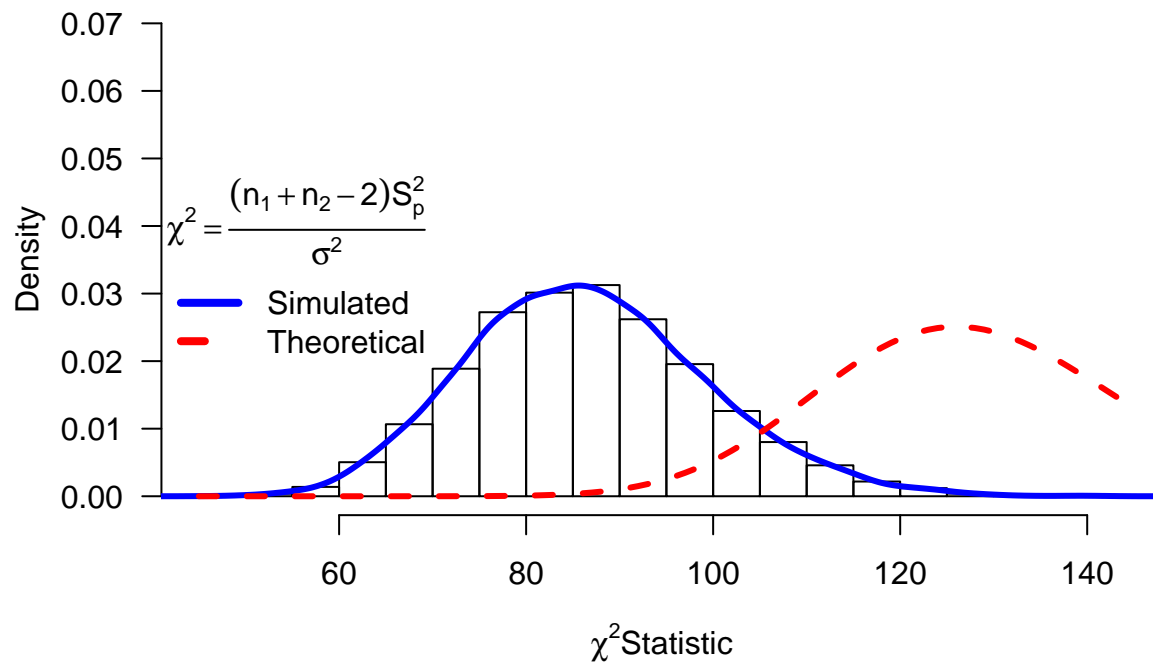
Sample size = $n_1 + n_2 = 50 + 50$ statistic = χ^2



```
## NULL
```

```
mychisim2(n1=80,n2=50,mean1=3,mean2=5,sigma1=10,sigma2=4,iter=10000)
```

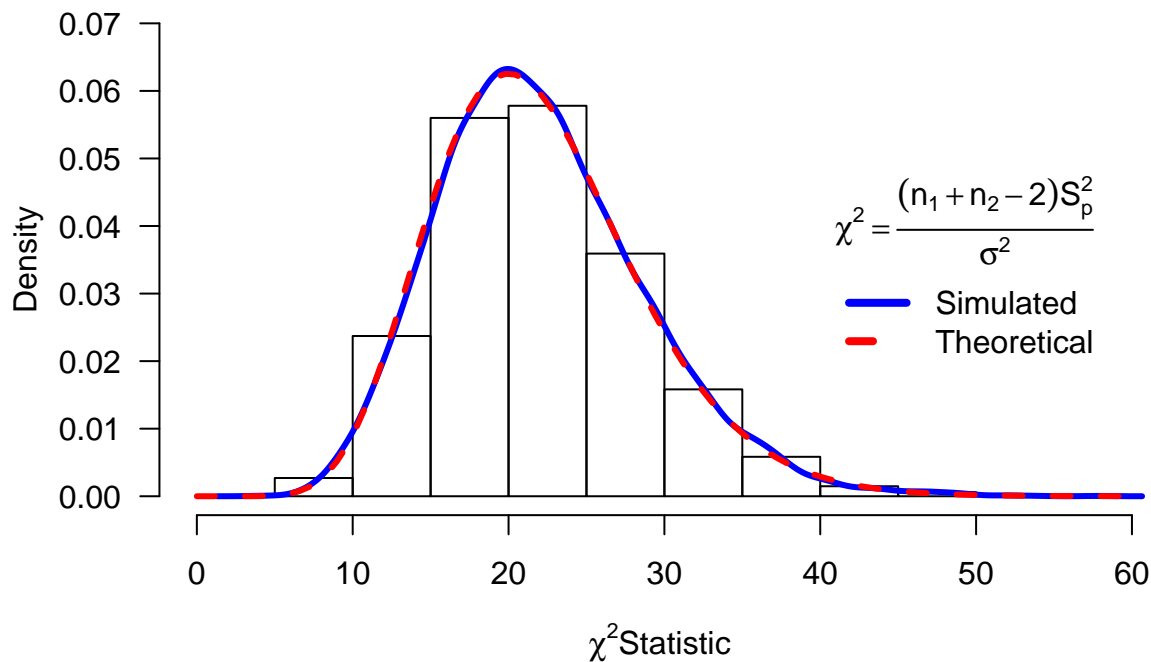
Sample size = $n_1 + n_2 = 80 + 50$ statistic = χ^2



```
## NULL
```

```
mychisim2(iter=10000)
```

Sample size = $n_1 + n_2 = 10 + 14$ statistic = χ^2



NULL

T Distribution with 2 populations

```
myTsim2<-function(n1=10,n2=14,sigma1=3,sigma2=3,mean1=5,mean2=10,iter=1000,ymax=0.5,x=2,y=0.4,...){

  y1=rnorm(n1*iter,mean=mean1,sd=sigma1)# generate iter samples of size n1
  y2=rnorm(n2*iter,mean=mean2,sd=sigma2)

  data1.mat=matrix(y1,nrow=n1,ncol=iter,byrow=TRUE) # Each column is a sample size n1
  data2.mat=matrix(y2,nrow=n2,ncol=iter,byrow=TRUE)

  ssq1=apply(data1.mat,2,var) # ssq1 is s squared
  ssq2=apply(data2.mat,2,var)

  ybar1= apply(data1.mat,2,mean)
  ybar2=apply(data2.mat,2,mean)

  spsq=((n1-1)*ssq1 + (n2-1)*ssq2)/(n1+n2-2) # pooled s squared

  w=((ybar1-ybar2)-(mean1-mean2))/sqrt(spsq*(1/n1+1/n2))#sigma1=sigma2, Chi square stat

  hist(w,freq=FALSE, ylim=c(0,ymax), # Histogram with annotation
        main=substitute(paste("Sample size = ",n[1]+n[2]," = ",n1+n2," statistic = ",T)),
```

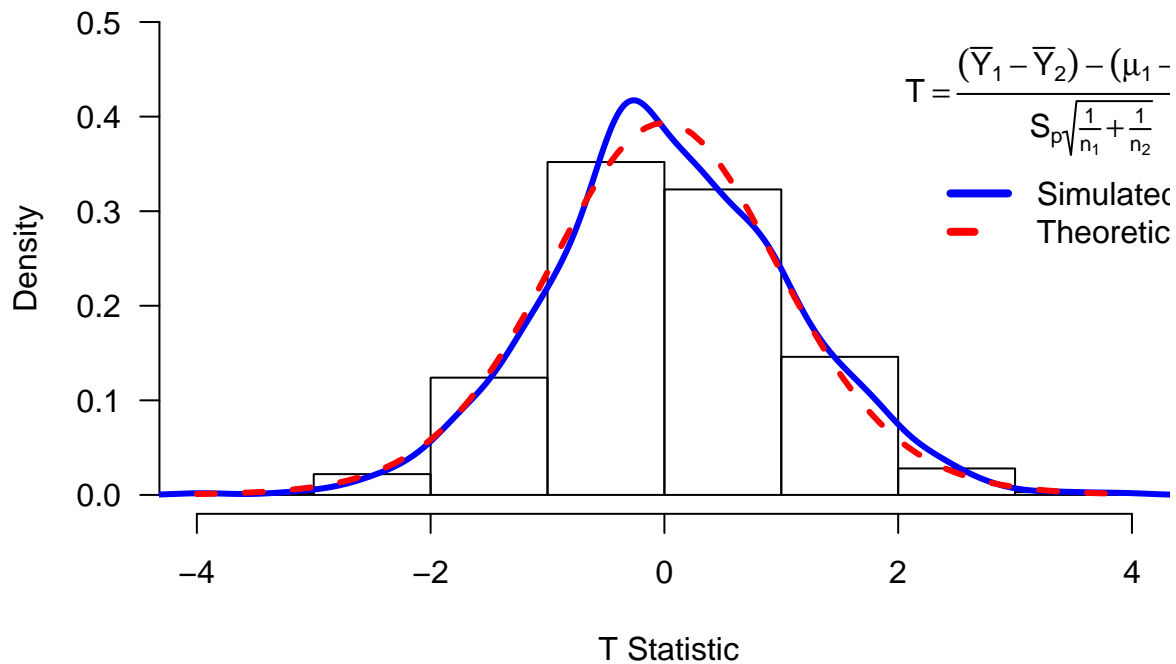


```

      xlab=paste(" T Statistic",sep=""), las=1)
lines(density(w),col="Blue",lwd=3) # add a density plot
curve(dt(x,n1+n2-2),add=TRUE,col="Red",lty=2,lwd=3) # add a theoretical curve
title=expression(T==frac((bar(Y)[1]-bar(Y)[2])-(mu[1]-mu[2]),S[p]*sqrt(frac(1,n[1])+frac(1,n[2])))) #
legend(x,y,c("Simulated","Theoretical"),col=c("Blue","Red"),lwd=4,lty=1:2,bty="n",title=title)# Legend
return()#list(w=w,summary=summary(w),sdw=sd(w),fun="T") # some output to use if needed
}
myTsim2(n1=10,n2=10,mean1=5,mean2=10,sigma1=4,sigma2=4,iter=1000)

```

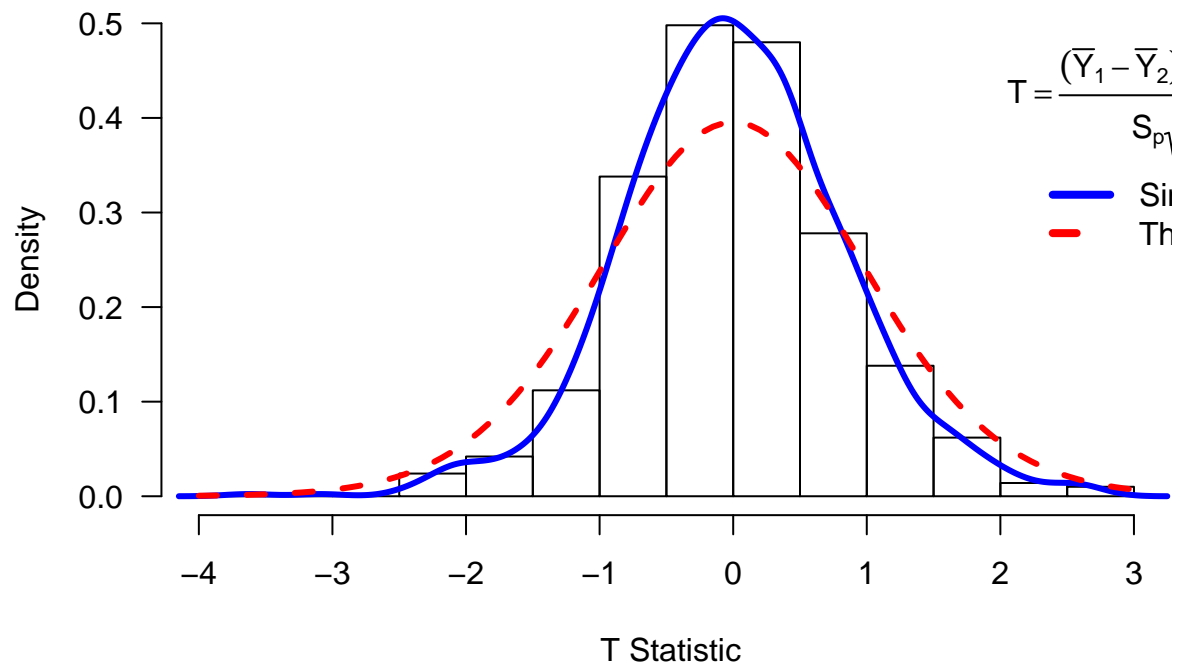
Sample size = $n_1 + n_2 = 10 + 10$ statistic = T



NULL

```
myTsim2(n1=20,n2=10,mean1=3,mean2=5,sigma1=10,sigma2=4,iter=1000)
```

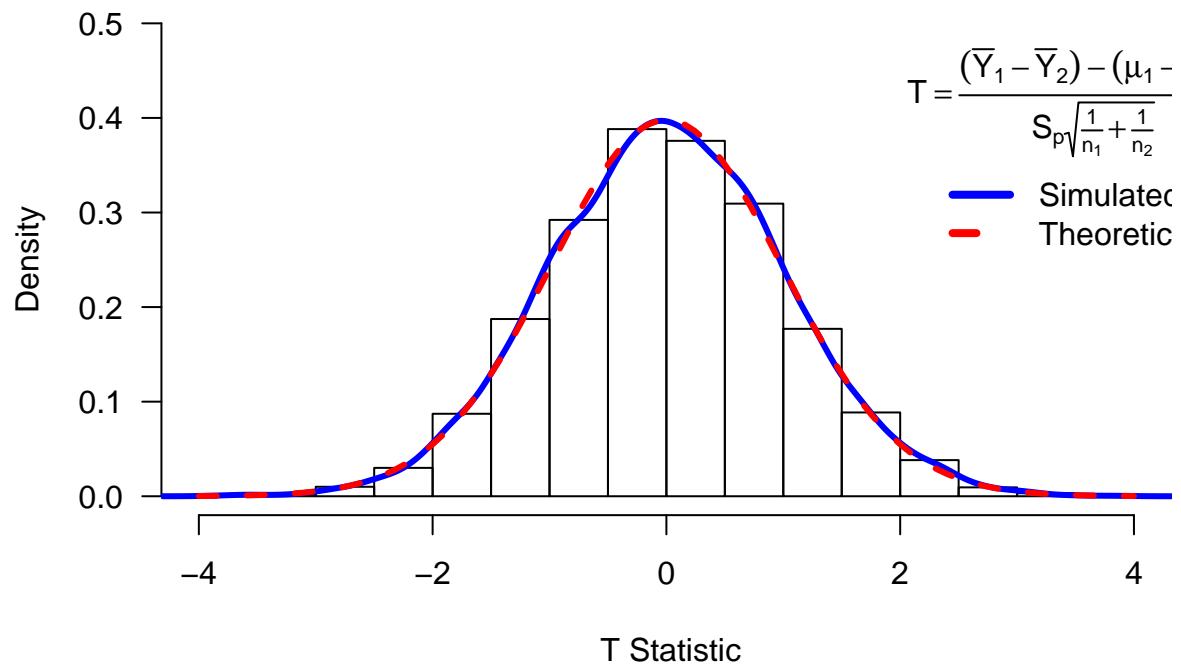
Sample size = $n_1 + n_2 = 20 + 10$ statistic = T



NULL

```
myTsim2(n1=50,n2=50,mean1=5,mean2=10,sigma1=4,sigma2=4,iter=10000)
```

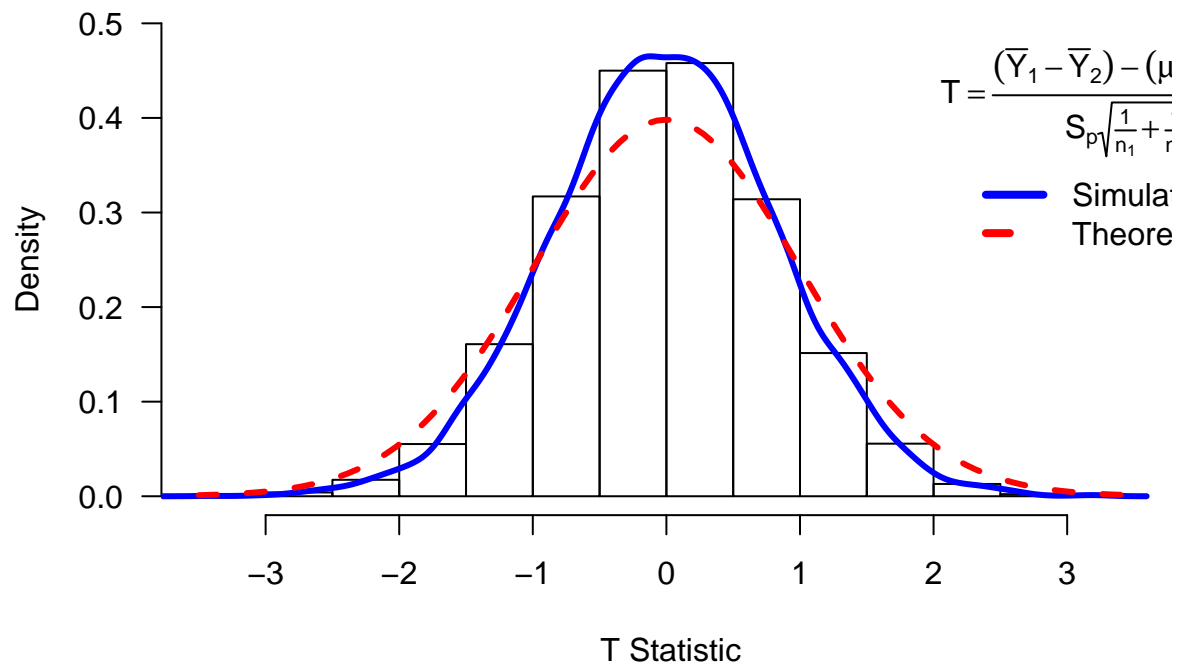
Sample size = $n_1 + n_2 = 50 + 50$ statistic = T



```
## NULL
```

```
myTsim2(n1=80,n2=50,mean1=3,mean2=5,sigma1=10,sigma2=4,iter=10000)
```

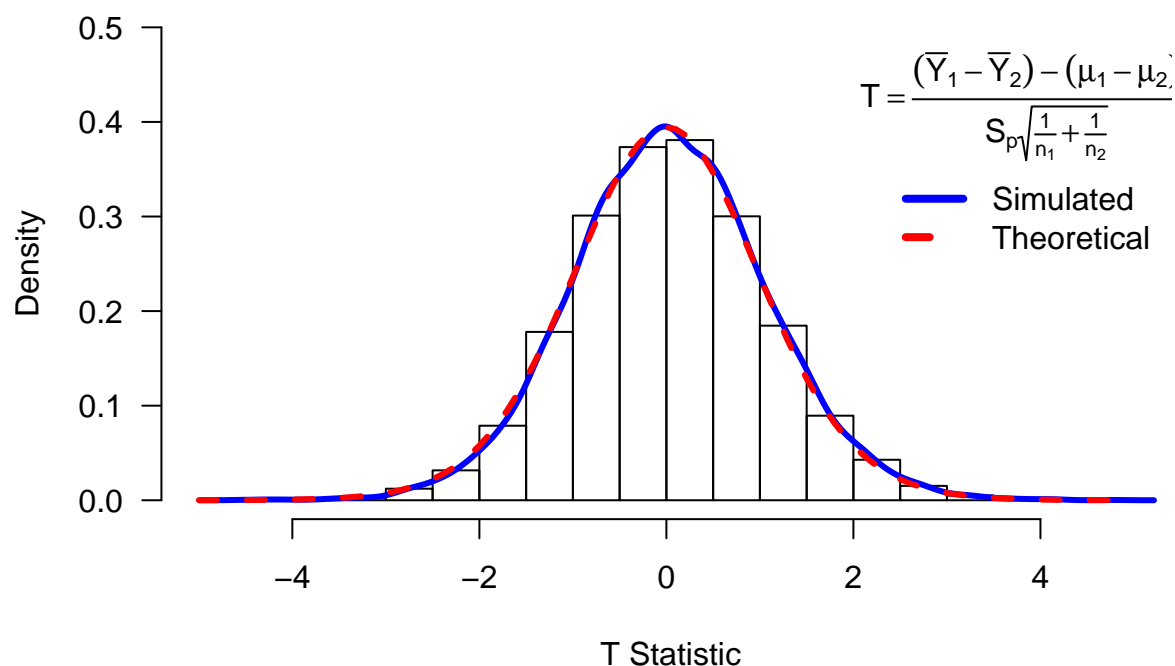
Sample size = $n_1 + n_2 = 80 + 50$ statistic = T



```
## NULL
```

```
myTsim2(iter=10000)
```

Sample size = $n_1 + n_2 = 10 + 14$ statistic = T



NULL

F Distribution with 2 populations

```
myFsim2<-function(n1=10,n2=14,sigma1=3,sigma2=2,mean1=5,mean2=10,iter=1000,ymax=0.9,x=6,y=0.5,...){

  y1=rnorm(n1*iter,mean=mean1,sd=sigma1)# generate iter samples of size n1
  y2=rnorm(n2*iter,mean=mean2,sd=sigma2)

  data1.mat=matrix(y1,nrow=n1,ncol=iter,byrow=TRUE) # Each column is a sample size n1
  data2.mat=matrix(y2,nrow=n2,ncol=iter,byrow=TRUE)

  ssq1=apply(data1.mat,2,var) # ssq1 is s squared
  ssq2=apply(data2.mat,2,var)

  #spsq=((n1-1)*ssq1 + (n2-1)*ssq2)/(n1+n2-2) # pooled s squared

  w=ssq1*sigma2^2/(ssq2*sigma1^2) #

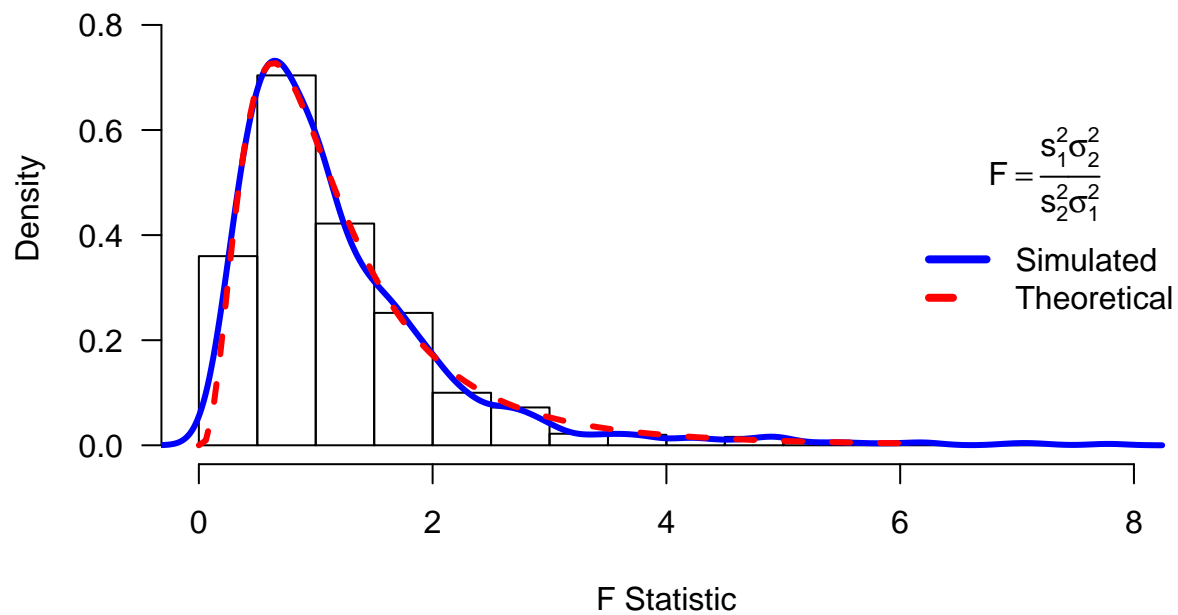
  hist(w,freq=FALSE, ylim=c(0,ymax), # Histogram with annotation
       main=substitute(paste("Sample size = ",n[1]+n[2], " = ",n1+n2," statistic = ",F)),
       xlab=paste("F Statistic",sep=""), las=1)
  lines(density(w),col="Blue",lwd=3) # add a density plot
  curve(df(x,n1-1,n2-1),xlim=c(0,6),add=TRUE,col="Red",lty=2,lwd=3) # add a theoretical curve
}
```

```

title=expression(F==frac(s[1]^2,s[2]^2)*frac(sigma[2]^2,sigma[1]^2)) #mathematical annotation -see ?p
legend(x,y,c("Simulated","Theoretical"),col=c("Blue","Red"),lwd=4,lty=1:2,bty="n",title=title)# Legen
return() #list(w=w,summary=summary(w),sd=sd(w),fun="F") # some output to use if needed
}
myFsim2(n1=10,n2=10,mean1=5,mean2=10,sigma1=4,sigma2=4,iter=1000)

```

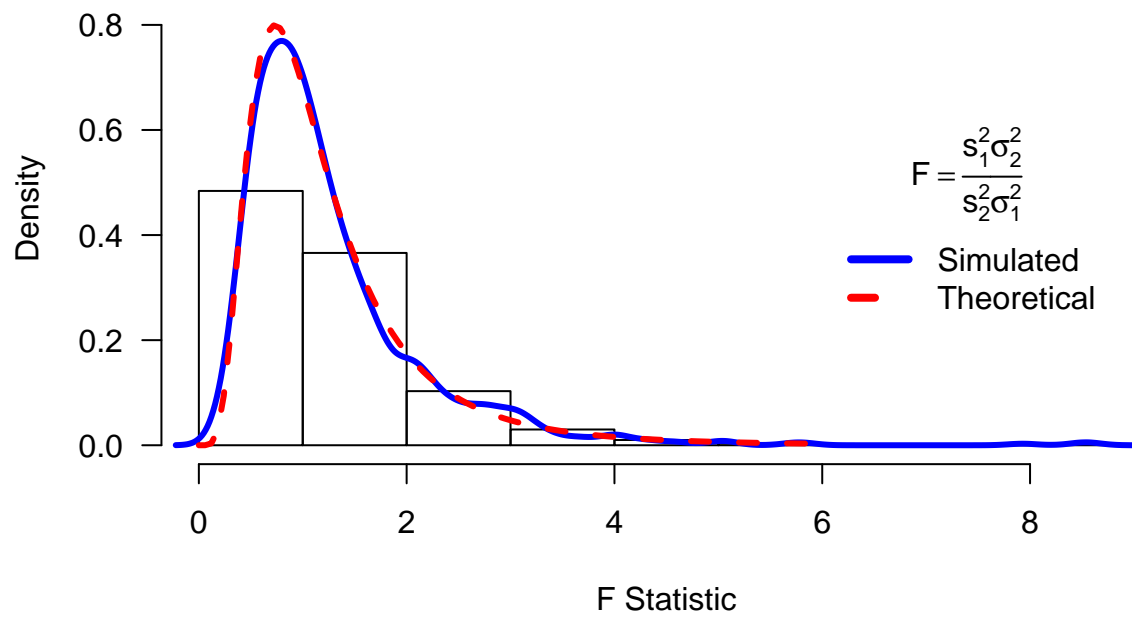
Sample size = $n_1 + n_2 = 10 + 10$ statistic = F



NULL

```
myFsim2(n1=20,n2=10,mean1=3,mean2=5,sigma1=10,sigma2=4,iter=1000)
```

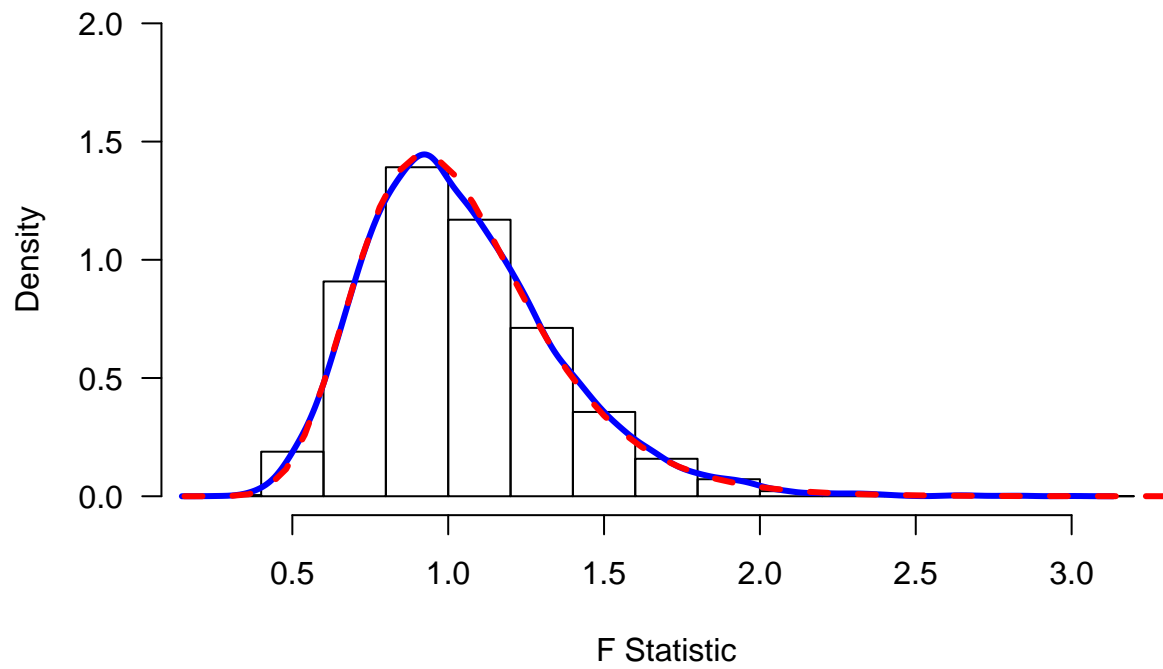
Sample size = $n_1 + n_2 = 20 + 10$ statistic = F



```
## NULL
```

```
myFsim2(n1=50,n2=50,mean1=5,mean2=10,sigma1=4,sigma2=4,iter=10000, ymax=2)
```

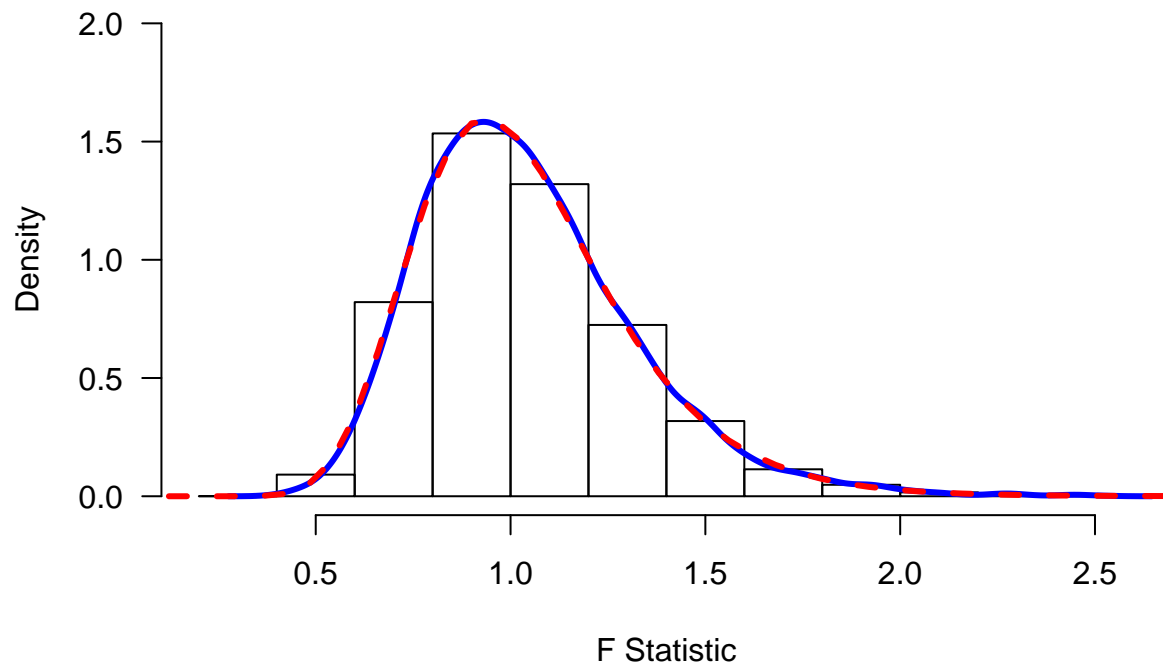
Sample size = $n_1 + n_2 = 50 + 50$ statistic = F



```
## NULL
```

```
myFsim2(n1=80,n2=50,mean1=3,mean2=5,sigma1=10,sigma2=4,iter=10000, ymax=2)
```

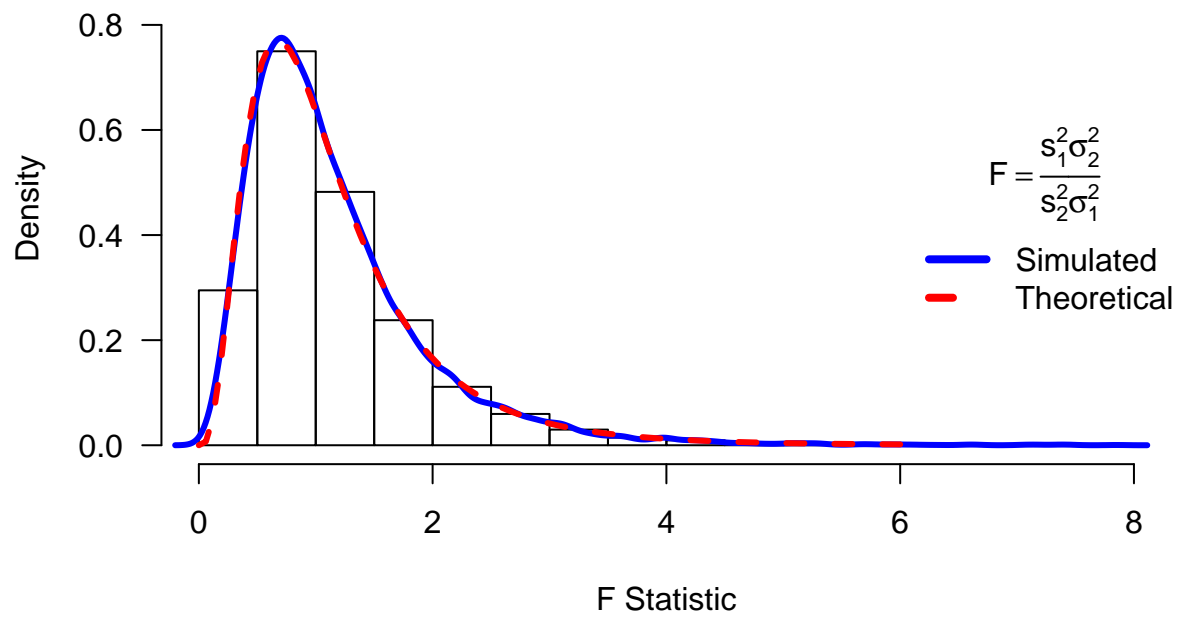

Sample size = $n_1 + n_2 = 80 + 50$ statistic = F



```
## NULL
```

```
myFsim2(iter=10000)
```

Sample size = $n_1 + n_2 = 10 + 14$ statistic = F



NULL

In F distribution, we assume the data points are independent from one another.